$$C = \sqrt{g(H-\alpha)} = \sqrt{g\frac{H-\alpha}{H}H} = \sqrt{g'H}$$