$$
\begin{aligned}
u &= \hat{u} e^{ik(x - c_n t)} \\
&= \hat{u} \left\{ e^{ik(x - c_{n,\mathrm{real}} t)} + e^{k c_{n,\mathrm{imag}} t} \right\}
\end{aligned}
$$