$$\omega \sim \pm\sqrt{c^2k^2 + c\beta(2n+1)}$$