$$\omega^2 - c^2k^2 - c^2\beta\frac{k}{\omega} = c\beta(2n+1)$$