$$\omega = ck/2 + \sqrt{(ck/2)^2 + \beta c}$$

$$\omega = ck/2 - \sqrt{(ck/2)^2 + \beta c}$$