$$\omega \sim -\frac{\beta k}{k^2 + \beta(2n+1)/c}$$