

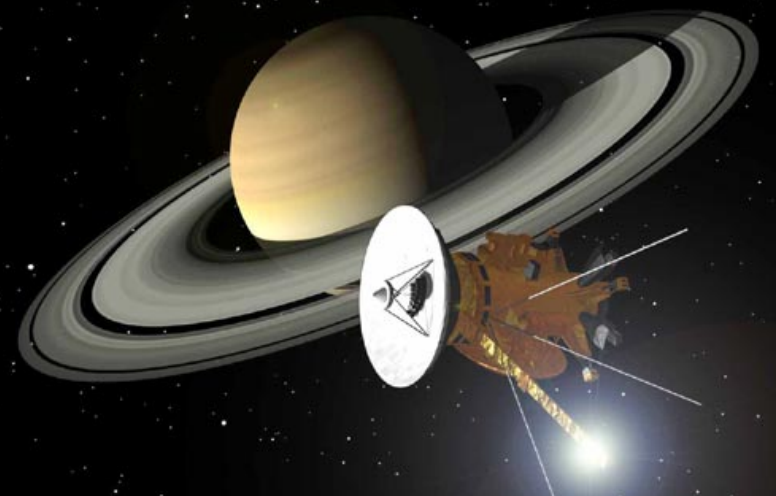


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Dust-plasma interaction in Saturn's inner magnetosphere and its magnetosphere-ionosphere coupling

Shotaro Sakai

Department of Natural History Sciences,
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1. Introduction
 1. Saturn's system
 2. Plasma and dust in Saturn's inner magnetosphere
 3. Modeling of the inner magnetosphere
2. Modeling of the ionosphere
3. Magnetosphere-ionosphere coupling
4. Summary



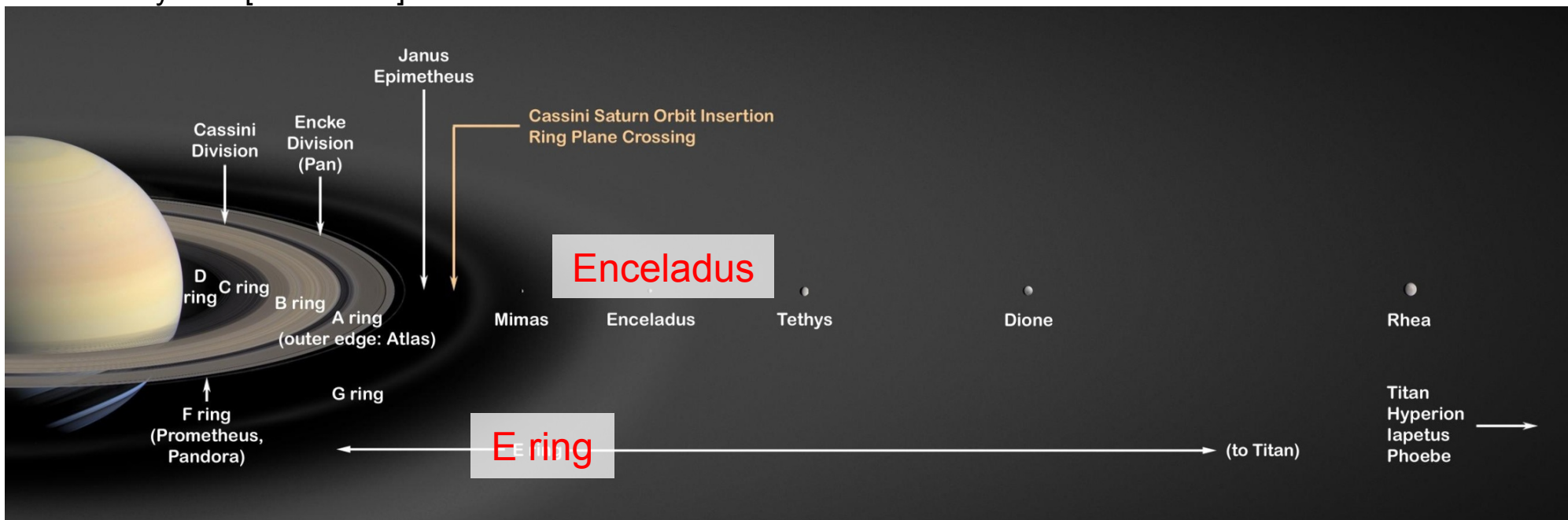
Introduction

Saturn's system



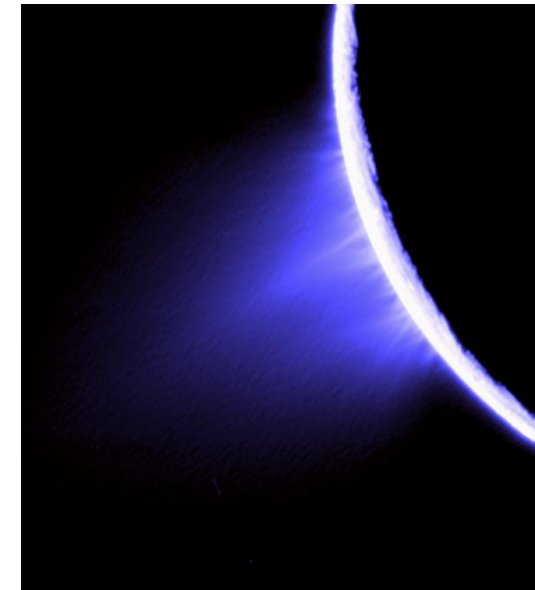
- Equatorial radius: 60,268 km (1 R_s)
- Mass: 5.68×10^{26} kg
- Equatorial gravity: 10.44 m/s^2
- Rotation period: 0.436 day
- Revolution period: 29.46 year
- Magnetic moment: $4.6 \times 10^{18} \text{ T/m}^3$
- Tilt of magnetic axis respect to rotational axis: $< 1^\circ$
- Satellites#: 64
- Rings: D, C, B, A, F, G and E
- Exploration of Saturn: Pioneer 11, Voyager 1 and 2, Cassini

Saturn's system [NASA/JPL]

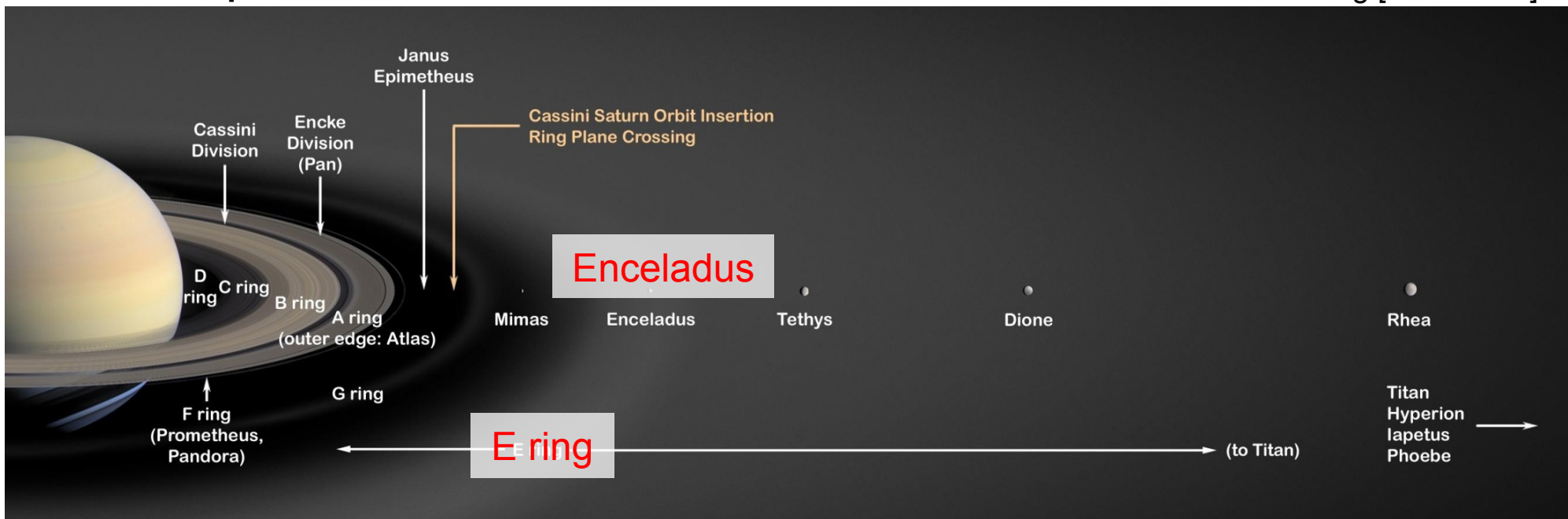


Enceladus plume & E ring

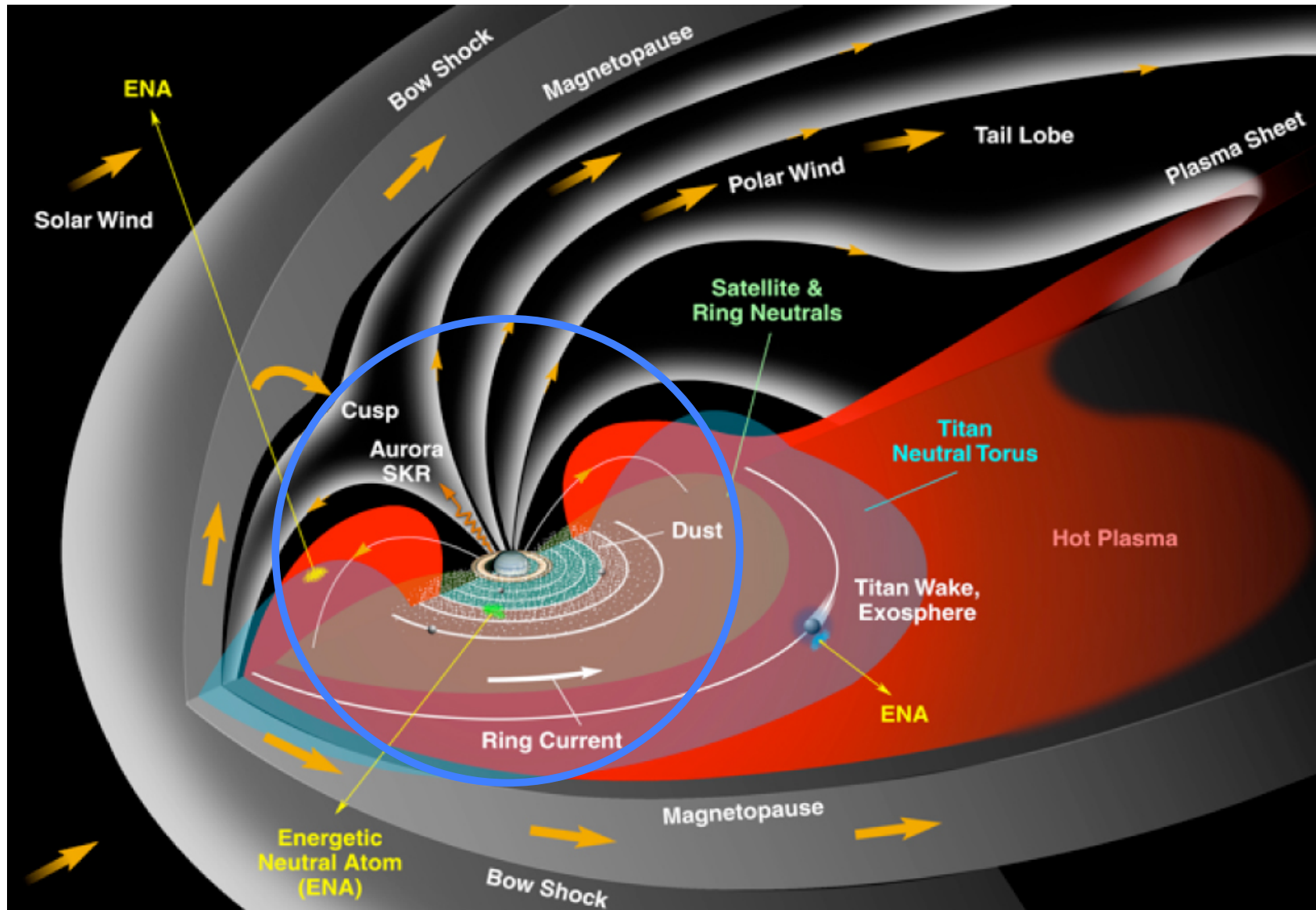
- Enceladus plume (~3.95 Rs)
 - Water gas
- E ring
 - 3 – 8 Rs
 - Water group ion
 - Dust
 - Source: **Mainly Enceladus plume**
 - Kepler motion



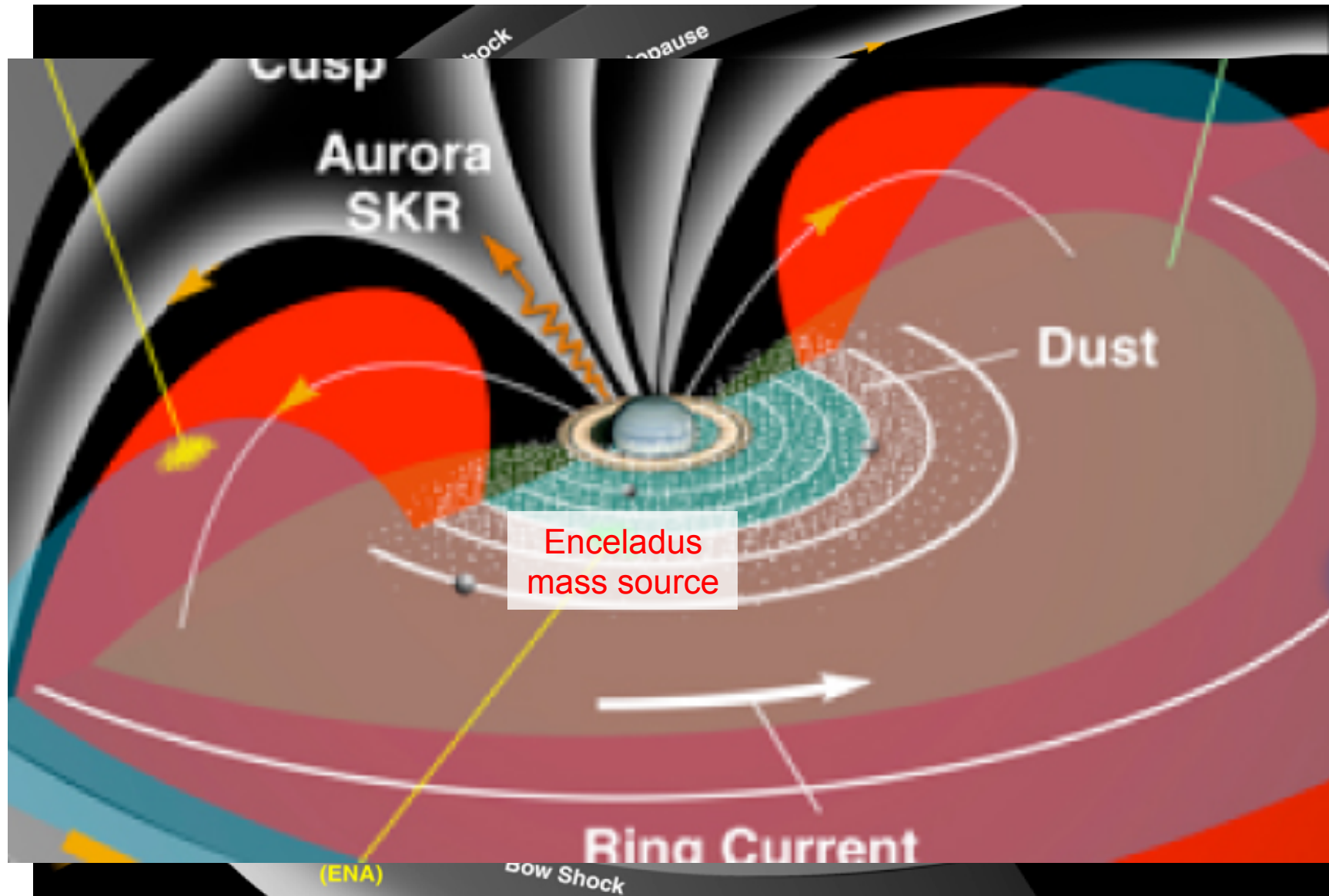
Enceladus & E ring [NASA/JPL]



Saturn's magnetosphere



Saturn's magnetosphere



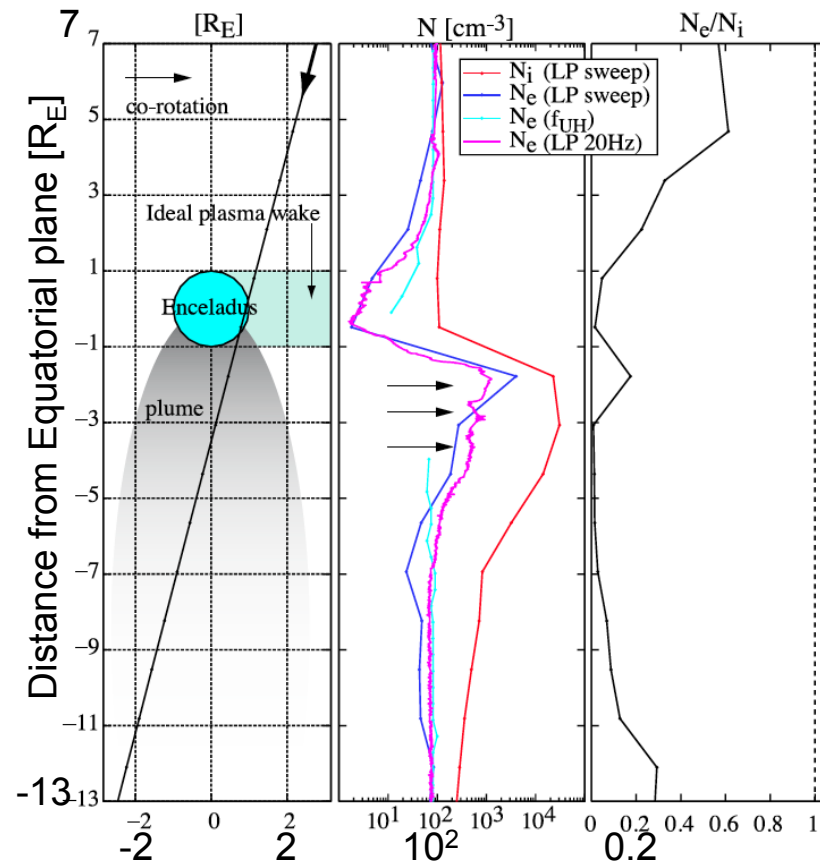
Why Saturn?



- Quite different from Earth's magnetosphere
 - Source of plasma
 - Satellites and rings [*Moncuquet et al.*, 2005; *Persoonet al.*, 2005; *Wahlund et al.*, 2005; *Sittler et al.*, 2006]
 - **Enceladus plume** [*Porco et al.*, 2006; *Waite et al.*, 2006]
 - Dust
 - Charged dust of E ring from satellites [*Wahlund et al.*, 2005, 2009]
 - Also different from Jovian magnetosphere
 - Dust is also existence [*Johnson et al.*, 1980; *Morfill et al.*, 1980].
 - **Acceleration of dust by the magnetic force** [*Horányi et al.*, 1993]
 - Strong magnetic field (200 times than Saturn's)
- Plasma can affect dust in Saturn's magnetosphere!!
- Because of smaller magnetic field

Electron depletion

- Electron depletion
 - $N_i > N_e$
 - $N_e/N_i < 1\%$ [Morooka et al., 2011].
 - Negatively charged dust? [Wahlund et al., 2009; Morooka et al., 2011]



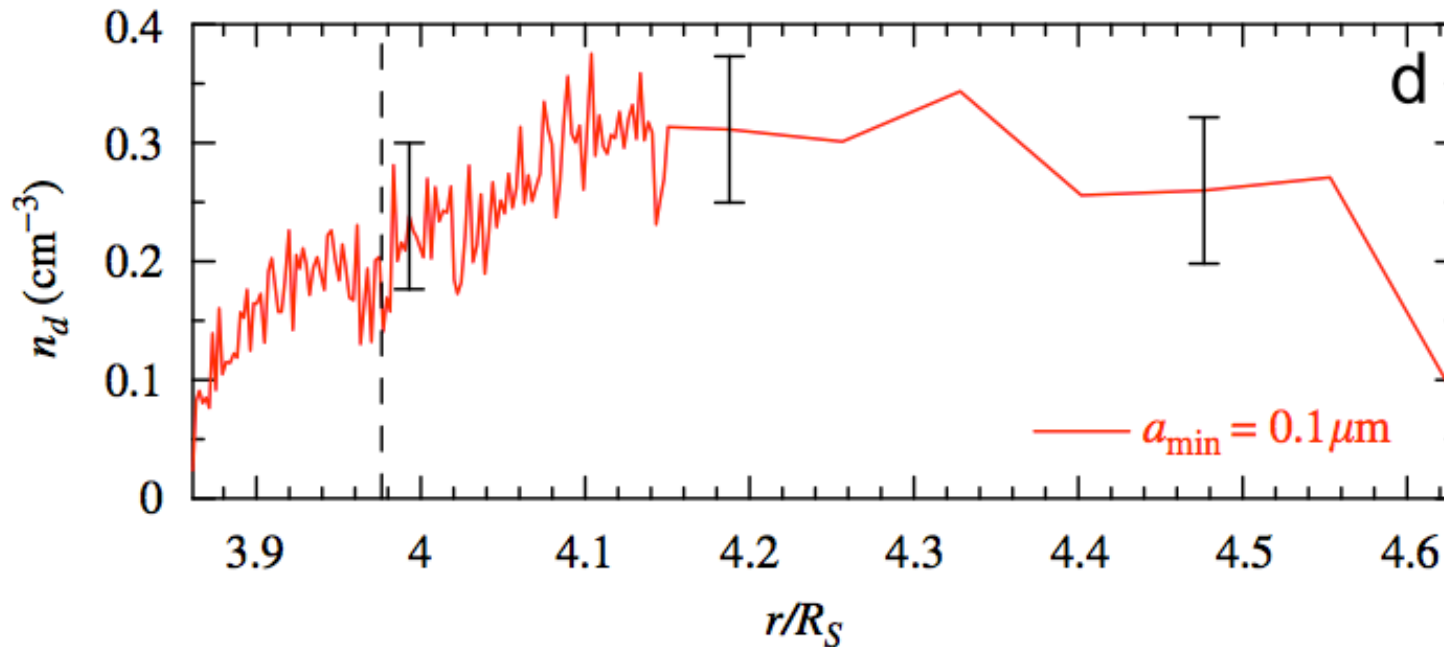
E03 Density profile [Morooka et al., 2011]

Dusts around Enceladus



- Total dust density: 10^4 — 10^7 m⁻³

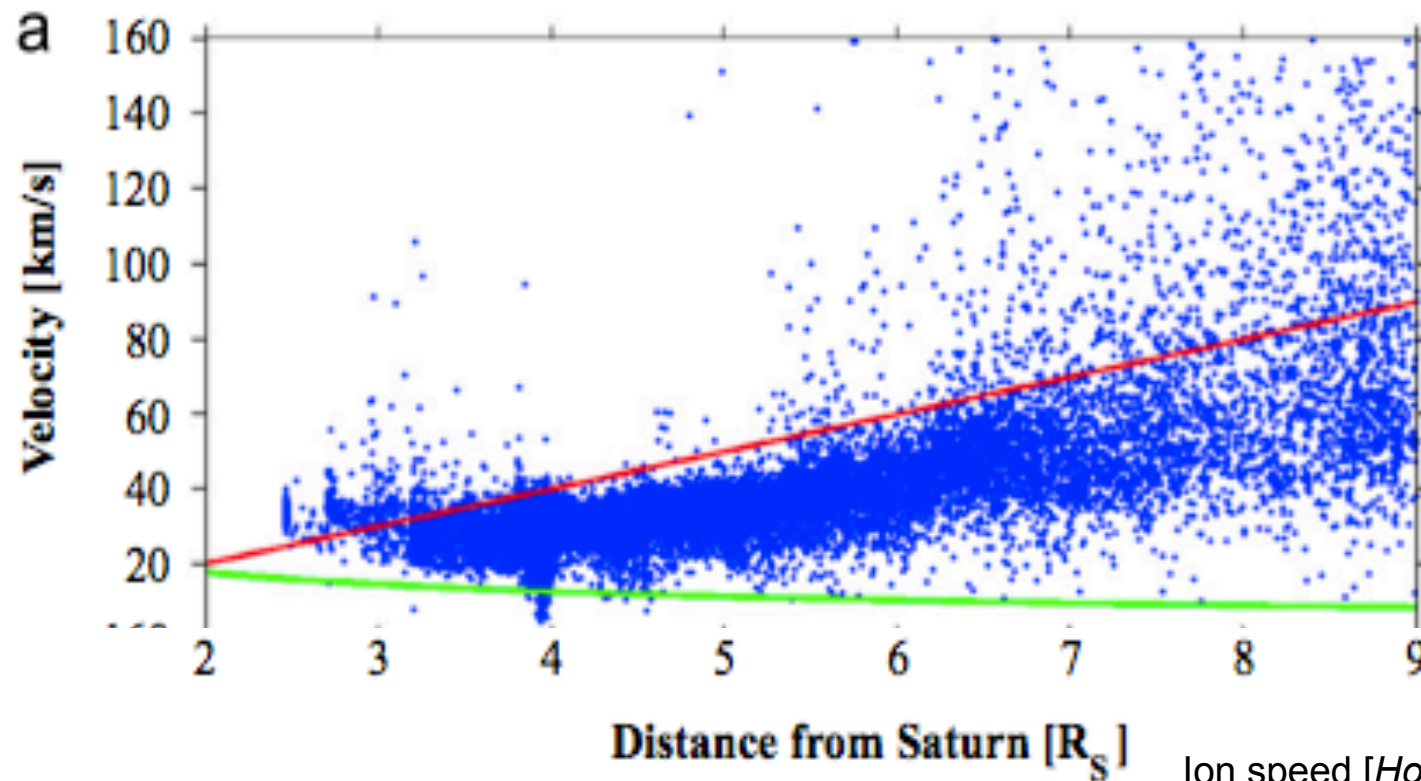
$$n_{dtot} = \int_{r_{min}}^{r_{max}} n_d(r_d) dr_d \approx \frac{e(n_i - n_e)}{4\pi\epsilon_0 U_{SC}} \frac{2 - \mu}{1 - \mu} \frac{1}{r_{min}}$$



Co-rotation deviation by dusts?



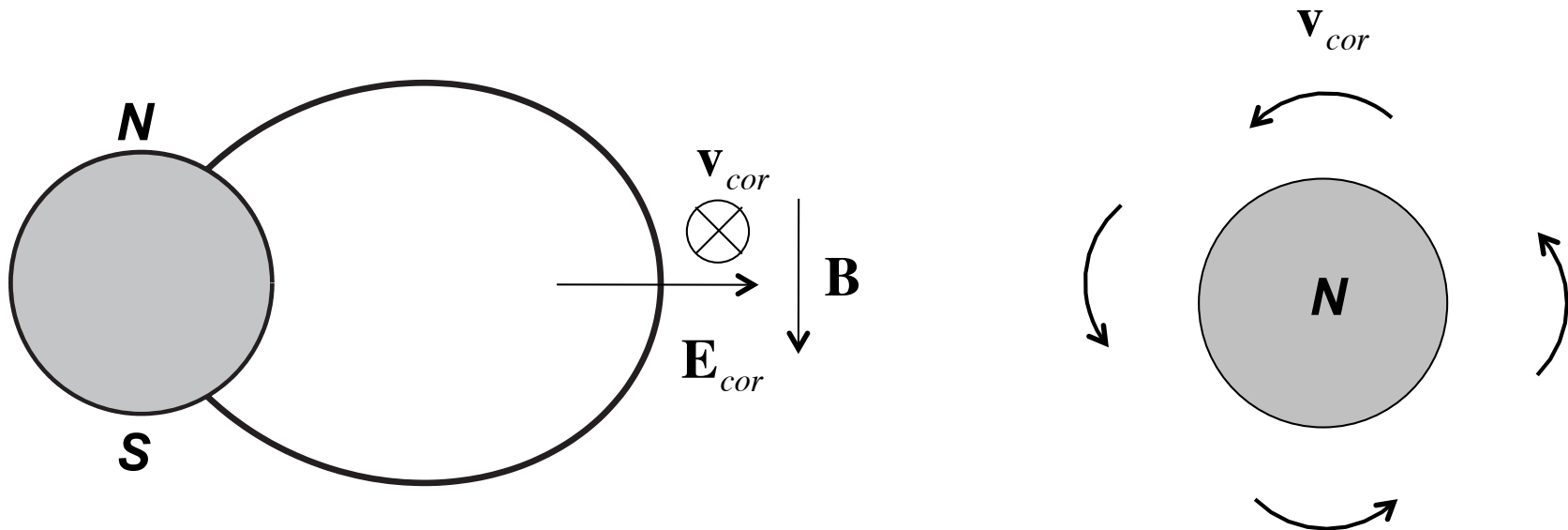
- Ion observations from the Cassini RPWS/LP in Saturn's magnetosphere
 - $V_i < V_{\text{cor}}$ [Wahlund et al., 2009; Morooka et al., 2011; Holmberg et al., 2012].



- Magnetospheric plasma should be **co-rotating**.

Co-rotation velocity:
$$\mathbf{v}_{cor} = \frac{\mathbf{E}_{cor} \times \mathbf{B}}{B^2}$$

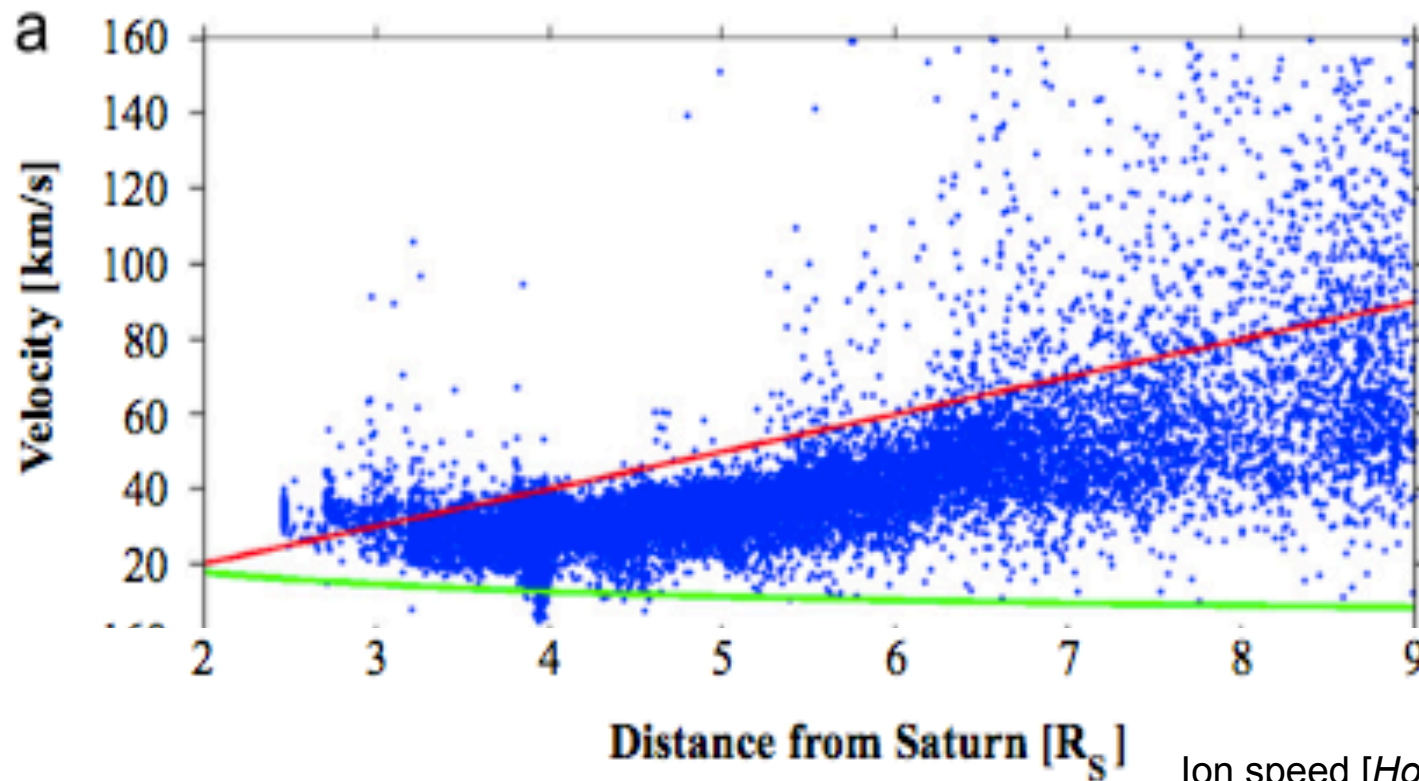
Saturn's case



Co-rotation deviation by dusts?



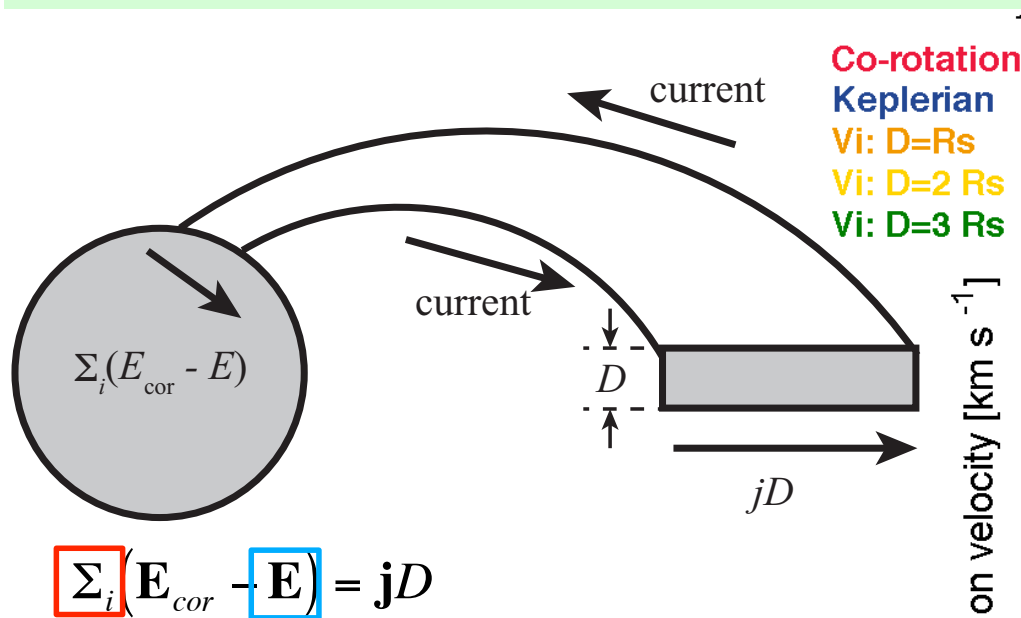
- Ion observations from the Cassini RPWS/LP in Saturn's magnetosphere
 - $V_i < V_{\text{cor}}$ [Wahlund et al., 2009; Morooka et al., 2011; Holmberg et al., 2012].
 - Dusts affect V_i in the inner magnetosphere?



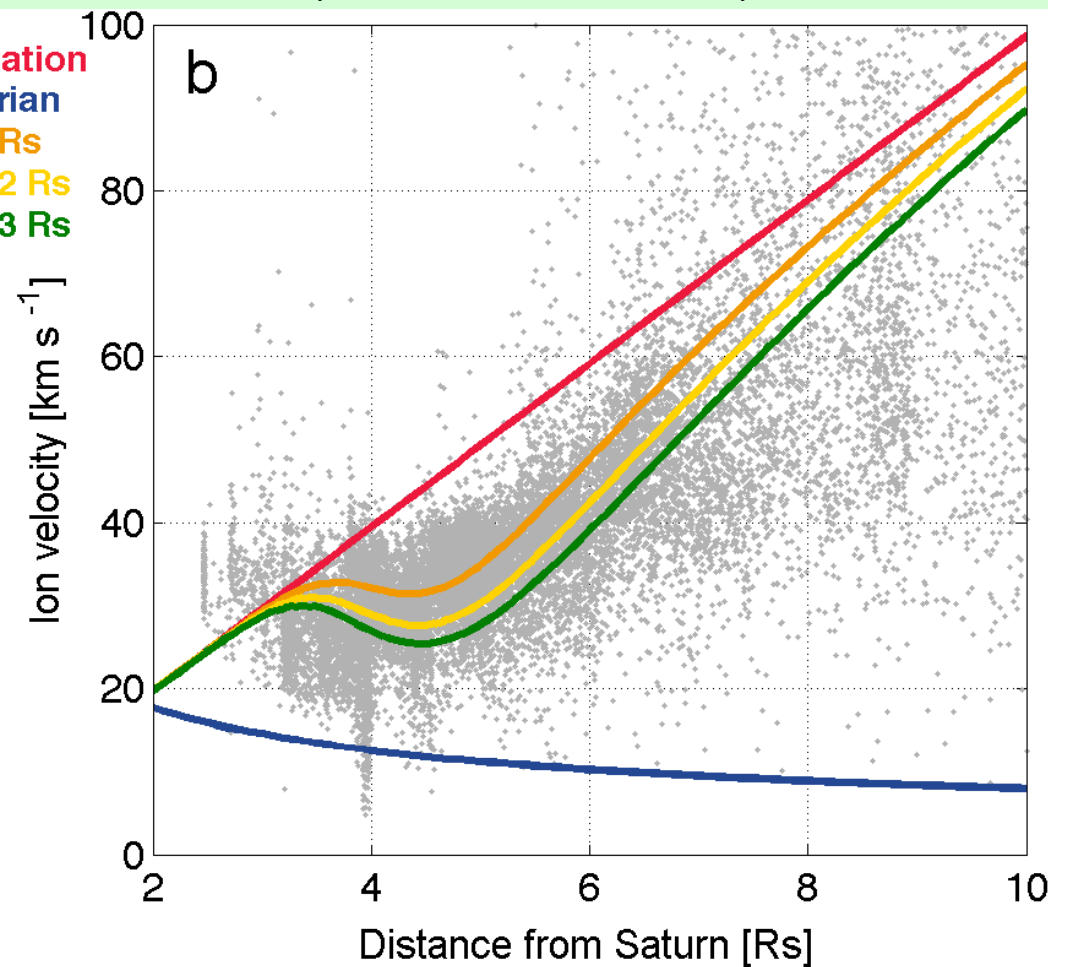
Comparison with LP observation



$$\rho_k \frac{\partial \mathbf{v}_k}{\partial t} + \rho_k (\mathbf{v}_k \cdot \nabla) \mathbf{v}_k = n_k q_k (\mathbf{E} + \mathbf{v}_k \times \mathbf{B}) - \nabla p_k - \rho_k \mathbf{g} + \sum_l \rho_k \mathbf{v}_{kl} (\mathbf{v}_k - \mathbf{v}_l) - \sum_l S_{k,l} (\mathbf{v}_k - \mathbf{v}_l)$$



- $\mathbf{j}_{mag,tot}$ weakens \mathbf{E} .



Magnetospheric ion velocity [Sakai et al., 2013]

Inner magnetospheric model

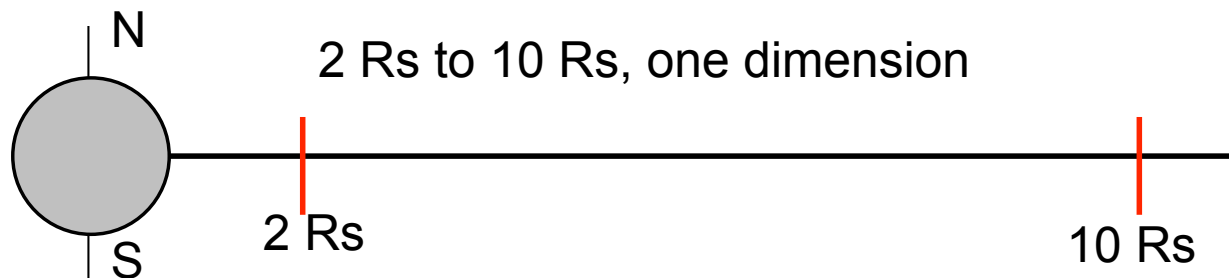


- Momentum equations
 - H^+ , H_2O^+ , e^- and dust

$$\rho_k \frac{\partial \mathbf{v}_k}{\partial t} + \rho_k (\mathbf{v}_k \cdot \nabla) \mathbf{v}_k = n_k q_k (\mathbf{E} + \mathbf{v}_k \times \mathbf{B}) - \nabla p_k - \rho_k \mathbf{g} + \sum_l \rho_k \nu_{kl} (\mathbf{v}_k - \mathbf{v}_l) - \sum_l S_{k,l} (\mathbf{v}_k - \mathbf{v}_l)$$

Electric field
Collision term
Chemical term

- Dust: $q_d = 4\pi\epsilon_0 r_d \phi$
 - $r_d = 100 \text{ nm}$; $\phi = -2 \text{ V}$



S_k	Production rate
n_k	Number density
\mathbf{B}	Magnetic field
q_d	Charge quantity of dust
r_d	Dust radius
ϕ	Dust surface potential
ϵ_0	Permittivity

\mathbf{v}_k	Velocity
\mathbf{E}	Electric field
\mathbf{g}	Gravity
ρ_k	Mass density
p	Pressure
e	Charge quantity
ν_{kl}	Collision frequency

- M-I coupling for deriving **electric field, E**

$$\Sigma_i (\mathbf{E}_{cor} - \mathbf{E}) = \mathbf{j}D$$

$$\mathbf{j} = en_i \mathbf{v}_i - en_e \mathbf{v}_e - q_d n_d \mathbf{v}_d$$

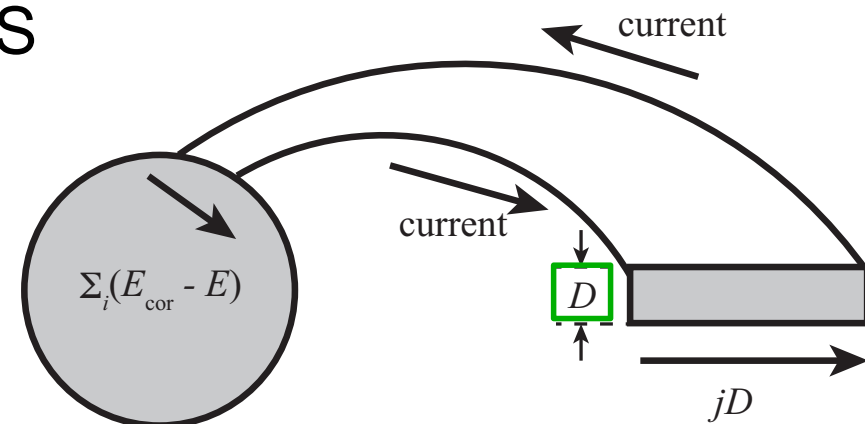
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$$\mathbf{E} = \mathbf{E}_{cor} - \frac{\mathbf{j}D}{\Sigma_i}$$

Thickness of dust distribution

\mathbf{j}	Current density
\mathbf{E}_{cor}	Co-rotational Electric field
Σ_i	Ionospheric conductivity
D	Thickness of dust
v_{thk}	Thermal velocity

- Ionospheric conductivity Σ_i : 1 S



Comparison with LP observation



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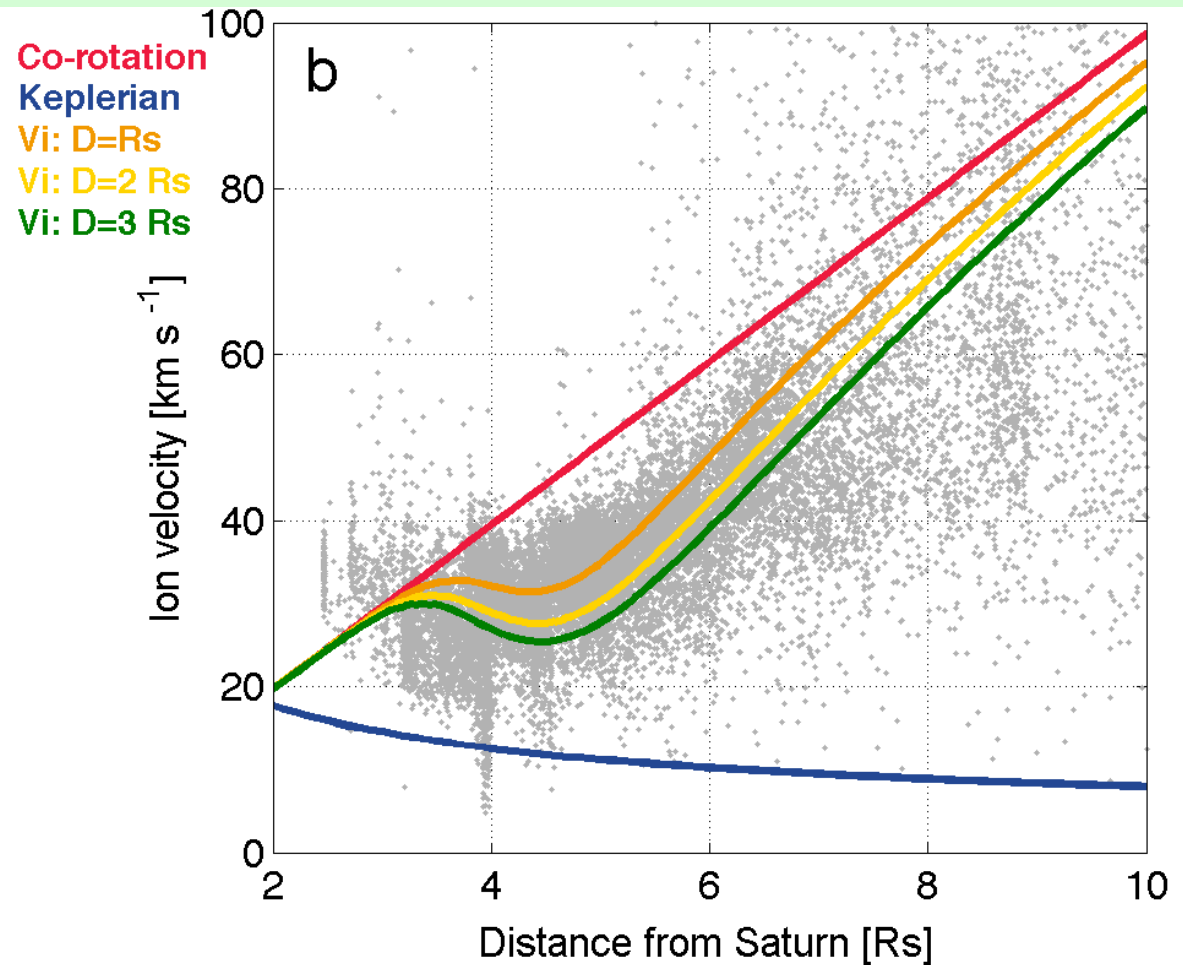
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$$\mathbf{E} = \mathbf{E}_{cor} - \frac{\mathbf{j}D}{\Sigma_i}$$

$$\mathbf{v}_i \approx \frac{\mathbf{E} \times \mathbf{B}}{B^2}$$

$$< \mathbf{v}_{cor}$$

- $\mathbf{j}_{mag,tot}$ weakens \mathbf{E} .



Magnetospheric ion velocity [Sakai et al., 2013]

Comparison with LP observation



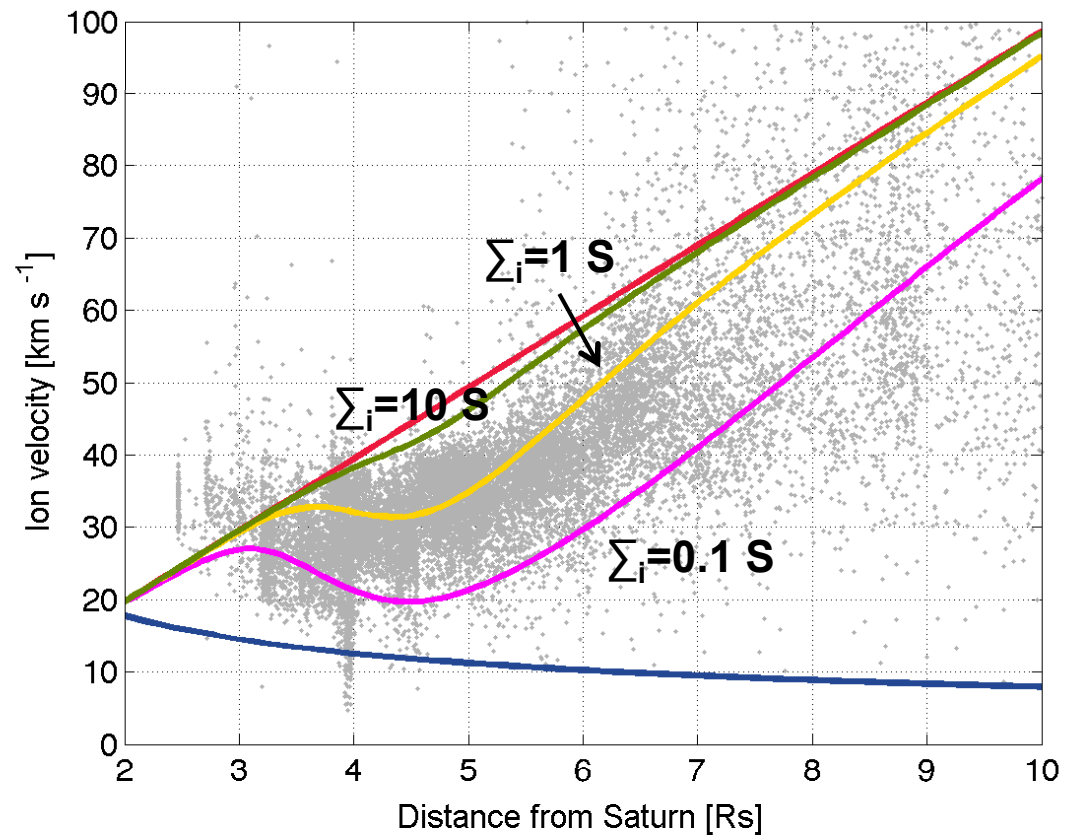
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$$\mathbf{E} = \mathbf{E}_{cor} - \frac{jD}{\Sigma_i}$$

$$\mathbf{v}_i \approx \frac{\mathbf{E} \times \mathbf{B}}{B^2}$$

$$< \mathbf{v}_{cor}$$

- 3 cases for Σ_i
 - 0.1 S
 - 1 S
 - 10 S
- V_i is slower when Σ_i is smaller.
- V_i strongly depends on Σ_i .



Co-rotation deviation by dusts?



- Ionospheric Pedersen conductivity
 - E depends on the conductivity.

$$\rho_k \frac{\partial \mathbf{v}_k}{\partial t} + \rho_k (\mathbf{v}_k \cdot \nabla) \mathbf{v}_k = n_k q_k (\mathbf{E} + \mathbf{v}_k \times \mathbf{B}) - \nabla p_k - \rho_k \mathbf{g} + \sum_l \rho_k \nu_{kl} (\mathbf{v}_k - \mathbf{v}_l) - \sum_l S_{k,l} (\mathbf{v}_k - \mathbf{v}_l)$$

Electric field

$$\sum_i (\mathbf{E}_{cor} - \mathbf{E}) = \mathbf{j}D$$

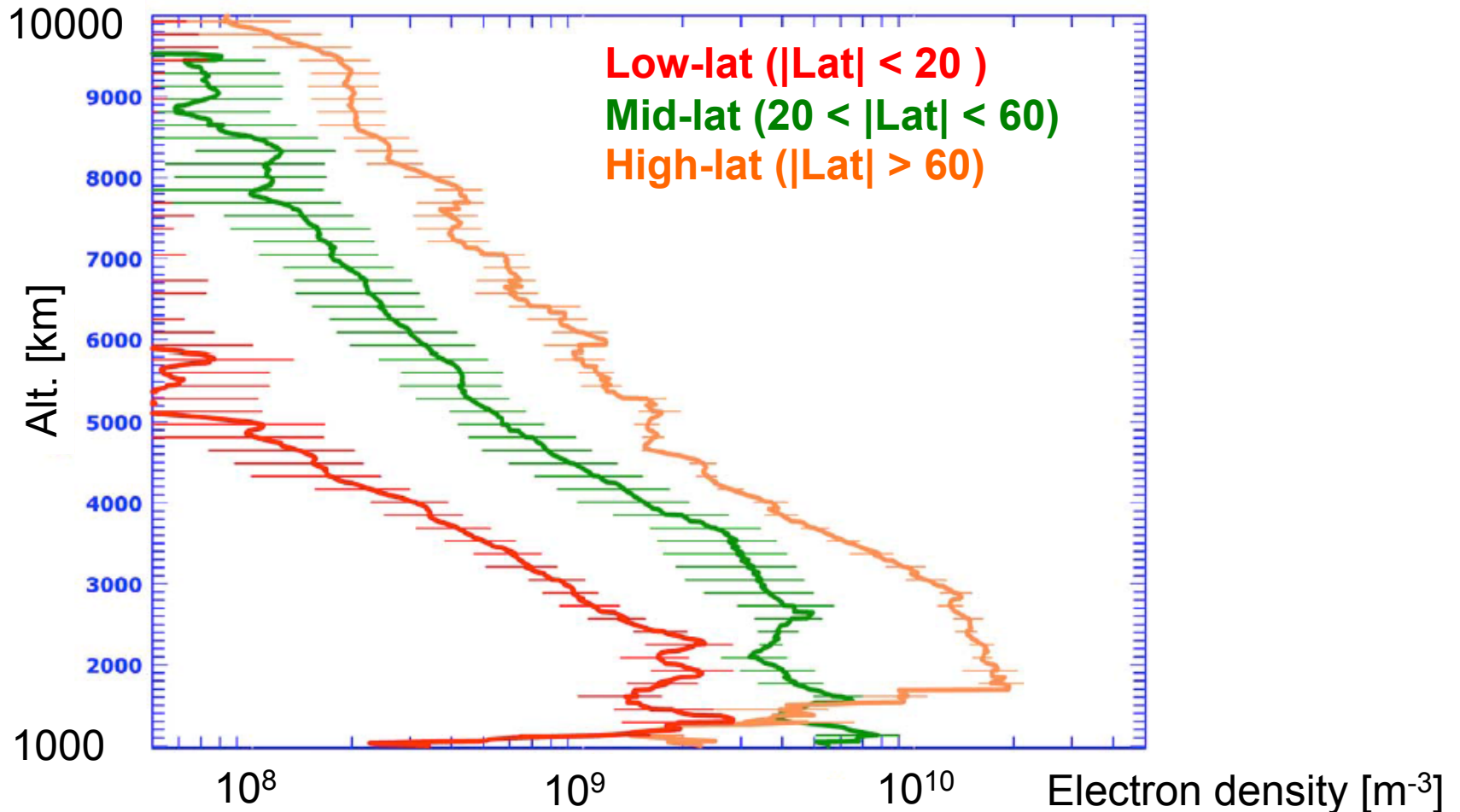
Pedersen conductivity

$$\sigma_p = \sum_i \frac{\nu_i}{\nu_{in}^2 + \omega_{ci}^2} \frac{n_i e^2}{m_i} + \frac{\nu_e}{\nu_{en}^2 + \omega_{ce}^2} \frac{n_e e^2}{m_e} \quad \Sigma_i = \int_{z_1}^{z_2} \sigma_p ds$$

- One of the open questions.
 - ~0.1-100 S [Connerney *et al.*, 1983; Cheng and Waite, 1988]
 - ~0.02 S [Saur *et al.*, 2004]
 - 1--10 S [Cowley *et al.*, 2004; Moore *et al.*, 2010]
- Estimate the ionospheric N_i for deriving Σ_i .

Saturn's ionosphere

- N_e observation from Cassini occultations
 - N_e (average between dusk and dawn)
 - Peak density: $\sim 10^{10} \text{ m}^{-3}$; Peak alt.: $\sim 1200 \text{ km}$

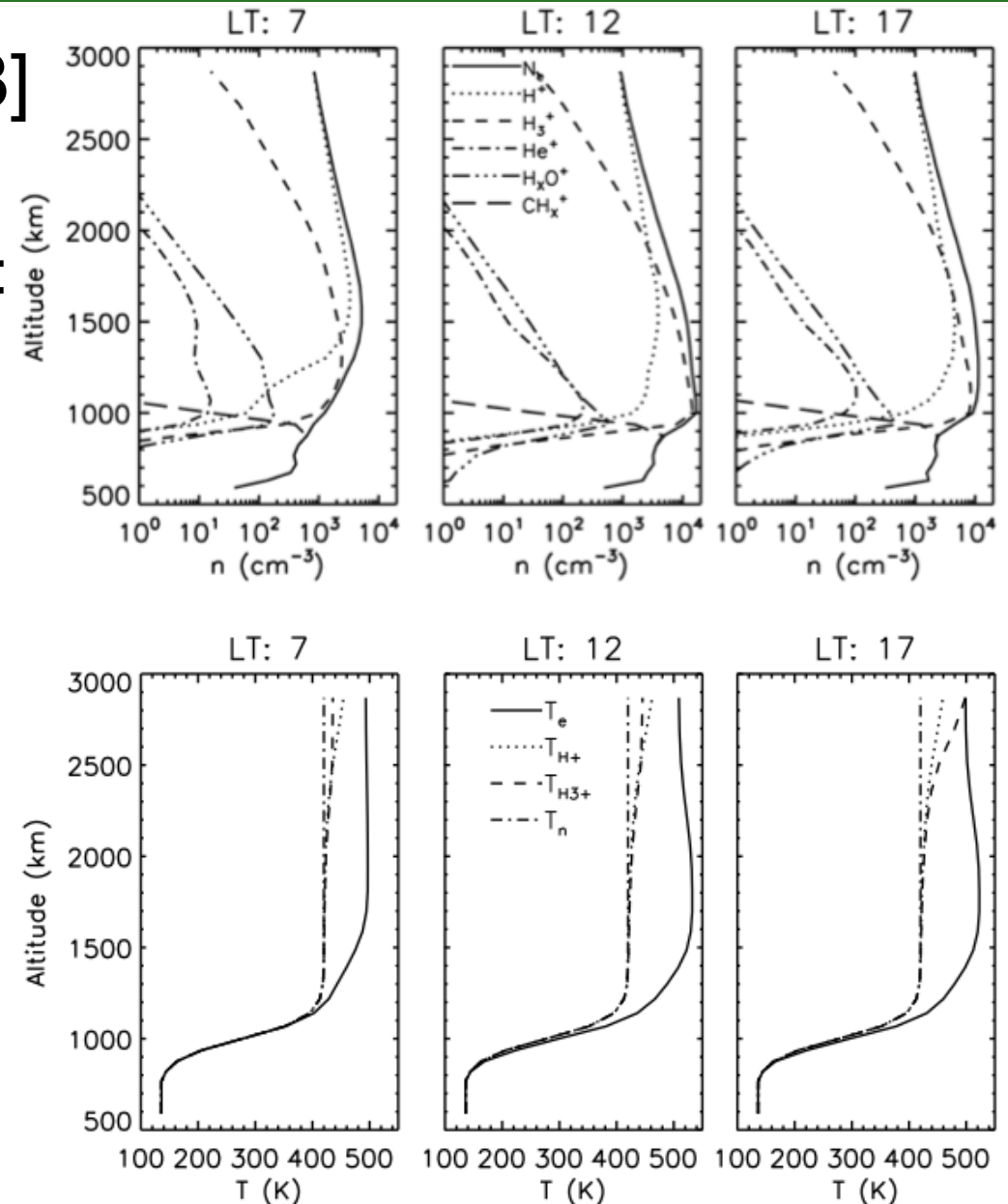


Electron density by occultations [*Kliore et al.*, 2009]

Saturn's ionosphere



- Model [*Moore et al. 2008*]
 - N_e
 - Average peak density: $\sim 10^{10} \text{ m}^{-3}$
 - Peak alt.: $\sim 1200 \text{ km}$
 - T_e
 - Max: 500 K
 - Alt.: $> 1500 \text{ km}$
- Only below $\sim 3000 \text{ km}$
 - Magnetospheric effect?



Plasma density and temperature by modeling [*Moore et al., 2008*]

- Construction of an ionospheric model including the inner magnetosphere.
- Estimation of the **ionospheric Pedersen conductivity** from **plasma density** in the Saturn's ionosphere
- Investigation of the influence of magnetosphere to ionosphere



Modeling of the ionosphere

3 dimensional ionospheric model



- Primitive equations

- Ion

Density:
$$\frac{\partial \rho_i}{\partial t} + \frac{1}{A} \frac{\partial (A \rho_i v_{i,\parallel})}{\partial s} = S_i - L_i$$

Momentum:
$$\rho_i \frac{\partial v_{i,\parallel}}{\partial t} + \rho_i v_{i,\parallel} \frac{\partial v_{i,\parallel}}{\partial s} = n_i e E_{\parallel} - \frac{\partial p_i}{\partial s} - \rho_i g - \sum_k \rho_i v_{ik} (v_{i,\parallel} - v_{k,\parallel})$$

Temperature: $T_i = T_e$

V_{\parallel}	Field-aligned Velocity
E_{\parallel}	Electric field
A	Magnetic flux cross-section
g	Gravity and CF
T	Temperature
Q	Heating rate
κ	Diffusion coefficient

- Electron

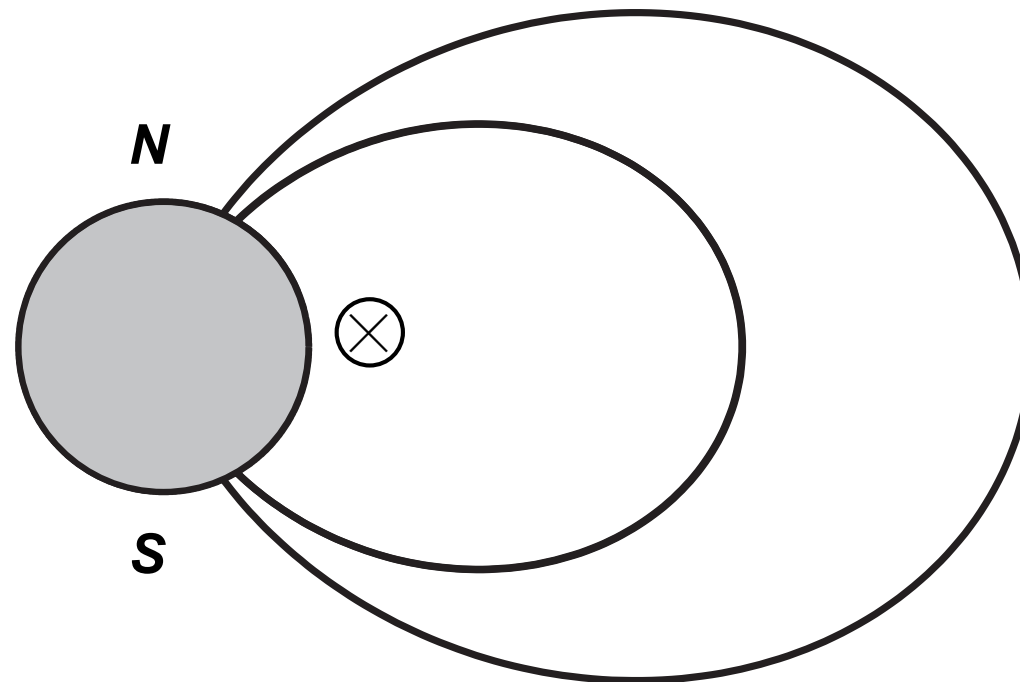
Density:
$$n_e = \sum_i n_i$$

Momentum:
$$E_{\parallel} = -\frac{1}{en_e} \frac{\partial p_e}{\partial s}$$

Temperature:
$$\frac{\partial T_e}{\partial t} - \frac{2}{3} \frac{1}{A} \frac{\partial}{\partial s} \left(A \kappa_e \frac{\partial T_e}{\partial s} \right) = Q_{EUV} + Q_{coll} + Q_{joule} + Q_{ph,ionos} + Q_{ph,mag}$$

N_i (H^+ , H_2^+ , H_3^+ , He^+ , H_2O^+ and H_3O^+),
 V_i (H^+ , H_2^+ , H_3^+ , He^+ , H_2O^+ and H_3O^+),
 T_e, T_i

- Dipole coordinate system
 - Along the magnetic field line \rightarrow 1 dimension
 - + Increasing the number of magnetic field line \rightarrow 2 dimensions
 - + Time evolution \rightarrow 3 dimensions



3 dimensional ionospheric model



• Primitive equations

• Ion

Density:
$$\frac{\partial \rho_i}{\partial t} + \frac{1}{A} \frac{\partial (A \rho_i v_{i,\parallel})}{\partial s} = \boxed{S_i - L_i}$$
 Source and Loss rate

Momentum:
$$\rho_i \frac{\partial v_{i,\parallel}}{\partial t} + \rho_i v_{i,\parallel} \frac{\partial v_{i,\parallel}}{\partial s} = n_i e E_{\parallel} - \frac{\partial p_i}{\partial s} - \rho_i g - \sum_k \rho_i v_{ik} (v_{i,\parallel} - v_{k,\parallel})$$

Temperature: $T_i = T_e$

v_{\parallel}	Field-aligned Velocity
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• Electron

Density:
$$n_e = \sum_i n_i$$

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Temperature:
$$\frac{\partial T_e}{\partial t} - \frac{2}{3} \frac{1}{A} \frac{\partial}{\partial s} \left(A \kappa_e \frac{\partial T_e}{\partial s} \right) = Q_{EUV} + Q_{coll} + Q_{joule} + Q_{ph,ionos} + Q_{ph,mag}$$

N_i (H^+ , H_2^+ , H_3^+ , He^+ , H_2O^+ and H_3O^+),
 V_i (H^+ , H_2^+ , H_3^+ , He^+ , H_2O^+ and H_3O^+),
 T_e, T_i

- Chemical reactions of 6 ion components

- H^+ , H_2^+ , H_3^+ , He^+ , H_2O^+ and H_3O^+

- 29 reactions

Chemical reaction	Rate coefficients	References
$H + h\nu \rightarrow H^+ + e^-$		<i>Moses and Bass</i> [2000]
$H_2 + h\nu \rightarrow H^+ + H + e^-$		<i>Moses and Bass</i> [2000]
$H_2 + h\nu \rightarrow H_2^+ + e^-$		<i>Moses and Bass</i> [2000]
$He + h\nu \rightarrow He^+ + e^-$		<i>Moses and Bass</i> [2000]
$H_2O + h\nu \rightarrow H^+ + OH + e^-$		<i>Moses and Bass</i> [2000]
$H_2O + h\nu \rightarrow H_2O^+ + e^-$		<i>Moses and Bass</i> [2000]
$H^+ + e^- \rightarrow H$	$1.9 \times 10^{-16} T_e^{-0.7}$	<i>Moses and Bass</i> [2000]; <i>Kim and Fox</i> [1994]
$H_2^+ + e^- \rightarrow H + H$	$2.3 \times 10^{-12} T_e^{-0.4}$	<i>Moses and Bass</i> [2000]; <i>Kim and Fox</i> [1994]
$H_3^+ + e^- \rightarrow H_2 + H$	$7.6 \times 10^{-13} T_e^{-0.5}$	<i>Moses and Bass</i> [2000]; <i>Kim and Fox</i> [1994]
$H_3^+ + e^- \rightarrow 3H$	$9.7 \times 10^{-13} T_e^{-0.5}$	<i>Moses and Bass</i> [2000]; <i>Kim and Fox</i> [1994]
$He^+ + e^- \rightarrow He$	$1.9 \times 10^{-16} T_e^{-0.7}$	<i>Moses and Bass</i> [2000]; <i>Kim and Fox</i> [1994]
$H_2O^+ + e^- \rightarrow O + H_2$	$3.5 \times 10^{-12} T_e^{-0.5}$	<i>Moses and Bass</i> [2000]; <i>Miller et al.</i> [1997]
$H_2O^+ + e^- \rightarrow OH + H$	$2.8 \times 10^{-12} T_e^{-0.5}$	<i>Moses and Bass</i> [2000]; <i>Miller et al.</i> [1997]
$H_3O^+ + e^- \rightarrow H_2O + H$	$6.1 \times 10^{-12} T_e^{-0.5}$	<i>Moses and Bass</i> [2000]; <i>Miller et al.</i> [1997]
$H_3O^+ + e^- \rightarrow OH + 2H$	$1.1 \times 10^{-11} T_e^{-0.5}$	<i>Moses and Bass</i> [2000]; <i>Miller et al.</i> [1997]
$H^+ + H_2 \rightarrow H_2^+ + H$	see text	<i>Moses and Bass</i> [2000]
$H^+ + H_2 + M \rightarrow H_3^+ + M$	3.2×10^{-41}	<i>Moses and Bass</i> [2000]; <i>Kim and Fox</i> [1994]
$H^+ + H_2O \rightarrow H_2O^+ + H$	8.2×10^{-15}	<i>Moses and Bass</i> [2000]; <i>Anicich</i> [1993]
$H_2^+ + H \rightarrow H^+ + H_2$	6.4×10^{-16}	<i>Moses and Bass</i> [2000]; <i>Anicich</i> [1993]
$H_2^+ + H_2 \rightarrow H_3^+ + H$	2.0×10^{-15}	<i>Moses and Bass</i> [2000]; <i>Kim and Fox</i> [1994]
$H_2^+ + H_2O \rightarrow H_2O^+ + H_2$	3.9×10^{-15}	<i>Moses and Bass</i> [2000]; <i>Anicich</i> [1993]
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$H_3^+ + H_2O \rightarrow H_3O^+ + H_2$	5.3×10^{-15}	<i>Moses and Bass</i> [2000]; <i>Anicich</i> [1993]
$He^+ + H_2 \rightarrow H^+ + H + He$	8.8×10^{-20}	<i>Matcheva et al.</i> [2001]; <i>Perry</i> [1999]
$He^+ + H_2 \rightarrow H_2^+ + He$	9.4×10^{-21}	<i>Moses and Bass</i> [2000]; <i>Kim and Fox</i> [1994]
$He^+ + H_2O \rightarrow H^+ + OH + He$	1.9×10^{-16}	<i>Moses and Bass</i> [2000]; <i>Anicich</i> [1993]
$He^+ + H_2O \rightarrow H_2O^+ + He$	5.5×10^{-17}	<i>Moses and Bass</i> [2000]; <i>Anicich</i> [1993]
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3 dimensional ionospheric model



• Primitive equations

• Ion

Density:
$$\frac{\partial \rho_i}{\partial t} + \frac{1}{A} \frac{\partial (A \rho_i v_{i,\parallel})}{\partial s} = \boxed{S_i - L_i}$$
 Source and Loss rate

Momentum:
$$\rho_i \frac{\partial v_{i,\parallel}}{\partial t} + \rho_i v_{i,\parallel} \frac{\partial v_{i,\parallel}}{\partial s} = n_i e E_{\parallel} - \frac{\partial p_i}{\partial s} - \rho_i g - \sum_k \rho_i v_{ik} (v_{i,\parallel} - v_{k,\parallel})$$

Temperature: $T_i = T_e$

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Density:
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Momentum:
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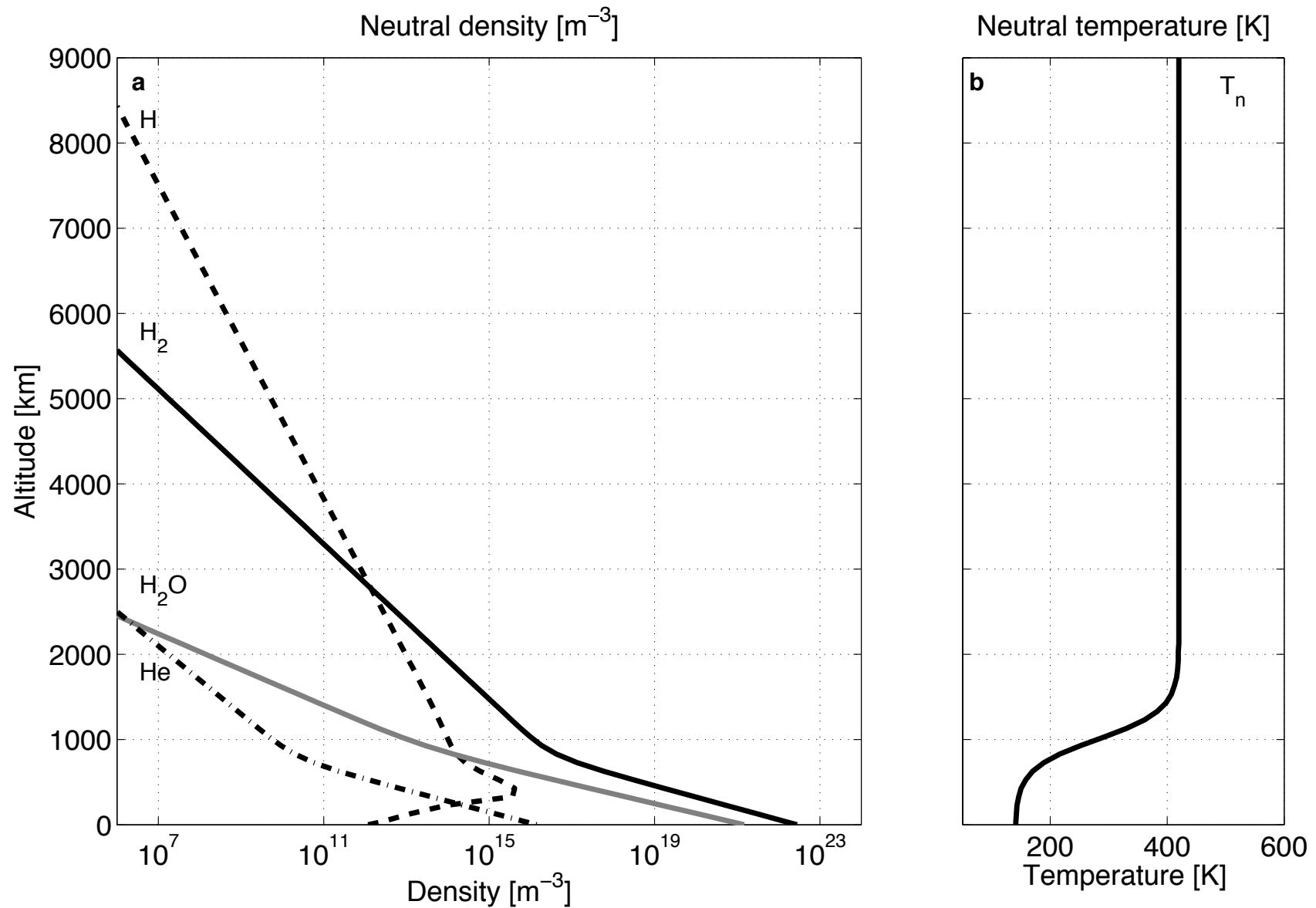
Temperature:
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Heat flow, Q_{HF}

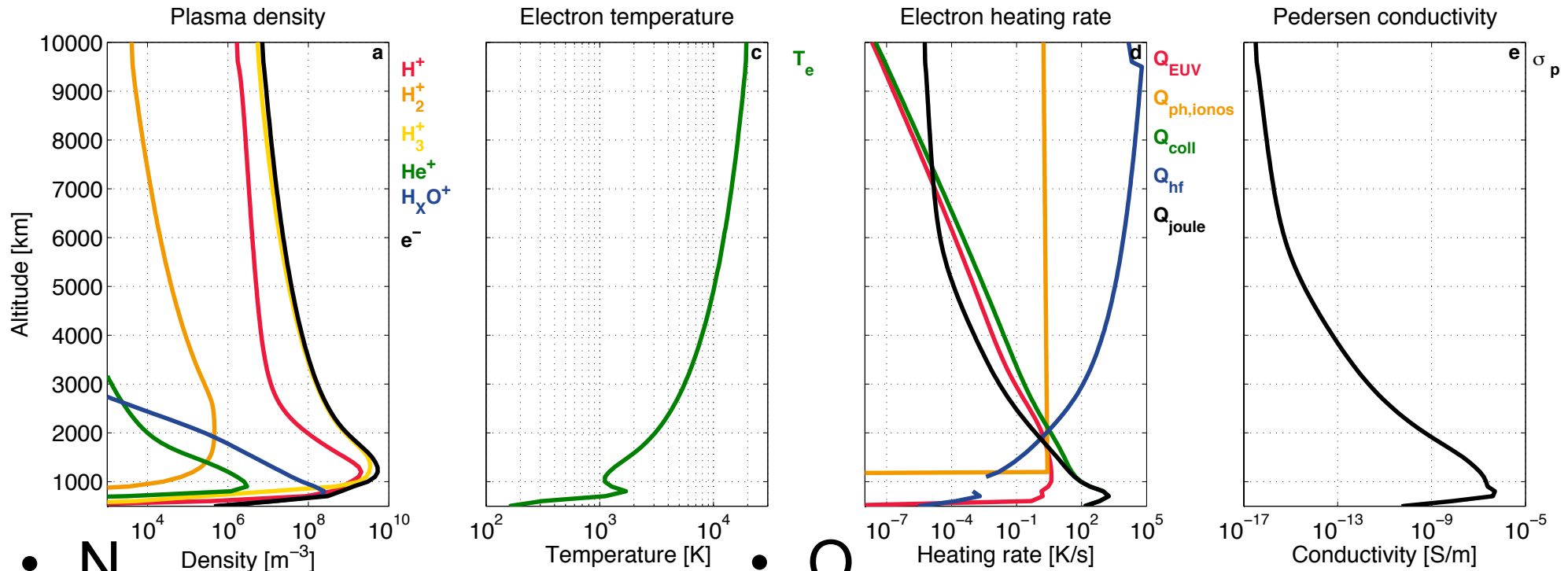
Heating rate

N_i (H^+ , H_2^+ , H_3^+ , He^+ , H_2O^+ and H_3O^+),
 V_i (H^+ , H_2^+ , H_3^+ , He^+ , H_2O^+ and H_3O^+),
 T_e, T_i

Background neutral atmosphere



N_i, σ_p, T_e, Q_e ($L=5, LT=12$)

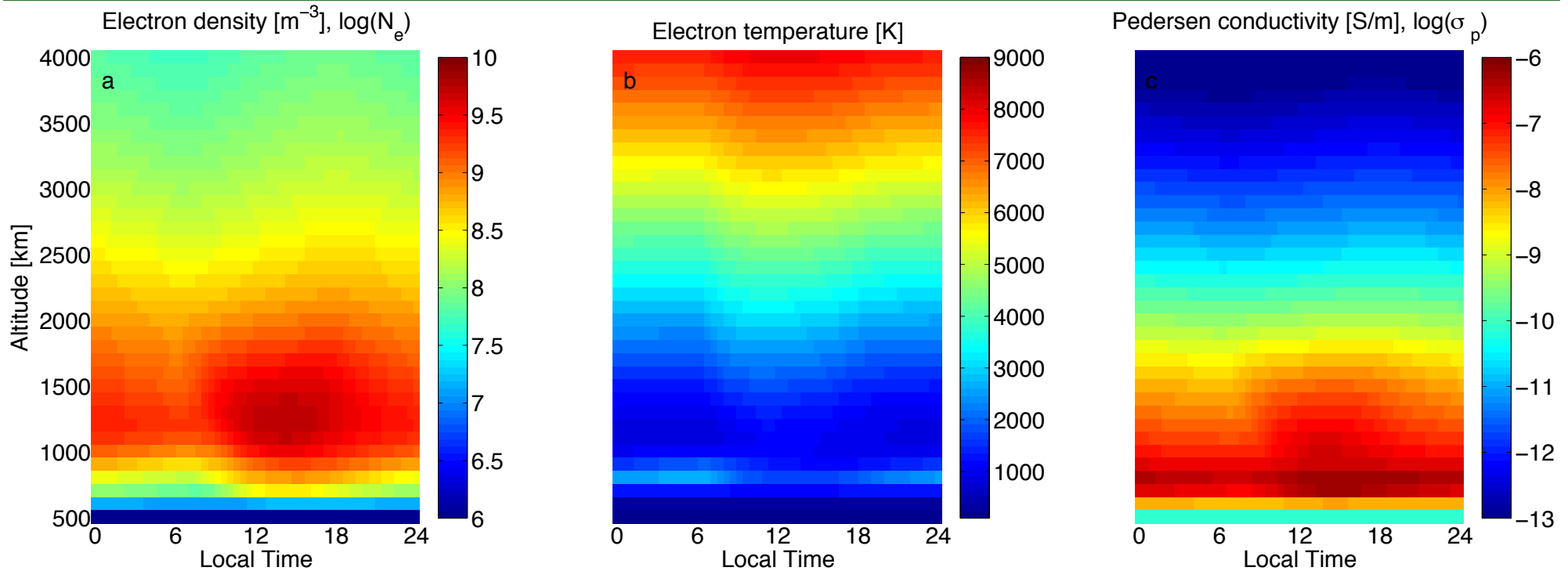


- N_i
 - H_3^+ is dominant.
 - Max: $\sim 10^{10} m^{-3}$
- T_e
 - 2000 K at ~ 1200 km
 - T_e drastically increases.
- Q_e
 - Q_{Joule} and Q_{coll} are important at low altitude.
 - Q_{HF} is contributing to heat process above topside.
- σ_i
 - Maximum around 1000 km

Diurnal variations of N_e , T_e and σ_p (L=5)



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- N_e , σ_p
 - Start to increase after 6 LT
 - Max: ~14 LT
 - N_e and σ_p decreases at high altitudes.

- T_e
 - Max: ~12 LT
 - T_e is kept to high temperature in all LT by Q_{HF} .



M-I coupling

Pedersen conductivity

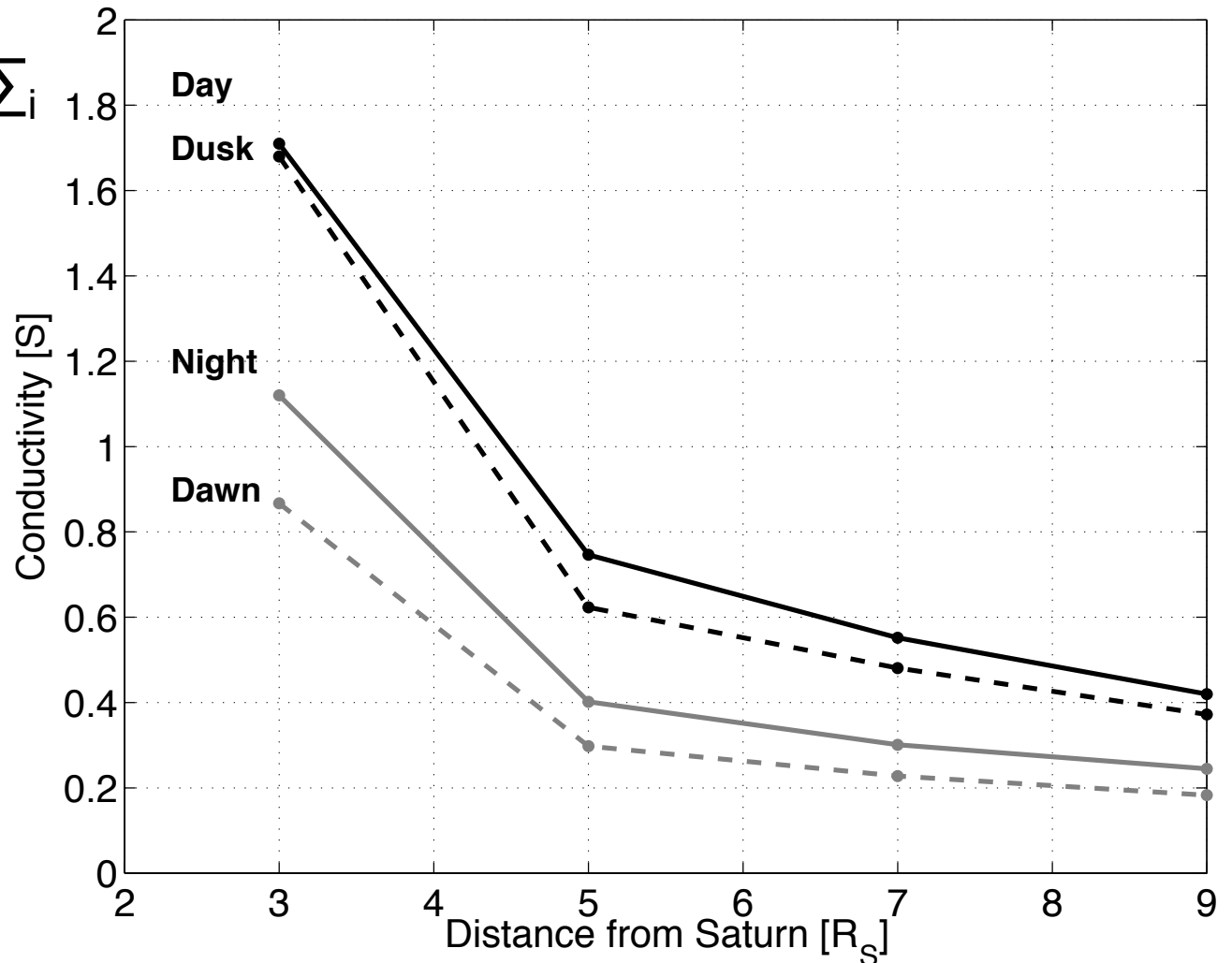


$$\sigma_p = \sum_i \frac{\nu_i}{\nu_{in}^2 + \omega_{ci}^2} \frac{n_i e^2}{m_i} + \frac{\nu_e}{\nu_{en}^2 + \omega_{ce}^2} \frac{n_e e^2}{m_e}$$

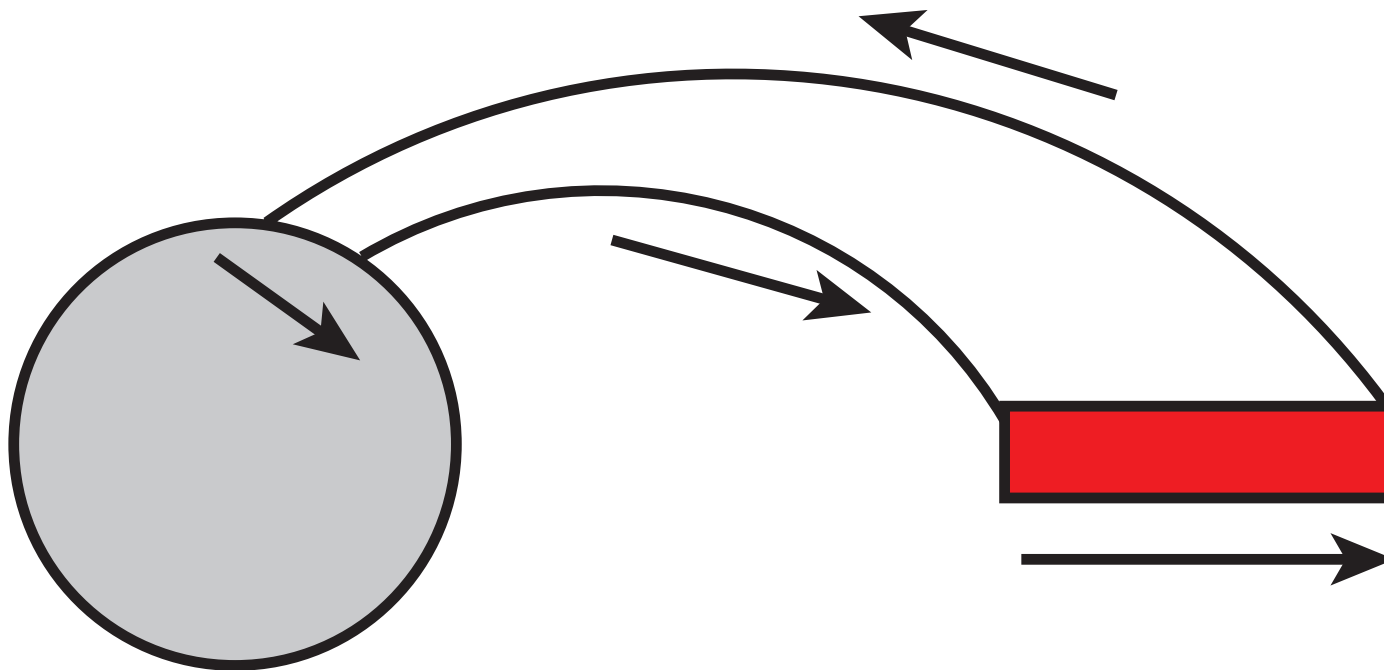
$$\Sigma_i = \int_{z_1}^{z_2} \sigma_p ds$$

Pedersen Conductivity

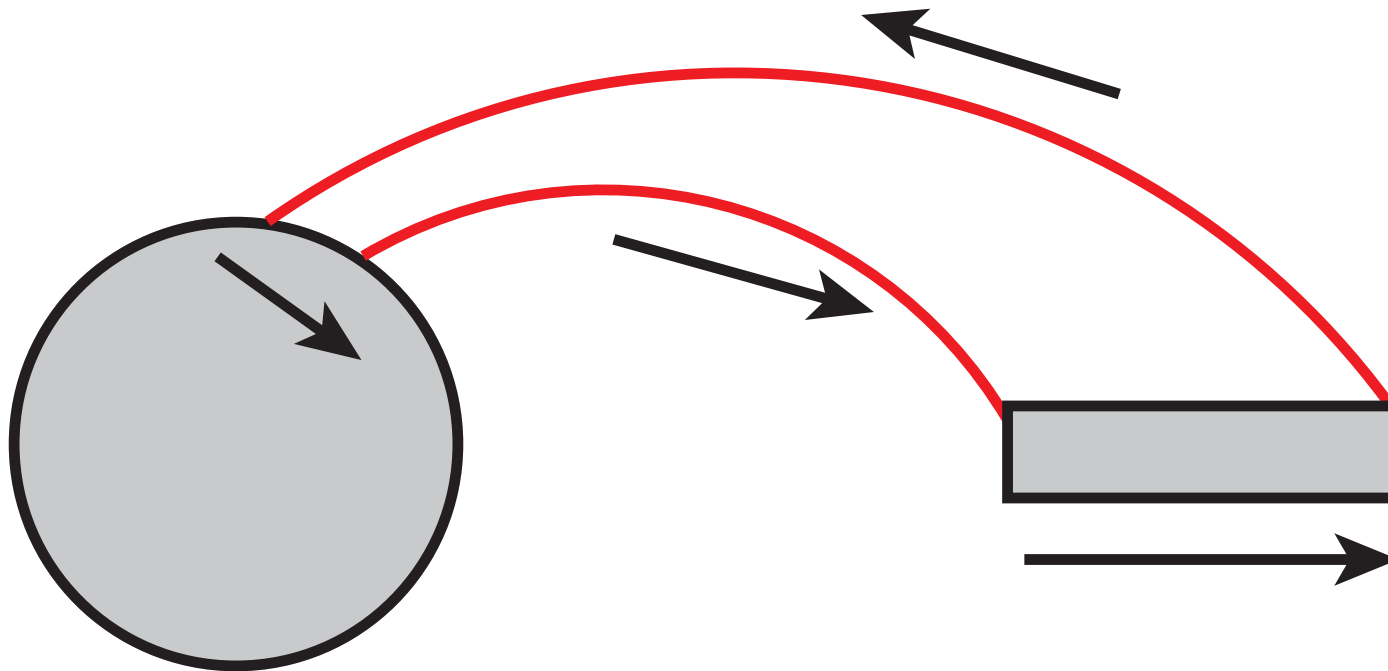
- LT dependence of Σ_i
- Σ_i decreases with increase of R_s



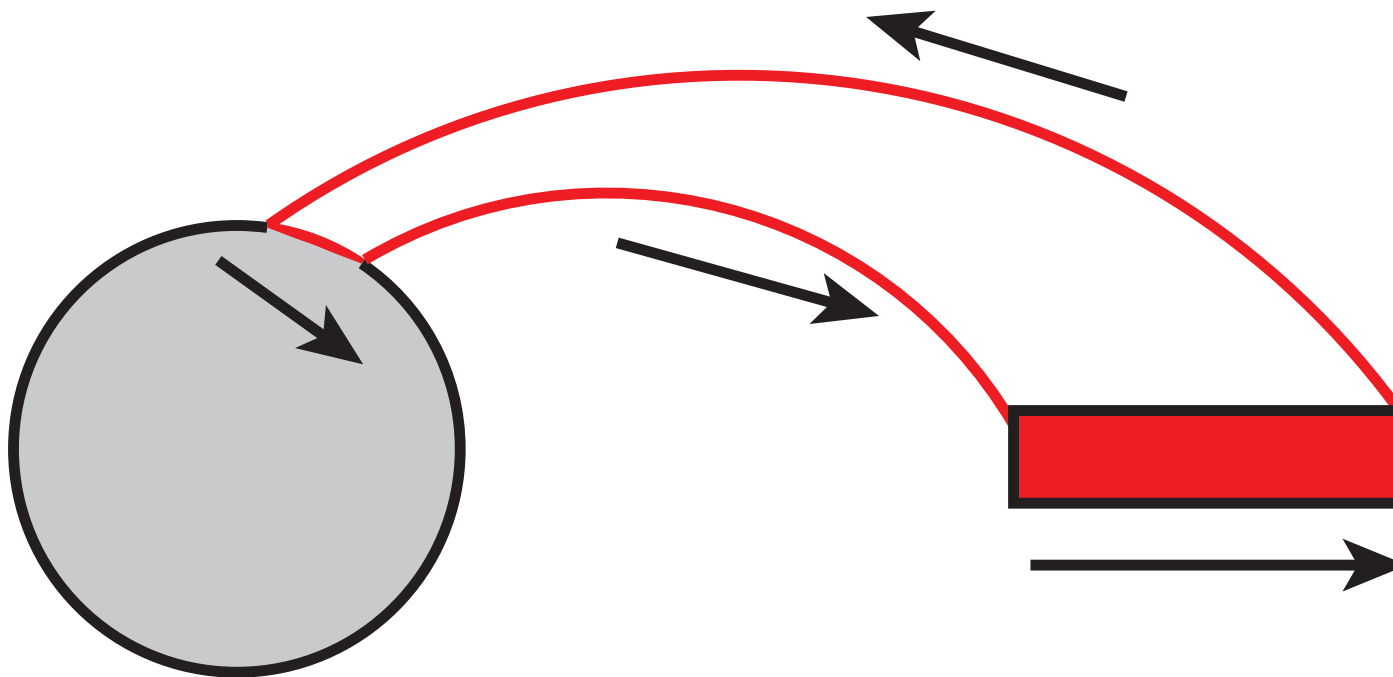
1. Modeling of inner magnetosphere with dust-plasma interaction
2. Modeling of ionosphere
3. Magnetosphere-ionosphere coupling



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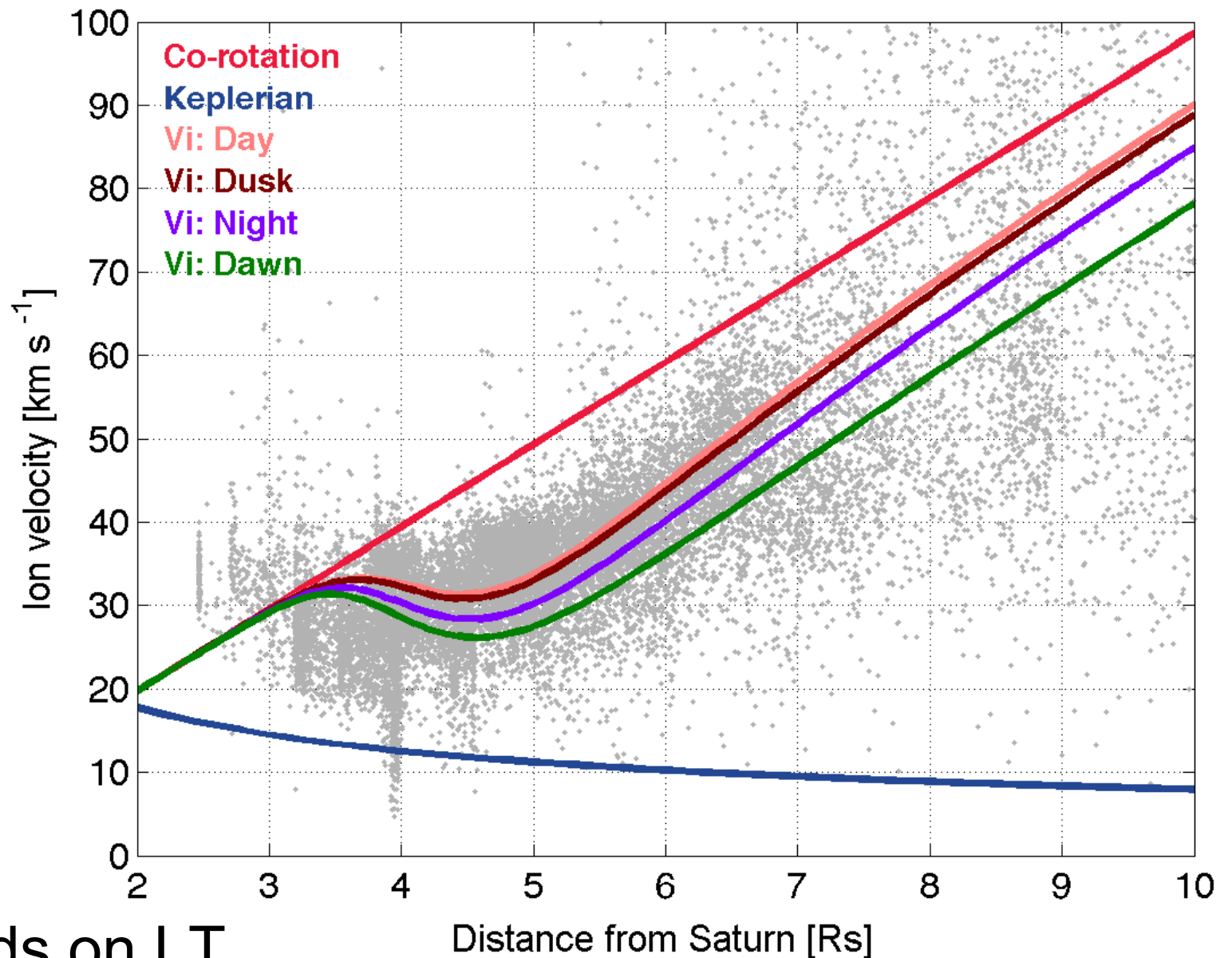
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Magnetospheric ion velocity



$$\sum_i (\mathbf{E}_{cor} - \mathbf{E}) = \mathbf{j}D$$



- V_i depends on LT.

- Ionospheric plasma distribution
 - H_3^+ is dominant at $L=5$.
 - Peak: 10^9 - 10^{10} m^{-3}
 - T_e is much higher than that of previous studies at high altitude.
 - 2000 K at $\sim 1200 \text{ km}$; 10000 K at $\sim 5000 \text{ km}$
 - **Joule heating** and **collision heating** are important at low altitude, and **heat flow** at high altitude.
- Ionospheric conductivity
 - Pedersen conductivity depends on LT.
 - Day > Dusk > Night > Dawn
 - The magnetospheric ion speed shows the same tendency as the diurnal variation of conductivity.

- Ion speed is slow down from the co-rotation speed due to **dust-plasma interaction** and **magnetosphere-ionosphere coupling**.
- The inner magnetosphere and ionosphere are **strongly coupled**.