Plasma Instabilities in the Earth's Ionosphere

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http:www.ep.sci.hokudai.ac.jp/~shw/Plasma.pdf

In December 12, 1901, Marconi demonstrated transatlantic communication by receiving a signal in St. John's Newfoundland that had been sent from Cornwall, England. Because of his pioneering work in the use of electromagnetic radiation for radio communications, Marconi was awarded the Nobel Prize in physics in 1909.







On the 12th of December 1924, Edward Appleton and his student Miles Barnett, started a series of pioneering experiments which proved the existence of an electrically charged layer in our atmosphere which is now known as the ionosphere.



Discovery of the lonosphere

- 1819 Hans Christian Oersted discovers that electricity and magnetism are related
- 1864–73 James Clerk Maxwell describes theory of eletromagnetic radiation and predicts existence of radiowaves
- 1882 Balfour Stewart suggests winds drive electric currents in the upper atmosphere
- 1887 Heinrich Hertz proves existence of radiowaves
- 1901 Marconi transmits radio signal across Atlantic Ocean from Cornwall, England to St. John's, Newfoundland
- 1902 Oliver Heaviside; Arthur Kennelly propose existence of conducting layer in upper atmosphere
- 1909 Marconi awarded Nobel Prize
- 1924 Edward Appleton and others develop the ionosonde and begin www. ground-based soundings; prove existence of ionosphere
- 1925 Appleton discovers second layer (the F region)
- 1926 Robert Watson-Watt (later developer of radar) coins word "ionosphere"
- 1927 Sydney Chapman describes theory for formation of ionosphere
- 1947 Appleton awarded Nobel Prize
- 1948 Rocket probes begin
- 1950's Riometer (Relative Ionospheric Opacity Meter using Extra Terrestrial Electromagnetic Radiation) developed
- 1958 Incoherent Scatter Radar developed
- 1962 Alouette 1 satellite makes first topside soundings





Atmospheric atom and molecule are ionized by Extreme UltraViolet lights from the Sun.



Fig. 5.18. Calculated ionization rates in the E- and F-regions. (From Hinteregger et al., 1965.)

Earth's Ionosphere/Thermosphere



Fig. 1.2. International Quiet Solar Year (IQSY) daytime atmospheric composition, based on mass spectrometer measurements above White Sands, New Mexico (32°N, 106°W). The helium distribution is from a nighttime measurement. Distributions above 250 km are from the Elektron II satellite results of Istomin (1966) and Explorer XVII results of Reber and Nicolet (1965). [C. Y. Johnson, U.S. Naval Research Laboratory, Washington, D.C. Reprinted from Johnson (1969) by permission of the MIT Press, Cambridge, Massachusetts. Copyright 1969 by MIT.]

Plasma

Langmuir (1928)

'We shall use the name plasma to describe this region containing balanced charges of ions and electrons'.

>99.9% of material in space are Plasma.





O+ (B=10^-5T, E=10^-3V/m)



$$v = r_L \omega_C$$

 r_L Larmor radius
 ω_C cyclotron frequency



e 1.7×10^{5} m/s 0.1 m 1.7×10^{6} r ad/s T = 1000K Magnetohydrodynamic Equations: MHD Equations

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{V}) = 0$$

$$\rho \frac{\partial \mathbf{V}}{\partial t} + \rho (\mathbf{V} \cdot \nabla) \mathbf{V} = -\nabla \mathbf{p} + (\mathbf{J} \times \mathbf{B})$$

$$\frac{\partial \mathbf{B}}{\partial t} = \nabla \times (\mathbf{V} \times \mathbf{B}) + \frac{1}{\mu \sigma} \Delta \mathbf{B}$$

$$\nabla \times \mathbf{B} = \mu \mathbf{J}$$

Alfven: The Nobel Prize in Physics 1970 for fundamental work and discoveries in magnetohydrodynamics with fruitful applications in different parts of plasma physics.





Ohm's law
$$J = \sigma (E + V \times B)$$

Induction equation $\frac{\partial \mathbf{B}}{\partial t} = \nabla \times (\mathbf{V} \times \mathbf{B}) + \frac{1}{\mu \sigma} \Delta \mathbf{B}$ Basic equations of plasma atmosphere

Equation of continuity $\frac{\partial \rho_{i}}{\partial t} + \nabla \cdot (\rho_{i} \mathbf{v}_{i}) = P_{i} - L_{i}$

Equation of motion

$$\frac{\partial \mathbf{v}_{i}}{\partial t} + (\mathbf{v}_{i} \cdot \nabla)\mathbf{v}_{i} = -\frac{1}{\rho_{i}}\nabla p_{i} + \mathbf{g} + \frac{q}{m_{i}}(\mathbf{E} + \mathbf{v}_{i} \times \mathbf{B}) - \sum_{k} v_{ik}(\mathbf{v}_{i} - \mathbf{u}_{k})$$

State equation (perfect gas) $p_i = n_i kT_i$ Equation of motion

$$\begin{split} & \overbrace{\partial \mathbf{v}_{i}}^{i} + \left(\mathbf{v}_{i} \cdot \nabla\right) \mathbf{v}_{i}^{i} = -\frac{1}{\rho_{i}} \nabla p_{i}^{i} + \mathbf{g} + \frac{q}{m_{i}} \left(\mathbf{E} + \mathbf{v}_{i} \times \mathbf{B}\right) - \sum_{k} v_{ik} \left(\mathbf{v}_{i}^{i} - \mathbf{u}_{k}^{i}\right) \\ & \mathbf{v}_{i}^{i} = \frac{v_{in} \Omega_{i}}{v_{in}^{2} + \Omega_{i}^{2}} \left(\frac{\mathbf{E}}{\mathbf{B}} - \frac{\nabla p_{i}}{nm_{i} \Omega_{i}} + \frac{\mathbf{g}}{\Omega_{i}} + \frac{v_{in} \mathbf{u}_{n}}{\Omega_{i}}\right) + \frac{\Omega_{i}^{2}}{v_{in}^{2} + \Omega_{i}^{2}} \left(\frac{\mathbf{E}}{\mathbf{B}} - \frac{\nabla p_{i}}{nm_{i} \Omega_{i}} + \frac{\mathbf{g}}{\Omega_{i}} + \frac{v_{in} \mathbf{u}_{n}}{\Omega_{i}}\right) \times \frac{\mathbf{B}}{\mathbf{B}} \\ & \mathbf{v}_{e}^{i} = -\frac{v_{en} \Omega_{e}}{v_{en}^{2} + \Omega_{e}^{2}} \left(\frac{\mathbf{E}}{\mathbf{B}} + \frac{\nabla p_{e}}{nm_{e} \Omega_{e}} - \frac{\mathbf{g}}{\Omega_{e}} - \frac{v_{en} \mathbf{u}_{n}}{\Omega_{e}}\right) + \frac{\Omega_{e}^{2}}{v_{en}^{2} + \Omega_{e}^{2}} \left(\frac{\mathbf{E}}{\mathbf{B}} + \frac{\nabla p_{e}}{nm_{e} \Omega_{e}} - \frac{\mathbf{g}}{\Omega_{e}} - \frac{v_{en} \mathbf{u}_{n}}{\Omega_{e}}\right) \times \frac{\mathbf{B}}{\mathbf{B}} \end{split}$$

In the ionospheric F region,

$$\Omega_{i} \gg v_{in}, \qquad \Omega_{e} \gg v_{en} \qquad \qquad v_{i} = \left(\frac{E}{B} - \frac{\nabla p_{i}}{nm_{i}\Omega_{i}} + \frac{g}{\Omega_{i}} + \frac{v_{in}u_{n}}{\Omega_{i}}\right) \times \frac{B}{B}$$
$$v_{e} = \left(\frac{E}{B} + \frac{\nabla p_{e}}{nm_{e}\Omega_{e}} - \frac{g}{\Omega_{e}} - \frac{v_{en}u_{n}}{\Omega_{e}}\right) \times \frac{B}{B}$$
$$\approx \frac{V_{th}^{2}}{\Omega L} = \frac{V_{th}r_{L}}{L}$$



Fig. 4. Sequence of airglow images taken on the night of 21 February, 1993 over SHAR (a) 630 nm images at 2256, 2316, 2326, 0006, 0016 and 0021 LT and (b) 777.4 nm images at 23:13:45, 23:18:45, 23:23:45, 23:43:45, 00:08:45 and 00:13:45 LT. The arrow points towards geomagnetic north.

Plasma Bubbles at Magnetic Equator

630nm

777.4nm

 $O^+ + e \rightarrow O + h v$ $O_2^+ + e \rightarrow O + O + h v$

Plasma Bubbles observed by ROCSAT Satellite



Jicamarca Radar Observation of Plasma Density Irregularities associated with Plasma Bubbles



Fig. 4.1. Range-time-intensity map displaying the backscatter power at 3-m wavelengths measured at Jicamarca, Peru. The gray scale is decibels above the thermal noise level. [After Kelley *et al.* (1981). Reproduced with permission of the American Geophysical Union.]

Signals from Geosynchronous Satellite



Nov. 30 - Dec.1, 1988

Stability of Equatorial Ionosphere
Continuity equation, Current conservation

$$\frac{\partial n}{\partial t} + \nabla (nv) = 0, \quad \nabla \cdot J = 0$$

$$= equilibrium state + perturbed state$$

$$n = n_0 + n', \quad v = v_0 + v', \quad J = J_0 + J'$$

$$v_0 = \frac{g}{\Omega_i} \times \frac{B}{B}, \quad v' = \frac{E' \times B}{B^2}, \quad J_0 = 0, \quad J' = en' \frac{g}{\Omega_i} \times \frac{B}{B}$$

Equations are linearized with respect to the perturbed quantities. $\partial n'$

$$\frac{\partial \mathbf{n}}{\partial t} + \mathbf{n}_0 \nabla (\mathbf{v}') + \mathbf{v}' \nabla (\mathbf{n}_0) + \mathbf{v}_0 \nabla (\mathbf{n}') = 0$$
$$\nabla \cdot \mathbf{J}' = 0$$

n', v' $\propto e^{-i(\omega t - kx)}$ Plane wave solutions are assumed. Continuity equation $-i\omega n' + ikn_0 \frac{E'}{B} + \frac{E'}{B} \frac{\partial n_0}{\partial z} + ik \frac{g}{\Omega_i} n' = 0$ Current conservation

$$ik \frac{en_0}{B} \frac{v_{in}}{\Omega_i} E' + ike \frac{g}{\Omega_i} n' = 0 \quad \rightarrow \quad \frac{E}{B} = -\frac{g}{v_{in}} \frac{n}{n_0}$$

$$\omega = \omega_{\rm r} + i\gamma$$

Growth rate Rayleigh-Tayler Instability

$$\gamma = \frac{g}{v_{in}} \frac{1}{n_0} \frac{\partial n_0}{\partial z}$$

Generalized Rayleigh-Tayler Instability $\gamma = \left(\frac{g}{v_{in}} + \frac{E_x}{B} + \frac{v_{in}u_{nx}}{\Omega_i}\right) \frac{1}{n_0} \frac{\partial n_0}{\partial z}$

Generation Process of Plasma Bubble in the Bottomside of equatorial F region



Evolution of Plasma Bubbles Continuity equation, Current conservation $\frac{\partial n}{\partial t} + \nabla (nv) = 0, \quad \nabla \cdot J = 0$





Space Weather



Plasma Bubble is One of the Important Research Themes for Space Weather Program.

> However, We don't understand * 3D structure and dynamics of plasma bubble, * Generation mechanism of small scale irregularity, * Seed mechanism. * Effect of penetrating electric field from polar ionosphere.