



HOKKAIDO
UNIVERSITY

Studies on dust-plasma interaction in Saturn's inner magnetosphere and its magnetosphere-ionosphere coupling

Shotaro Sakai

Planetary and Space Group



Outline of my thesis



HOKKAIDO UNIVERSITY

Structure of my doctoral thesis

1. General Introduction
2. Enceladus plume observed by Cassini RPWS/LP
3. Modeling of the inner magnetosphere
4. Modeling of the ionosphere
5. Magnetosphere-ionosphere coupling
6. Summary

Outline of my thesis



HOKKAIDO UNIVERSITY

Structure of my doctoral thesis

1. General Introduction
2. Enceladus plume observed by Cassini RPWS/LP
3. Modeling of the inner magnetosphere
4. Modeling of the ionosphere
5. Magnetosphere-ionosphere coupling
6. Summary



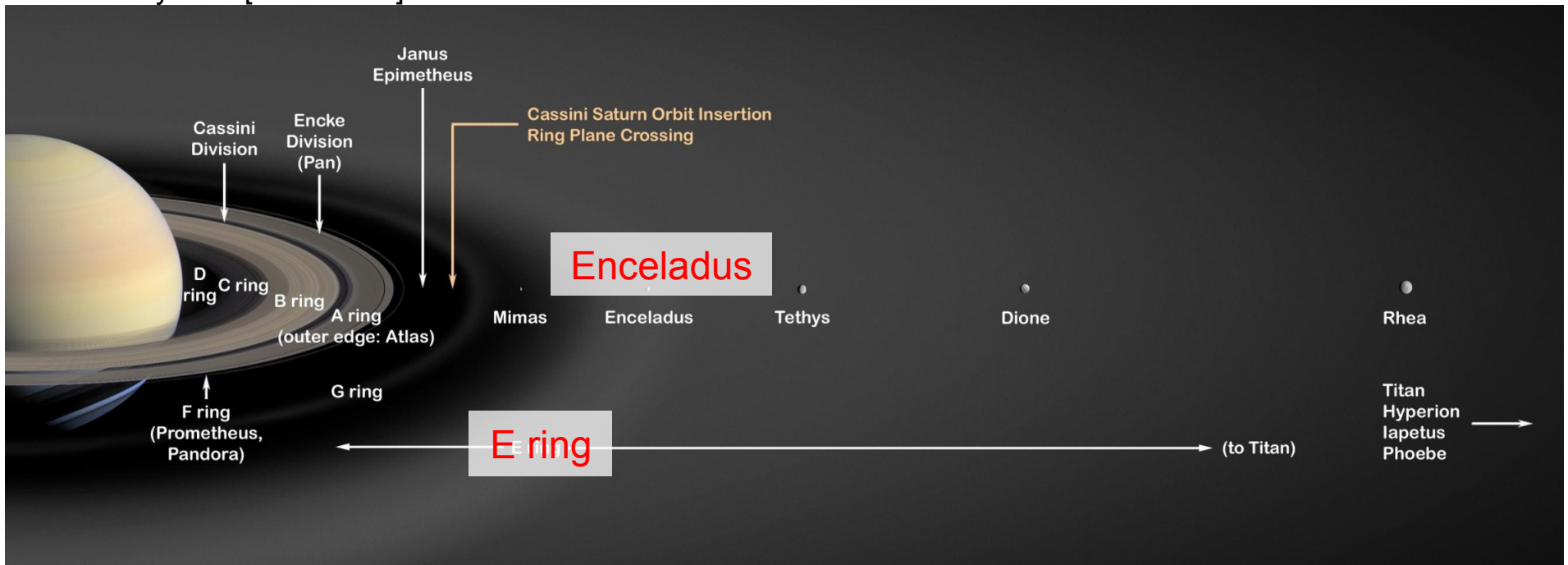
Introduction

Saturn's system



- Equatorial radius: 60,268 km (1 R_s)
- Mass: 5.68×10^{26} kg
- Equatorial gravity: 10.44 m/s^2
- Rotation period: 0.436 day
- Revolution period: 29.46 year
- Magnetic moment: $4.6 \times 10^{18} \text{ T/m}^3$
- Tilt of magnetic axis respect to rotational axis: $< 1^\circ$
- Satellites#: 64
- Rings: D, C, B, A, F, G and E
- Exploration of Saturn: Pioneer 11, Voyager 1 and 2, Cassini

Saturn's system [NASA/JPL]

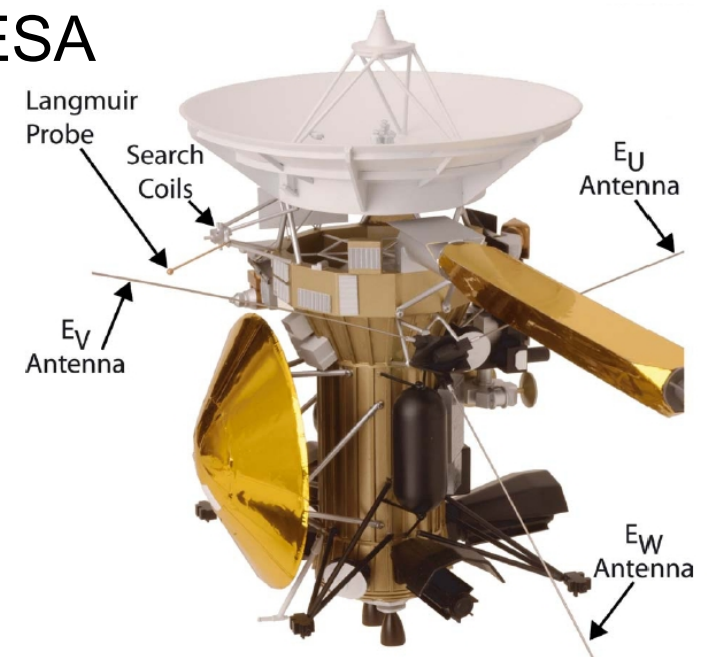


Cassini



HOKKAIDO UNIVERSITY

- Outline
 - Launch date: 15 Oct. 1997
 - Development & Operation: NASA, ESA
 - Orbit Insertion: Dec. 2004
 - Now Operating!
 - Until Sep. 2017
- Instruments (3 major)
 - Optical remote sensing
 - Electric-magnetic field, particles and wave observation
 - Microwave remote sensing

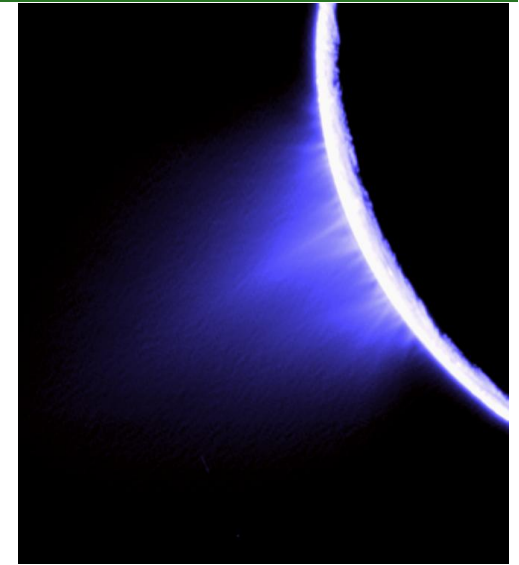


Cassini [Gurnett et al., 2004]

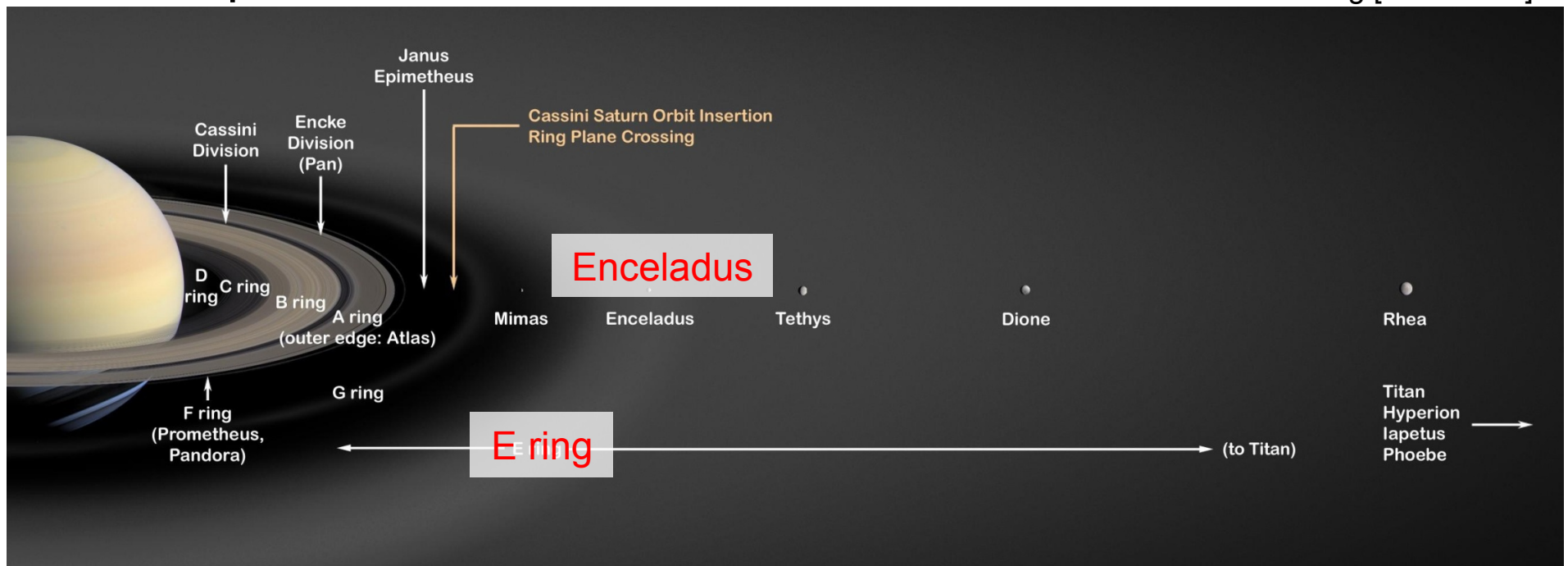
Enceladus plume & E ring



- Enceladus plume (~3.95 Rs)
 - Water gas
- E ring
 - 3 – 8 Rs
 - Water group ion
 - Dust
 - Source: **Mainly Enceladus plume**
 - Kepler motion



Enceladus & E ring [NASA/JPL]

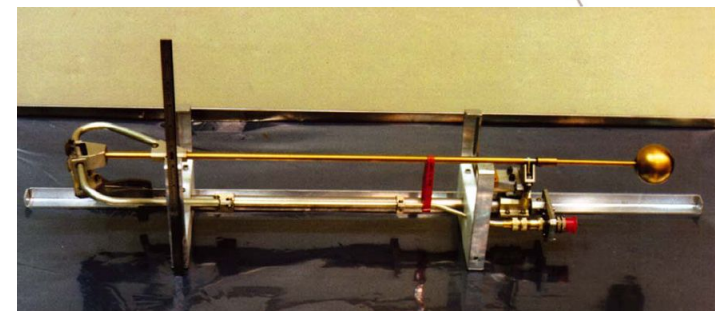
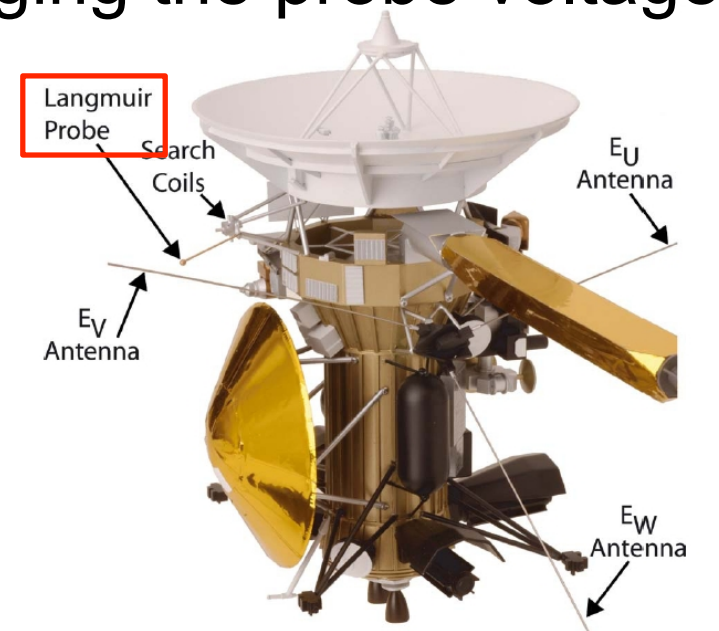
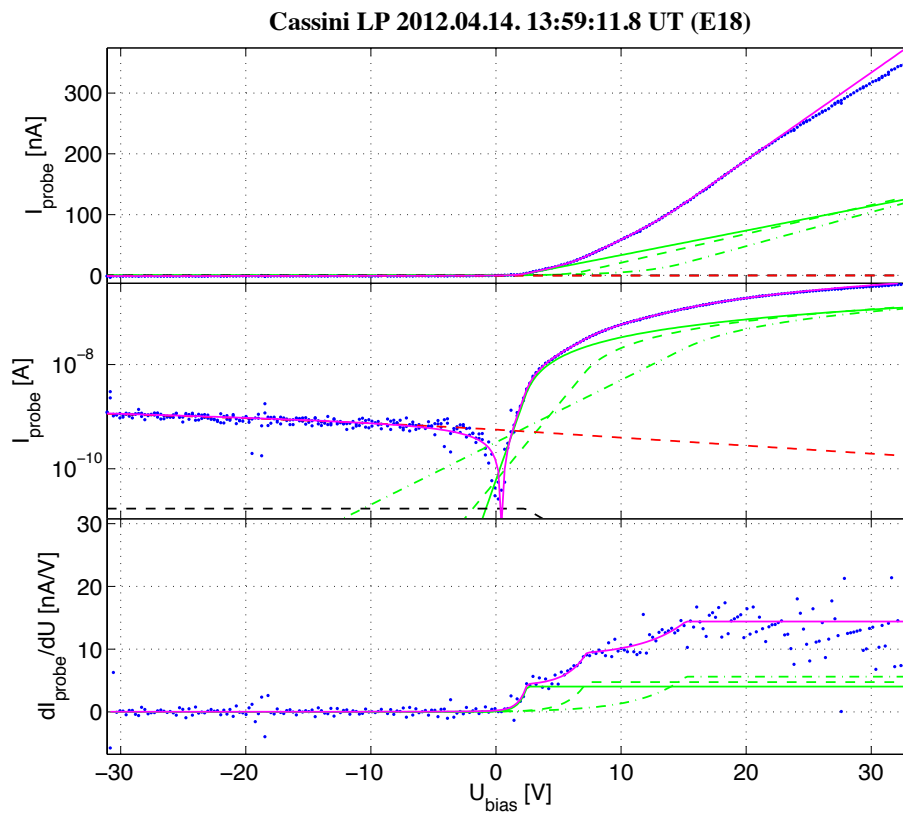


Cassini Langmuir Probe (LP)



HOKKAIDO UNIVERSITY

- Length: 1.5 m, Diameter: 50 mm
- Titanium
- LP measures currents by changing the probe voltage from -32 to 32 V.

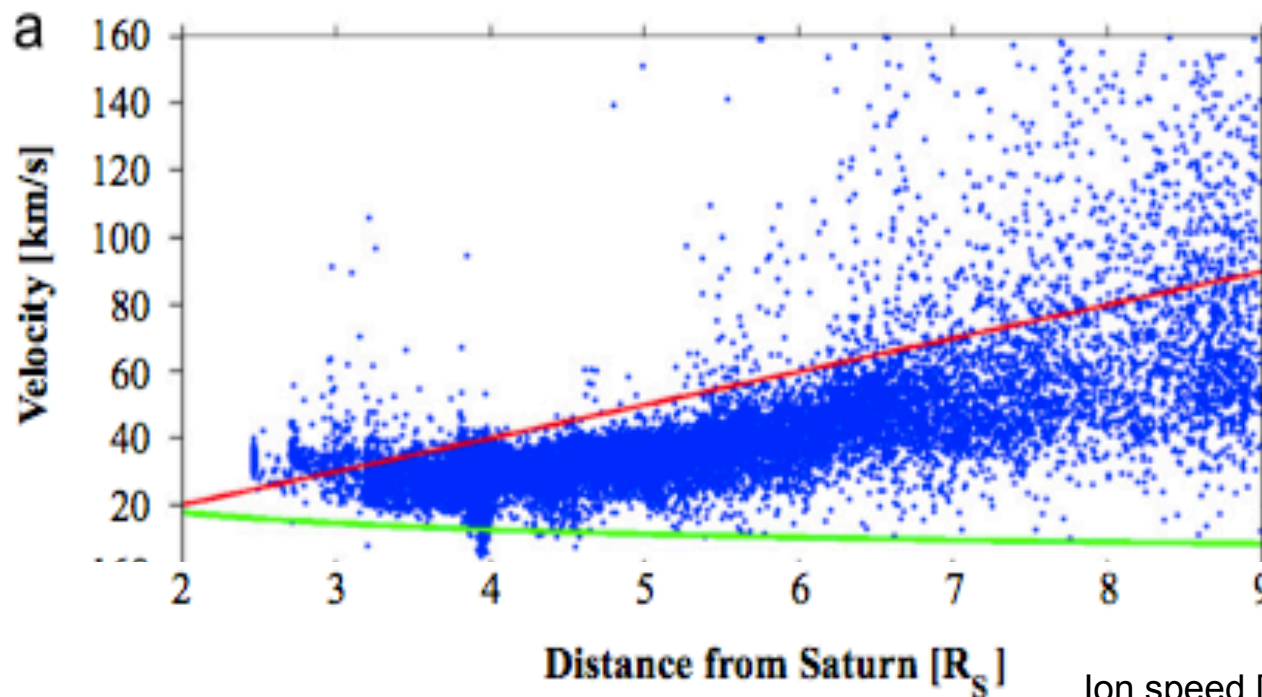


Cassini & Cassini LP [Gurnett et al., 2004]

Co-rotation deviation by dusts?



- Ion observations from the Cassini RPWS/LP in Saturn's magnetosphere
 - Ion has slower speed than the co-rotation [*Wahlund et al.*, 2009; *Morooka et al.*, 2011; *Holmberg et al.*, 2012].



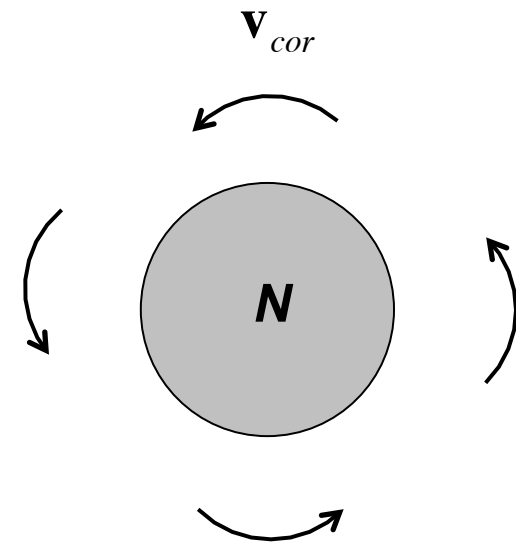
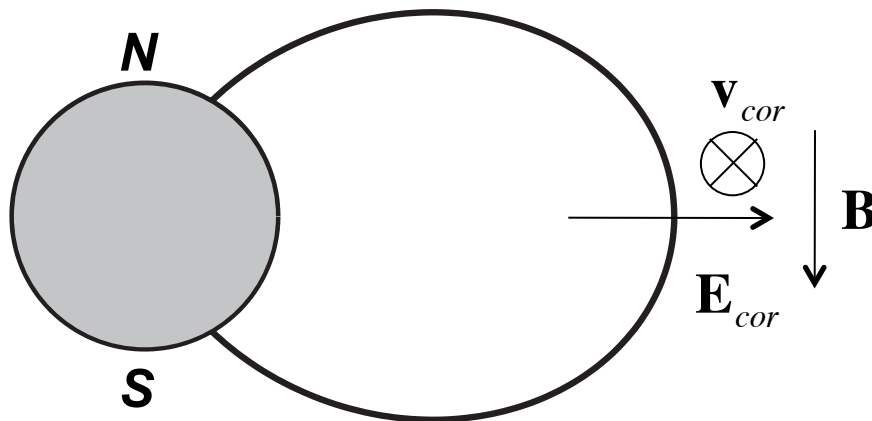
Co-rotation



- Magnetospheric plasma should be **co-rotating**.

Co-rotation velocity:
$$\mathbf{v}_{cor} = \frac{\mathbf{E}_{cor} \times \mathbf{B}}{B^2}$$

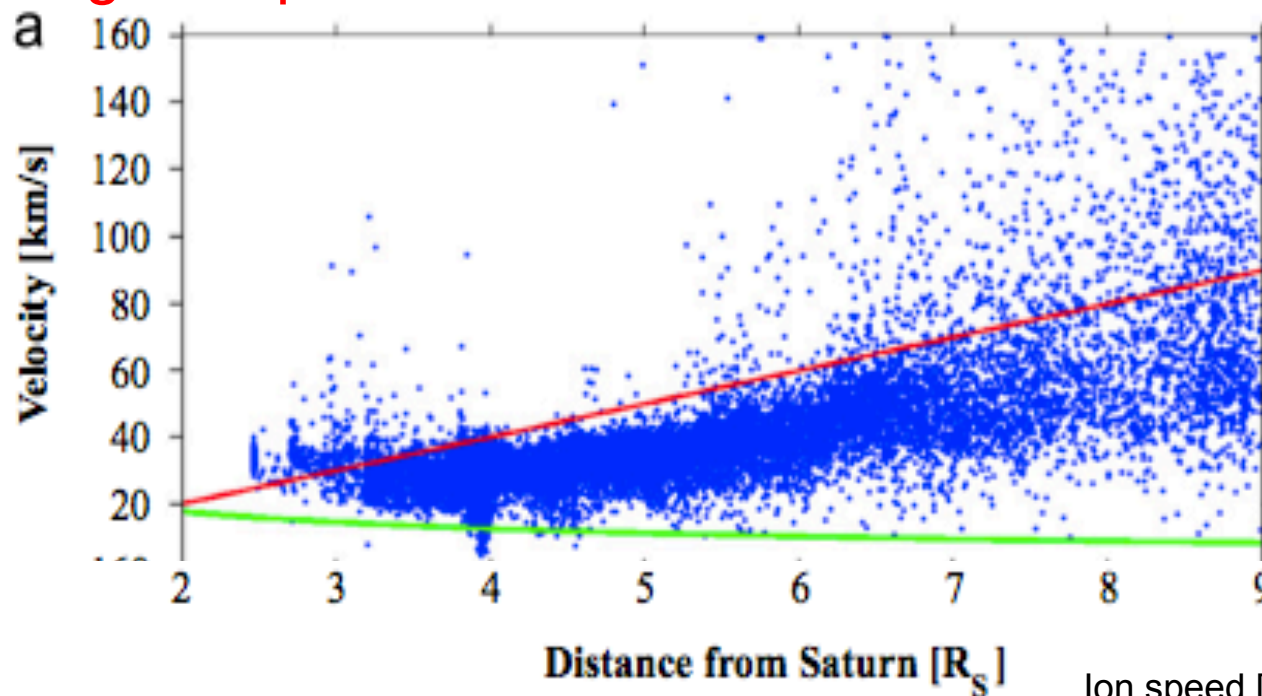
Saturn's case



Co-rotation deviation by dusts?



- Ion observations from the Cassini RPWS/LP in Saturn's magnetosphere
 - Ion has slower speed than the co-rotation [*Wahlund et al.*, 2009; *Morooka et al.*, 2011; *Holmberg et al.*, 2012].
 - Do dusts affect the ion velocities in the inner magnetosphere?



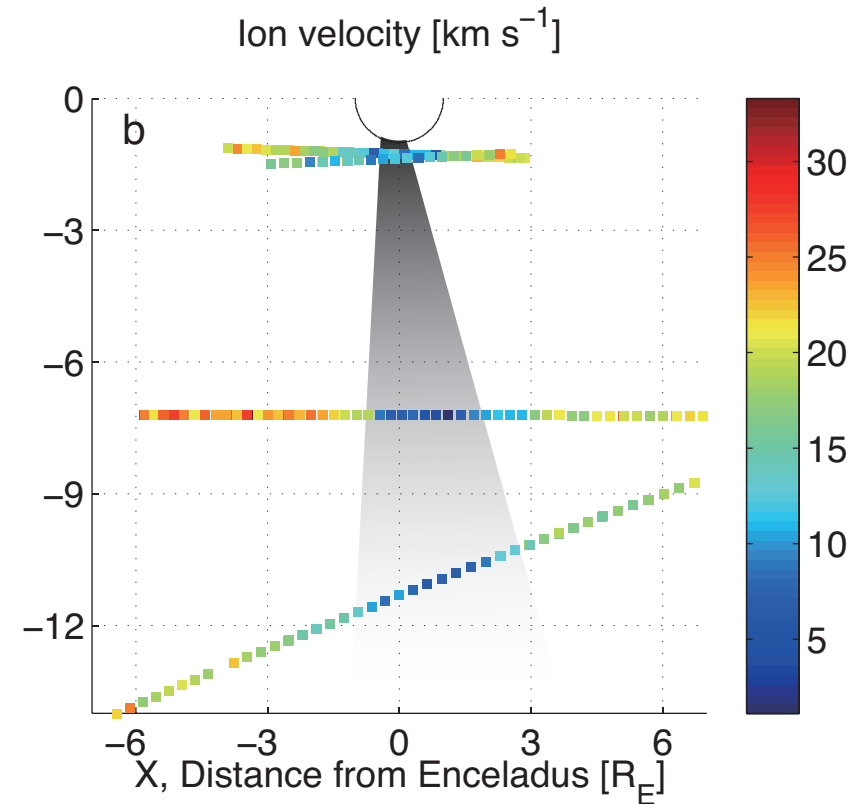
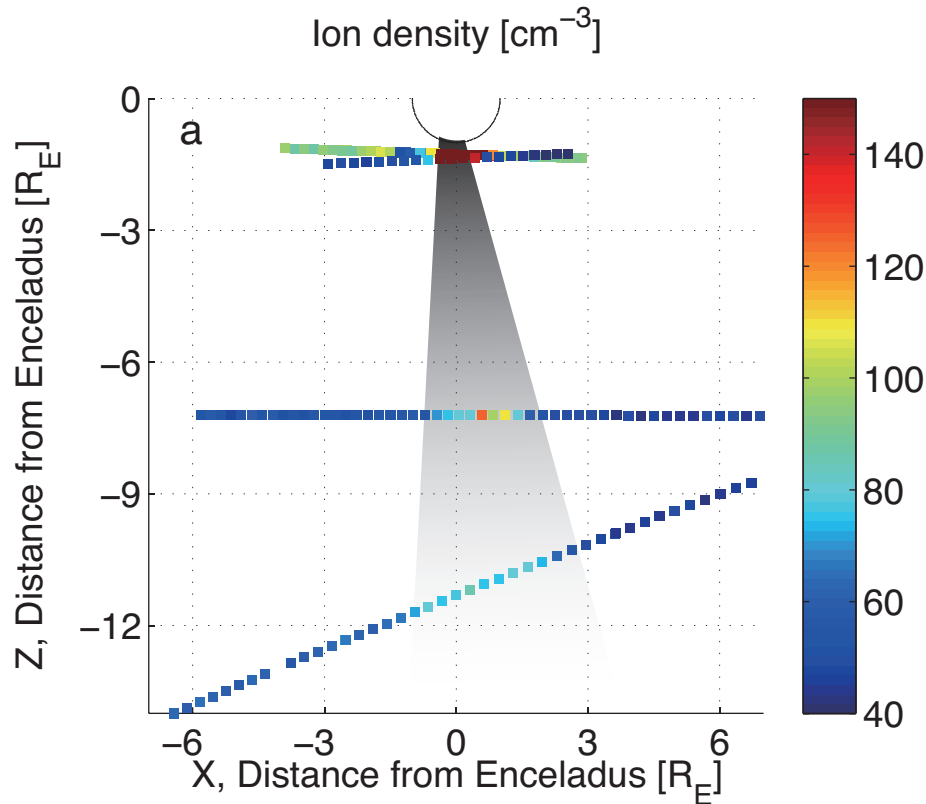
Purpose of this thesis



HOKKAIDO UNIVERSITY

- Investigation of dust-plasma interaction and magnetosphere-ionosphere coupling in the Saturn's inner magnetosphere
- Understanding of generation process for **magnetospheric current, electric field and ion-dust collision**
- Understanding of relationship of **ionospheric conductivity** with the **magnetospheric ion speed**

Plasma in the plume



- Density

- $N_e/N_i < 0.01$ at $1.3 R_E$
 ~ 0.7 at $11 R_E$

- Ion speed

- $V_i \sim V_{\text{Kepler}}$

Charged dust in the plume



- Dust density

$\sim 1.3 R_E$

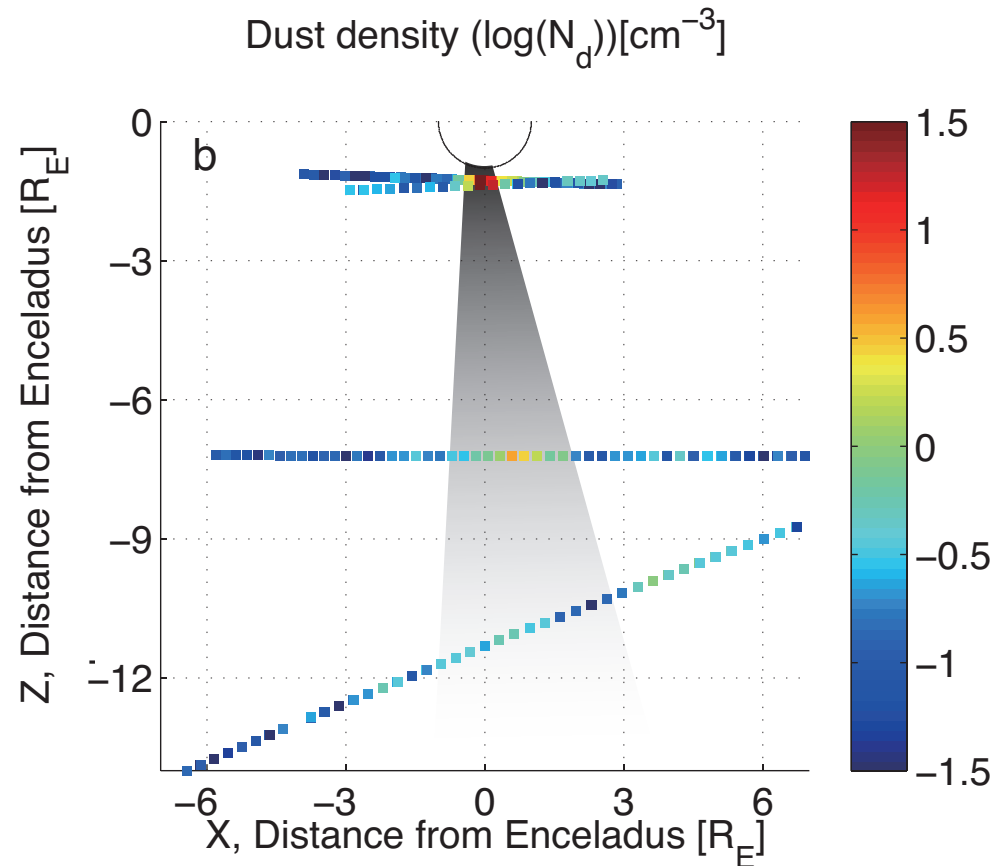
$N_{dmax} > 10 \text{ cm}^{-3}$

$\sim 7 R_E$

$N_{dmax} \sim 1 \text{ cm}^{-3}$

$\sim 11 R_E$

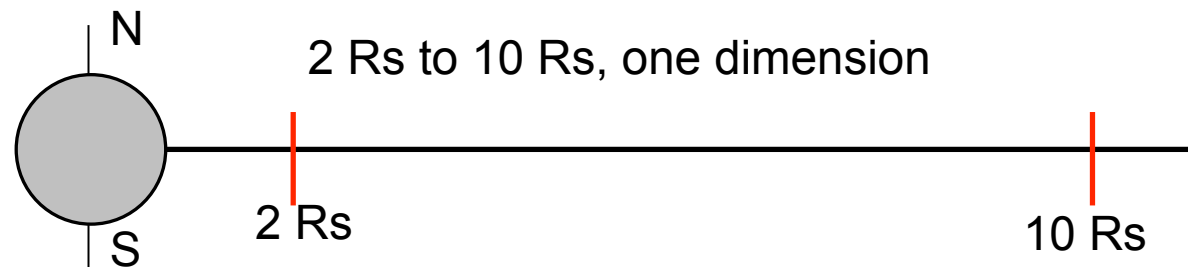
$N_{dmax} \sim 0.1 \text{ cm}^{-3}$





Modeling of the inner magnetosphere

- Multi-fluid model (H^+ , H_2O^+ , dust, e^-)
- 1 dimension (radial direction), $2 R_S$ to $10 R_S$
 - V_r , V_ϕ are calculated.



- Initial condition
 - Ion speed: Co-rotation speed; Dust speed: Keplerian speed
- Boundary condition
 - Inner boundary
 - Ion speed: Co-rotation speed; Dust speed: Keplerian speed
 - Open outer boundary

Inner magnetospheric model



HOKKAIDO UNIVERSITY

- Momentum equations
 - H^+ , H_2O^+ , e^- and dust

$$\rho_k \frac{\partial \mathbf{v}_k}{\partial t} + \rho_k (\mathbf{v}_k \cdot \nabla) \mathbf{v}_k = n_k q_k (\mathbf{E} + \mathbf{v}_k \times \mathbf{B}) - \nabla p_k - \rho_k \mathbf{g} + \sum_l \rho_k \nu_{kl} (\mathbf{v}_k - \mathbf{v}_l) - \sum_l S_{k,l} (\mathbf{v}_k - \mathbf{v}_l)$$

Chemical term

- Dust: $q_d = 4\pi\epsilon_0 r_d \phi$
 - $r_d = 100 \text{ nm}$; $\phi = -2 \text{ V}$

S_k	Production rate
n_k	Number density
\mathbf{B}	Magnetic field
q_d	Charge quantity of dust
r_d	Dust radius
ϕ	Dust surface potential
ϵ_0	Permittivity

\mathbf{v}_k	Velocity
\mathbf{E}	Electric field
\mathbf{g}	Gravity
ρ_k	Mass density
p	Pressure
e	Charge quantity
ν_{kl}	Collision frequency

Chemical reactions



- For ion production rate
 - Water group ion and H⁺
 - 9 reactions

Reactions	Rates [m ³ s ⁻¹]	References
$\text{H}^+ + \text{H}_2\text{O} \rightarrow \text{H} + \text{H}_2\text{O}^+$	2.60×10^{-15}	<i>Burger et al.</i> [2007], <i>Lindsay et al.</i> [1997]
$\text{O}^+ + \text{H}_2\text{O} \rightarrow \text{O} + \text{H}_2\text{O}^+$	2.13×10^{-15}	<i>Burger et al.</i> [2007], <i>Dressler et al.</i> [2006]
$\text{H}_2\text{O}^+ + \text{H}_2\text{O} \rightarrow \text{H}_2\text{O} + \text{H}_2\text{O}^+$	5.54×10^{-16}	<i>Burger et al.</i> [2007], <i>Lishawa et al.</i> [1997]
$\text{H}_2\text{O}^+ + \text{H}_2\text{O} \rightarrow \text{OH} + \text{H}_3\text{O}^+$	3.97×10^{-16}	<i>Burger et al.</i> [2007], <i>Lishawa et al.</i> [1997]
$\text{OH}^+ + \text{H}_2\text{O} \rightarrow \text{OH} + \text{H}_2\text{O}^+$	5.54×10^{-16}	<i>Burger et al.</i> [2007], <i>Itikawa and Mason</i> [2005]
$\text{H}_2\text{O} + \text{e} \rightarrow \text{H}_2\text{O}^+ + 2\text{e}$		<i>Burger et al.</i> [2007], <i>Itikawa and Mason</i> [2005]
$\text{H}_2\text{O} + \text{e} \rightarrow \text{OH}^+ + \text{H} + 2\text{e}$	10^{-18} (total)	<i>Burger et al.</i> [2007], <i>Itikawa and Mason</i> [2005]
$\text{H}_2\text{O} + \text{e} \rightarrow \text{O}^+ + \text{H}_2 + 2\text{e}$		<i>Burger et al.</i> [2007], <i>Itikawa and Mason</i> [2005]
$\text{H}_2\text{O} + \text{e} \rightarrow \text{H}^+ + \text{OH} + 2\text{e}$	10^{-22}	<i>Burger et al.</i> [2007], <i>Itikawa and Mason</i> [2005]

Inner magnetospheric model



HOKKAIDO UNIVERSITY

- Momentum equations
 - H^+ , H_2O^+ , e^- and dust

$$\rho_k \frac{\partial \mathbf{v}_k}{\partial t} + \rho_k (\mathbf{v}_k \cdot \nabla) \mathbf{v}_k = n_k q_k (\mathbf{E} + \mathbf{v}_k \times \mathbf{B}) - \nabla p_k - \rho_k \mathbf{g} + \sum_l \rho_k \nu_{kl} (\mathbf{v}_k - \mathbf{v}_l) - \sum_l S_{k,l} (\mathbf{v}_k - \mathbf{v}_l)$$

Electric field
Collision term
Chemical term

- Dust: $q_d = 4\pi\epsilon_0 r_d \phi$
 - $r_d = 100 \text{ nm}$; $\phi = -2 \text{ V}$

S_k	Production rate	\mathbf{V}_k	Velocity
n_k	Number density	\mathbf{E}	Electric field
\mathbf{B}	Magnetic field	\mathbf{g}	Gravity
q_d	Charge quantity of dust	ρ_k	Mass density
r_d	Dust radius	p	Pressure
ϕ	Dust surface potential	e	Charge quantity
ϵ_0	Permittivity	ν_{kl}	Collision frequency

Electric field



- M-I coupling for deriving **electric field, E**

$$\Sigma_i(\mathbf{E}_{cor} - \mathbf{E}) = \mathbf{j}D$$

$$\mathbf{j} = en_i\mathbf{v}_i - en_e\mathbf{v}_e - q_d n_d \mathbf{v}_d$$

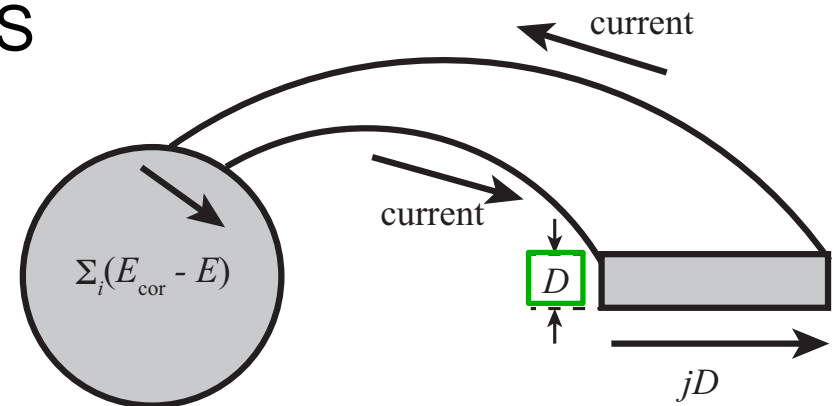


$$\mathbf{E} = \mathbf{E}_{cor} - \frac{\mathbf{j}D}{\Sigma_i}$$

Thickness of dust distribution

\mathbf{j}	Current density
\mathbf{E}_{cor}	Co-rotational Electric field
Σ_i	Ionospheric conductivity
D	Thickness of dust
v_{thk}	Thermal velocity

- Ionospheric conductivity Σ_i : 1 S

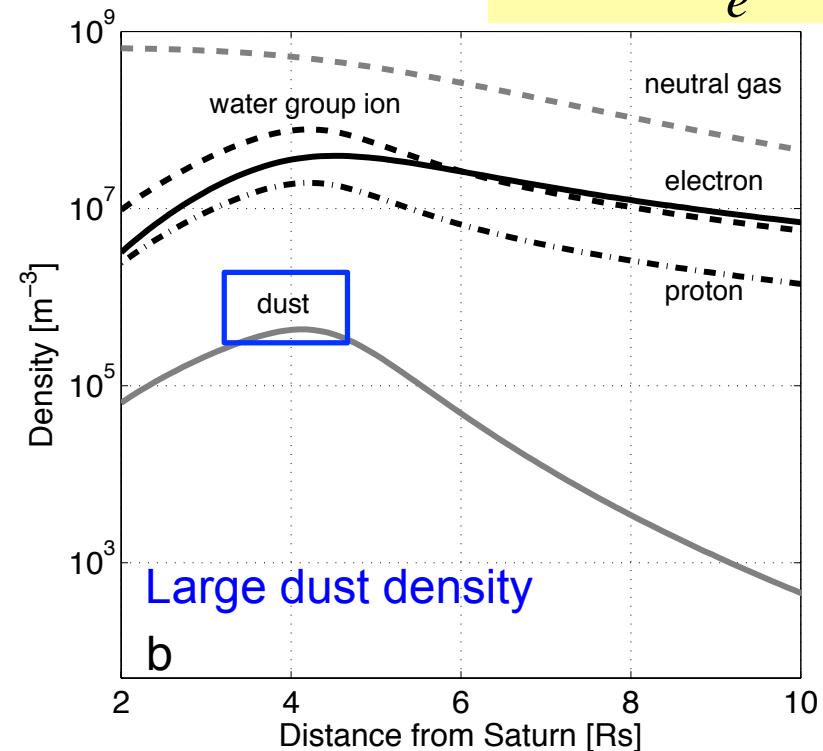
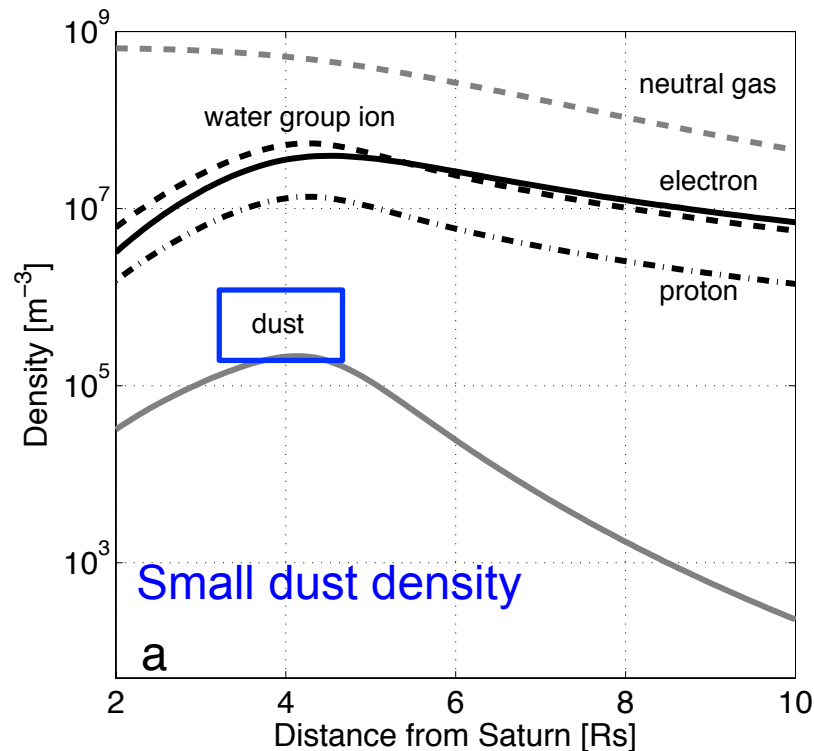


Density profile & Thickness of dust



- 2 cases for dust density N_d

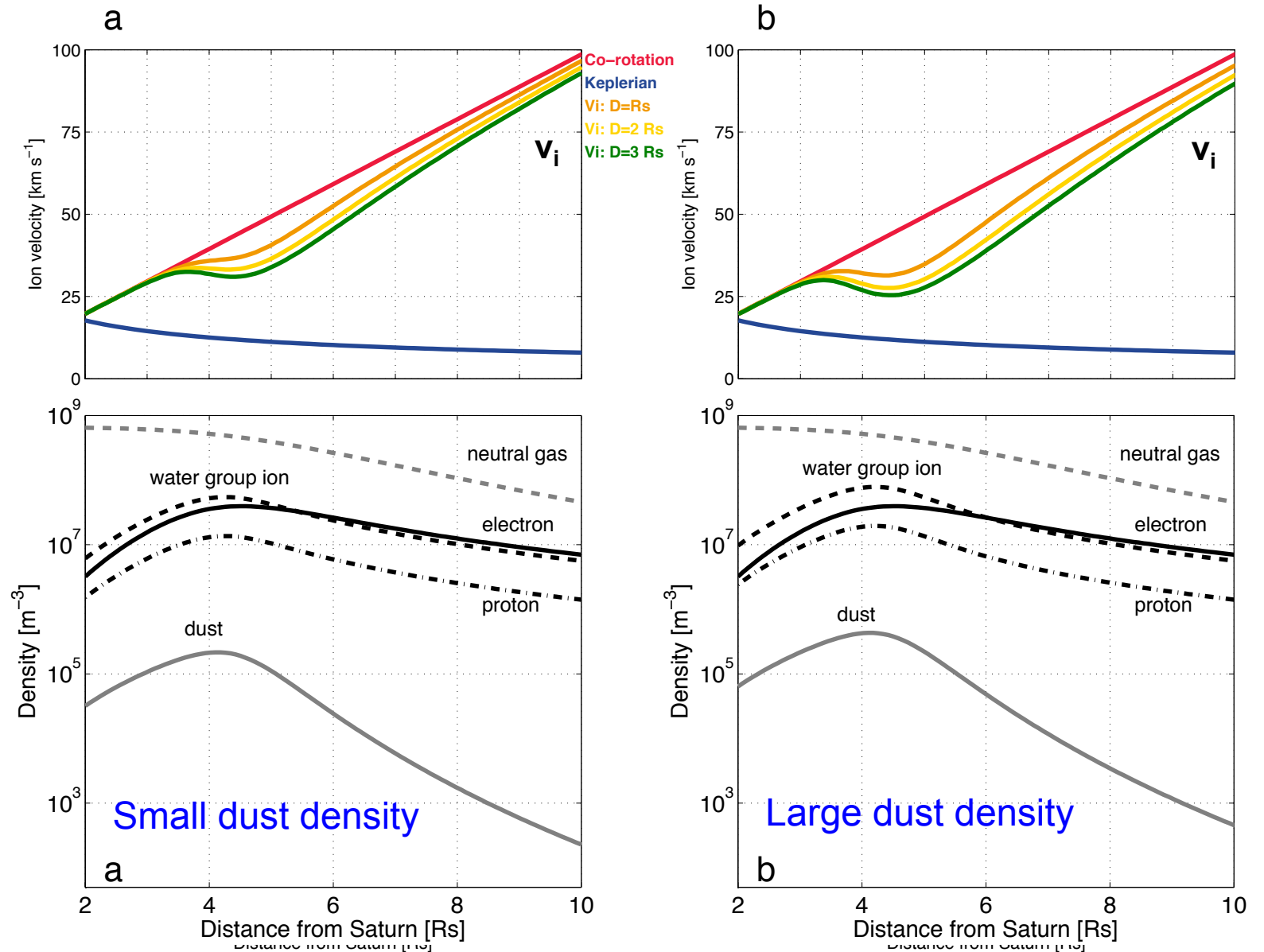
$$n_w = n_e + \frac{q_d}{e} n_d - n_p$$



- 3 cases for thickness of dust distribution D

1. $D = R_S$
2. $D = 2 R_S$
3. $D = 3 R_S$

Results: Ion velocity



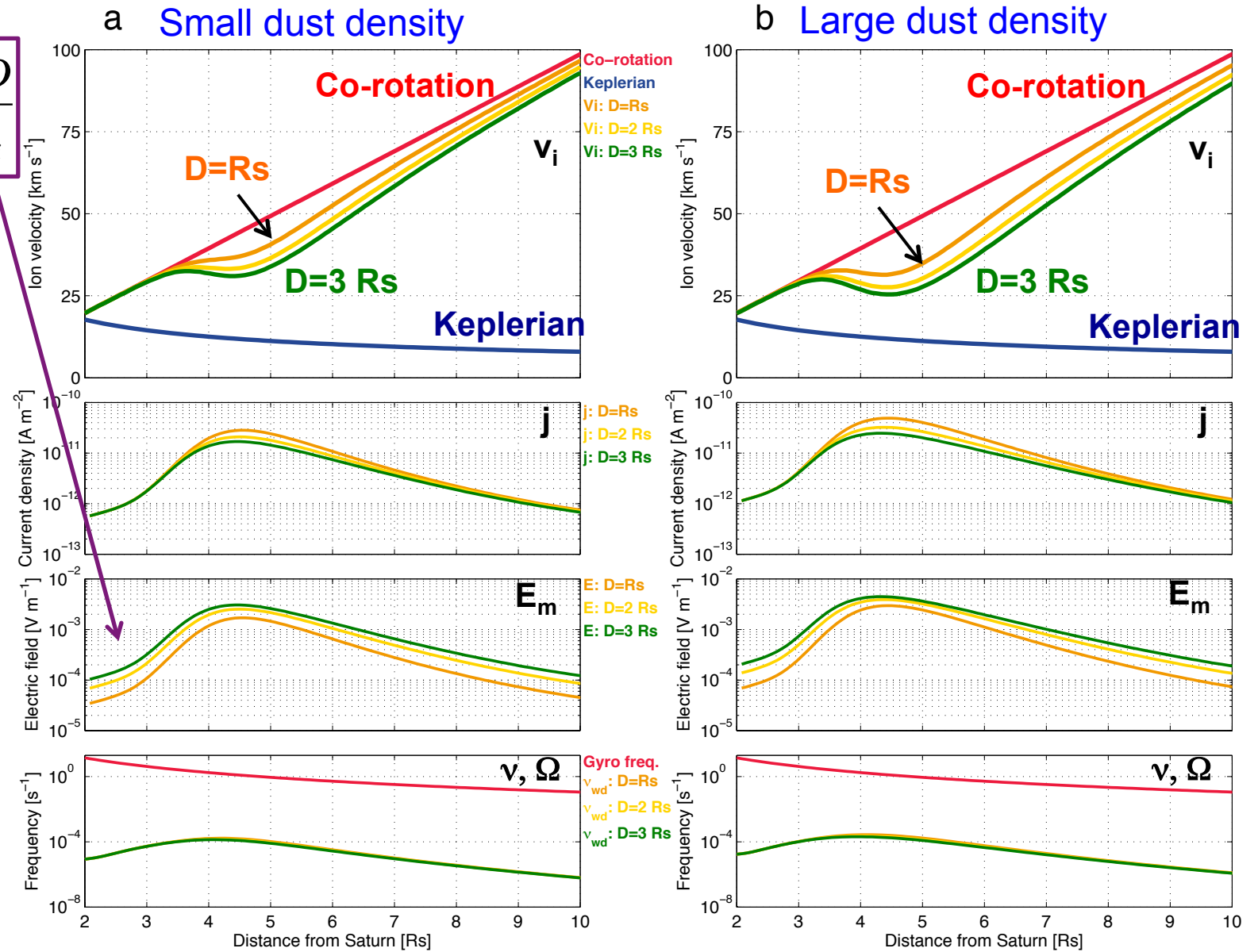
Results: Ion velocity



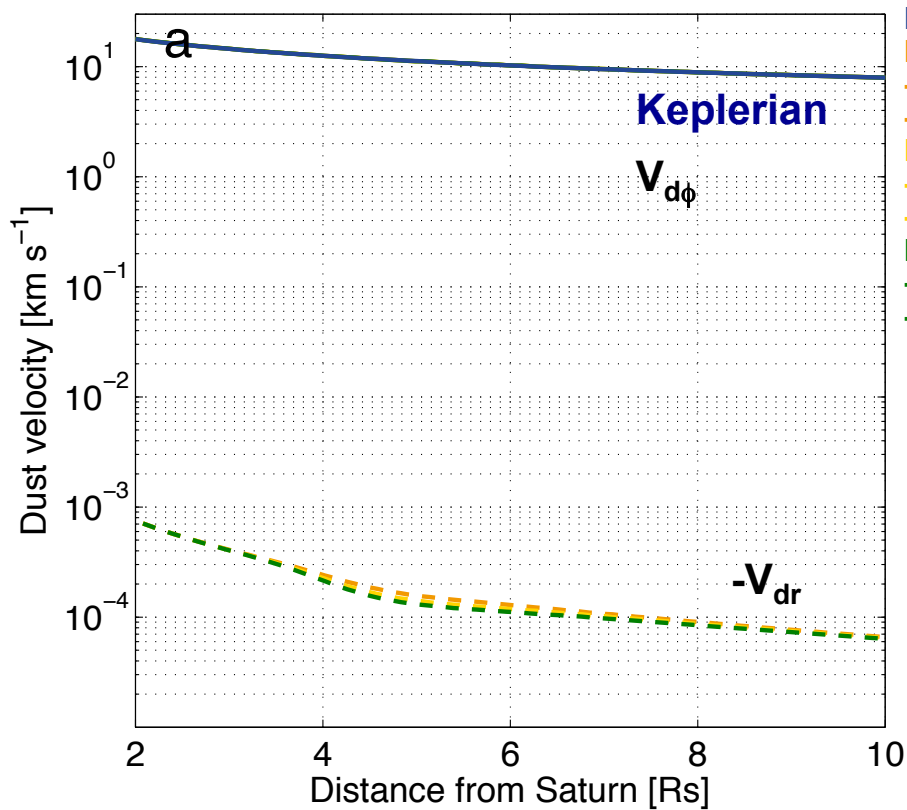
$$\mathbf{E} = \mathbf{E}_{cor} - \frac{\mathbf{j}D}{\Sigma_i}$$

$$\mathbf{v}_i \approx \frac{\mathbf{E} \times \mathbf{B}}{B^2}$$

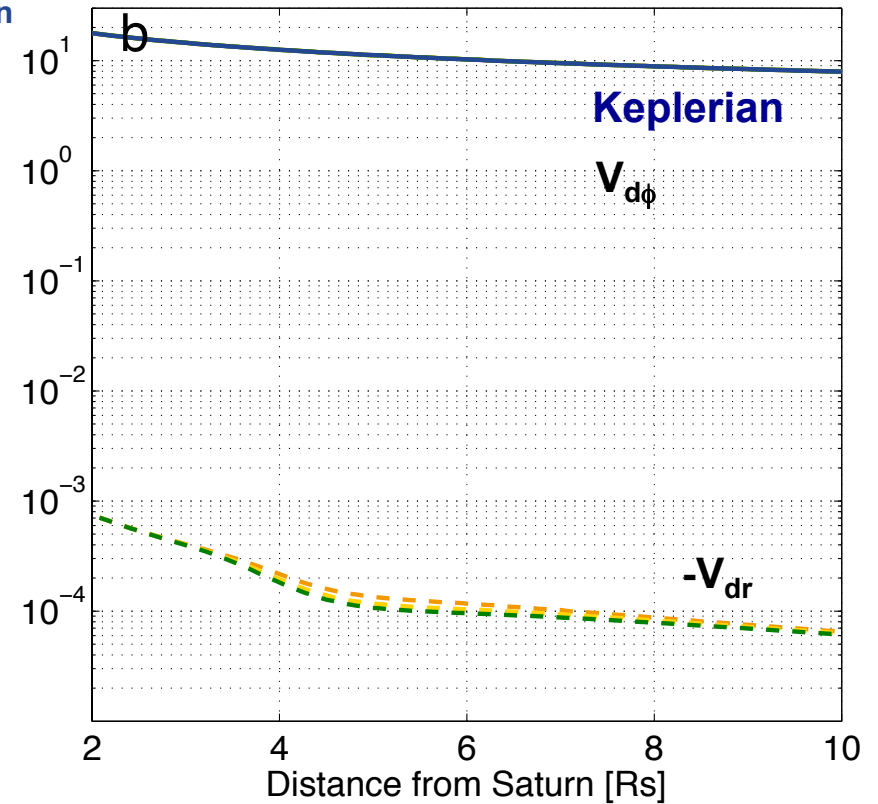
$$\ll \mathbf{v}_{cor}$$



Results: Dust velocity



Small dust density



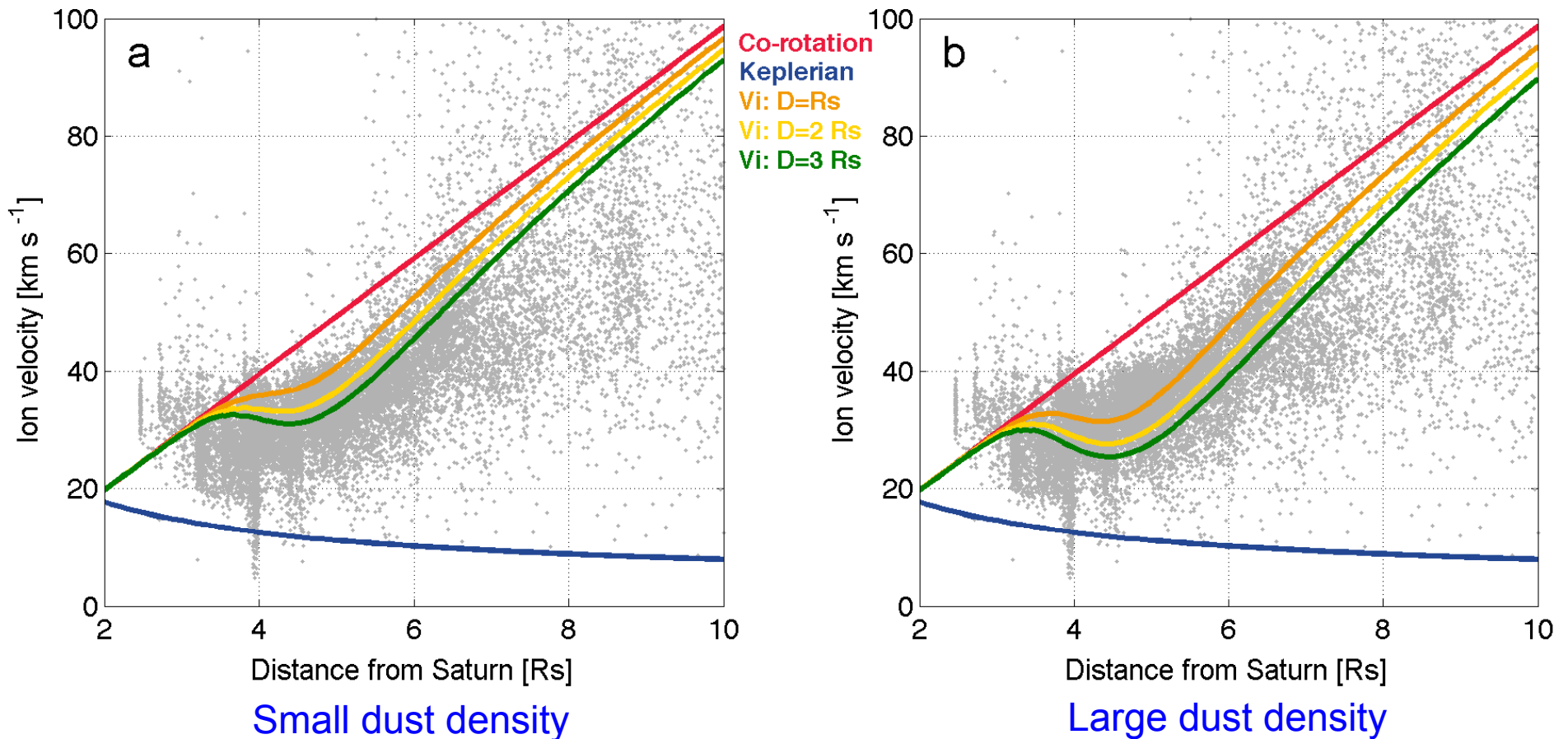
Large dust density

- V_d is almost Keplerian.
 - However, dusts are slightly affected by the electric field.

Comparison with LP observation



HOKKAIDO UNIVERSITY



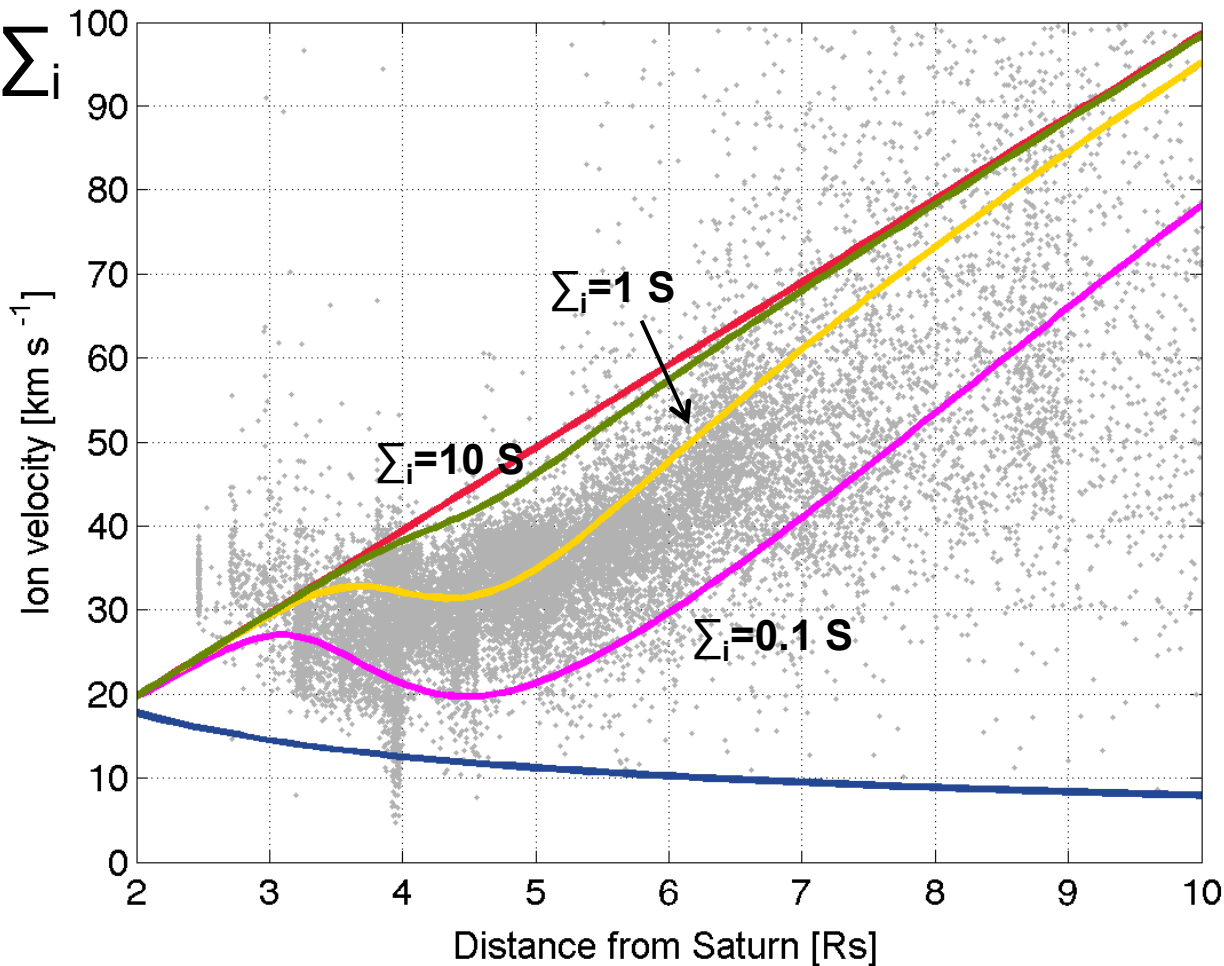
- Consistent with observations in $N_d > \sim 10^5 \text{ m}^{-3}$ and/or $D > 1 R_S$.

Comparison with LP observation



- Change Σ_i
 - 0.1 S
 - 1 S
 - 10 S

$$\Sigma_i(\mathbf{E}_{cor} - \mathbf{E}) = \mathbf{j}D$$



- V_i is slower when Σ_i is smaller.
- V_i strongly depends on Σ_i .

- Co-rotation lag
 - Dust-plasma interaction
 - The dust–plasma interaction is significant when D is large and/or N_d is high.
 - $N_{d \max} > \sim 10^5 \text{ m}^{-3}$
 - $D > 1 R_S$
 - The inner magnetospheric total current along a magnetic field line weakens E .
 - V_d is almost the Keplerian.
 - However, dusts are slightly affected by this interaction.
- Ionosphere and magnetosphere are strongly coupled.
 - V_i depends on Σ_i .



Modeling of the ionosphere & Magnetosphere-ionosphere coupling

Co-rotation deviation by dusts?



- Ionospheric Pedersen conductivity
 - E depends on the conductivity.

$$\rho_k \frac{\partial \mathbf{v}_k}{\partial t} + \rho_k (\mathbf{v}_k \cdot \nabla) \mathbf{v}_k = n_k q_k (\mathbf{E} + \mathbf{v}_k \times \mathbf{B}) - \nabla p_k - \rho_k \mathbf{g} + \sum_l \rho_k \nu_{kl} (\mathbf{v}_k - \mathbf{v}_l) - \sum_l S_{k,l} (\mathbf{v}_k - \mathbf{v}_l)$$

Electric field

$$\sum_i (\mathbf{E}_{cor} - \mathbf{E}) = \mathbf{j}D$$

Pedersen conductivity

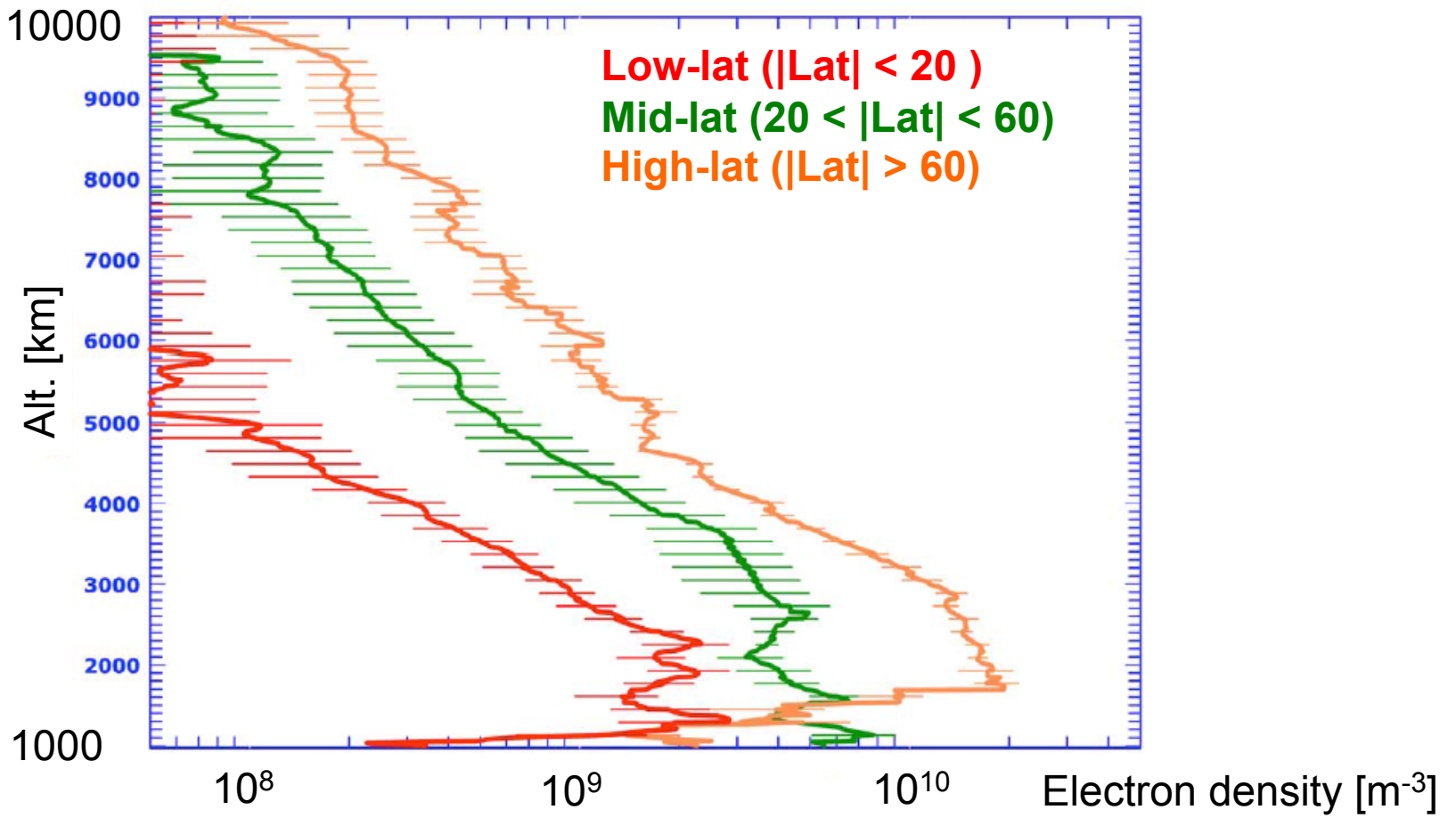
$$\sigma_p = \sum_i \frac{\nu_i}{\nu_{in}^2 + \omega_{ci}^2} \frac{n_i e^2}{m_i} + \frac{\nu_e}{\nu_{en}^2 + \omega_{ce}^2} \frac{n_e e^2}{m_e} \quad \Sigma_i = \int_{z_1}^{z_2} \sigma_p ds$$

- However, it is one of the open questions.
 - ~0.1-100 S [Connerney *et al.*, 1983; Cheng and Waite, 1988]
 - ~0.02 S [Saur *et al.*, 2004]
 - 1--10 S [Cowley *et al.*, 2004; Moore *et al.*, 2010]
- We find the ionospheric N_i for deriving Σ_i .

Saturn's ionosphere



- N_e observation from Cassini occultations
 - N_e (average between dusk and dawn)
 - Peak density: $\sim 10^{10} \text{ m}^{-3}$; Peak alt.: $\sim 1200 \text{ km}$



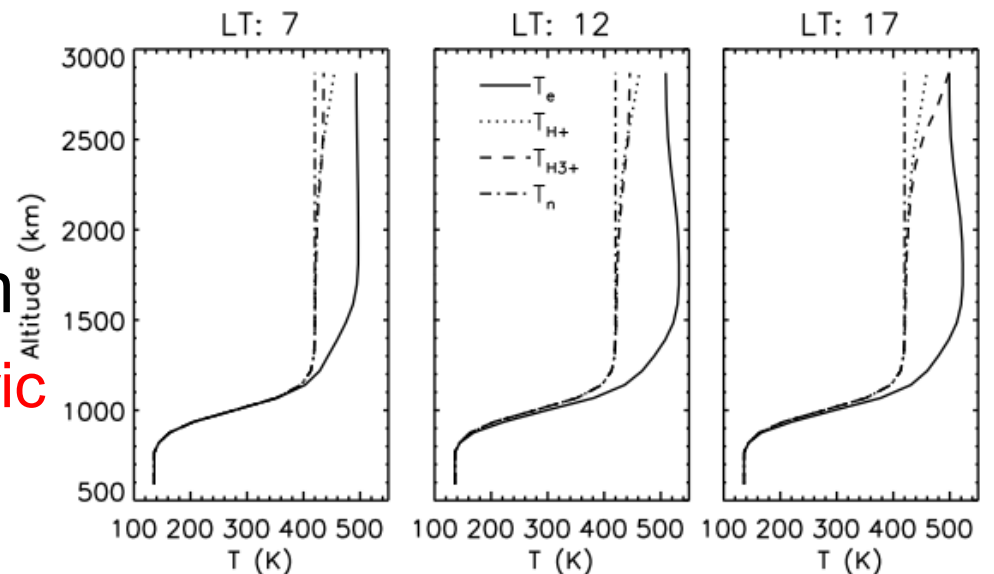
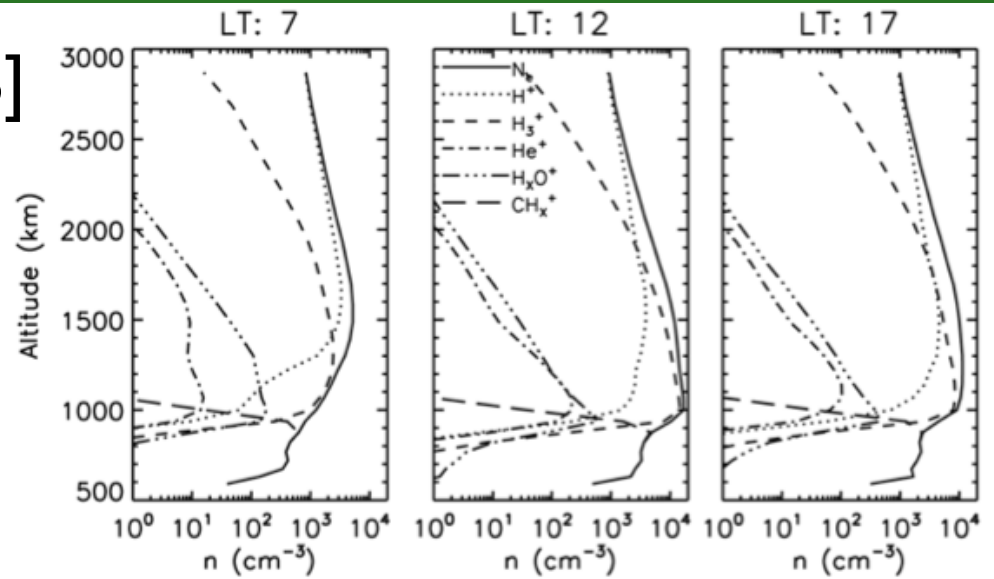
Electron density by occultations [*Kliore et al.*, 2009]

Saturn's ionosphere



- Model [*Moore et al. 2008*]

- N_e
 - Average peak density: $\sim 10^{10} \text{ m}^{-3}$
 - Peak alt.: $\sim 1200 \text{ km}$
- T_e
 - Max: 500 K
 - Alt.: $> 1500 \text{ km}$



- But only below $\sim 3000 \text{ km}$

- How is the magnetospheric influence?

- Construction of an ionospheric model including the inner magnetosphere.
- Estimation of the **ionospheric Pedersen conductivity** from **plasma density** in the Saturn's ionosphere
- Investigation of the influence of magnetosphere to ionosphere

3 dimensional ionospheric model



HOKKAIDO UNIVERSITY

- Primitive equations

- Ion

Density:
$$\frac{\partial \rho_i}{\partial t} + \frac{1}{A} \frac{\partial (A \rho_i v_{i,\parallel})}{\partial s} = S_i - L_i$$

Momentum:
$$\rho_i \frac{\partial v_{i,\parallel}}{\partial t} + \rho_i v_{i,\parallel} \frac{\partial v_{i,\parallel}}{\partial s} = n_i e E_{\parallel} - \frac{\partial p_i}{\partial s} - \rho_i g - \sum_k \rho_i v_{ik} (v_{i,\parallel} - v_{k,\parallel})$$

Temperature: $T_i = T_e$

v_{\parallel}	Field-aligned Velocity
E_{\parallel}	Electric field
A	Magnetic flux cross-section
g	Gravity and CF
T	Temperature
Q	Heating rate
κ	Diffusion coefficient

- Electron

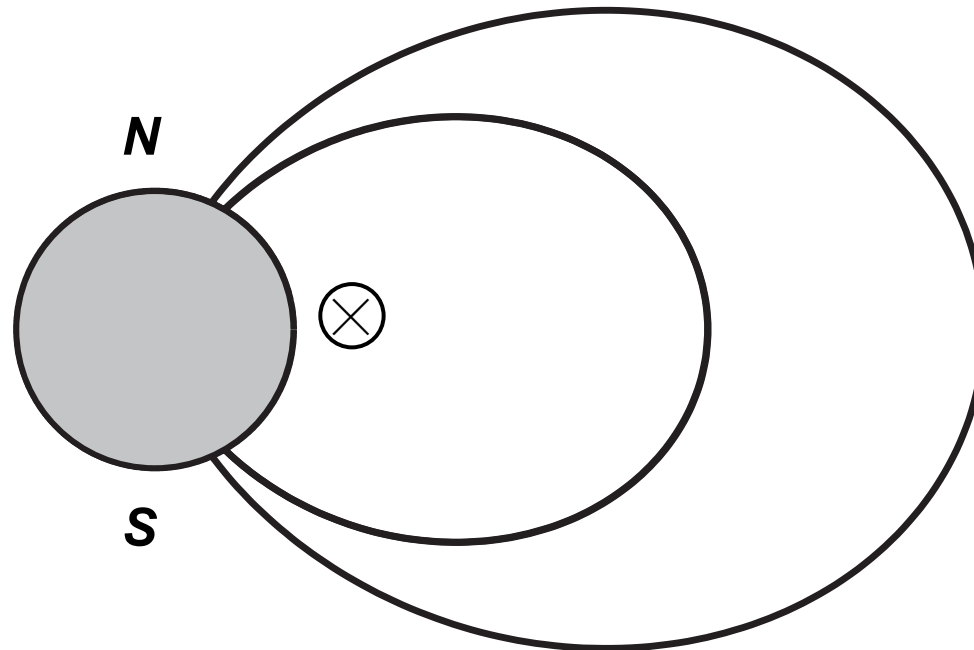
Density:
$$n_e = \sum_i n_i$$

Momentum:
$$E_{\parallel} = -\frac{1}{en_e} \frac{\partial p_e}{\partial s}$$

Temperature:
$$\frac{\partial T_e}{\partial t} - \frac{2}{3} \frac{1}{A} \frac{\partial}{\partial s} \left(A \kappa_e \frac{\partial T_e}{\partial s} \right) = Q_{EUV} + Q_{coll} + Q_{joule} + Q_{ph,ionos} + Q_{ph,mag}$$

N_i (H^+ , H_2^+ , H_3^+ , He^+ , H_2O^+ and H_3O^+),
 V_i (H^+ , H_2^+ , H_3^+ , He^+ , H_2O^+ and H_3O^+),
 T_e, T_i

- Dipole coordinate system
 - Along the magnetic field line \rightarrow 1 dimension
 - + Increasing the number of magnetic field line \rightarrow 2 dimensions
 - + Time evolution \rightarrow 3 dimensions



3 dimensional ionospheric model



HOKKAIDO UNIVERSITY

• Primitive equations

• Ion

Density:
$$\frac{\partial \rho_i}{\partial t} + \frac{1}{A} \frac{\partial (A \rho_i v_{i,\parallel})}{\partial s} = \boxed{S_i - L_i}$$
 Source and Loss rate

Momentum:
$$\rho_i \frac{\partial v_{i,\parallel}}{\partial t} + \rho_i v_{i,\parallel} \frac{\partial v_{i,\parallel}}{\partial s} = n_i e E_{\parallel} - \frac{\partial p_i}{\partial s} - \rho_i g - \sum_k \rho_i v_{ik} (v_{i,\parallel} - v_{k,\parallel})$$

Temperature: $T_i = T_e$

v_{\parallel}	Field-aligned Velocity
E_{\parallel}	Electric field
A	Magnetic flux cross-section
g	Gravity and CF
T	Temperature
Q	Heating rate
κ	Diffusion coefficient

• Electron

Density:
$$n_e = \sum_i n_i$$

Momentum:
$$E_{\parallel} = -\frac{1}{en_e} \frac{\partial p_e}{\partial s}$$

Temperature:
$$\frac{\partial T_e}{\partial t} - \frac{2}{3} \frac{1}{A} \frac{\partial}{\partial s} \left(A \kappa_e \frac{\partial T_e}{\partial s} \right) = Q_{EUV} + Q_{coll} + Q_{joule} + Q_{ph,ionos} + Q_{ph,mag}$$

N_i (H^+ , H_2^+ , H_3^+ , He^+ , H_2O^+ and H_3O^+),
 V_i (H^+ , H_2^+ , H_3^+ , He^+ , H_2O^+ and H_3O^+),
 T_e, T_i

Source & Loss



- Chemical reactions of 6 ion components
 - H^+ , H_2^+ , H_3^+ , He^+ , H_2O^+ and H_3O^+
 - 29 reactions

Chemical reaction	Rate coefficients	References
$H + h\nu \rightarrow H^+ + e^-$		<i>Moses and Bass</i> [2000]
$H_2 + h\nu \rightarrow H^+ + H + e^-$		<i>Moses and Bass</i> [2000]
$H_2 + h\nu \rightarrow H_2^+ + e^-$		<i>Moses and Bass</i> [2000]
$He + h\nu \rightarrow He^+ + e^-$		<i>Moses and Bass</i> [2000]
$H_2O + h\nu \rightarrow H^+ + OH + e^-$		<i>Moses and Bass</i> [2000]
$H_2O + h\nu \rightarrow H_2O^+ + e^-$		<i>Moses and Bass</i> [2000]
$H^+ + e^- \rightarrow H$	$1.9 \times 10^{-16} T_e^{-0.7}$	<i>Moses and Bass</i> [2000]; <i>Kim and Fox</i> [1994]
$H_2^+ + e^- \rightarrow H + H$	$2.3 \times 10^{-12} T_e^{-0.4}$	<i>Moses and Bass</i> [2000]; <i>Kim and Fox</i> [1994]
$H_3^+ + e^- \rightarrow H_2 + H$	$7.6 \times 10^{-13} T_e^{-0.5}$	<i>Moses and Bass</i> [2000]; <i>Kim and Fox</i> [1994]
$H_3^+ + e^- \rightarrow 3H$	$9.7 \times 10^{-13} T_e^{-0.5}$	<i>Moses and Bass</i> [2000]; <i>Kim and Fox</i> [1994]
$He^+ + e^- \rightarrow He$	$1.9 \times 10^{-16} T_e^{-0.7}$	<i>Moses and Bass</i> [2000]; <i>Kim and Fox</i> [1994]
$H_2O^+ + e^- \rightarrow O + H_2$	$3.5 \times 10^{-12} T_e^{-0.5}$	<i>Moses and Bass</i> [2000]; <i>Miller et al.</i> [1997]
$H_2O^+ + e^- \rightarrow OH + H$	$2.8 \times 10^{-12} T_e^{-0.5}$	<i>Moses and Bass</i> [2000]; <i>Miller et al.</i> [1997]
$H_3O^+ + e^- \rightarrow H_2O + H$	$6.1 \times 10^{-12} T_e^{-0.5}$	<i>Moses and Bass</i> [2000]; <i>Miller et al.</i> [1997]
$H_3O^+ + e^- \rightarrow OH + 2H$	$1.1 \times 10^{-11} T_e^{-0.5}$	<i>Moses and Bass</i> [2000]; <i>Miller et al.</i> [1997]
$H^+ + H_2 \rightarrow H_2^+ + H$	see text	<i>Moses and Bass</i> [2000]
$H^+ + H_2 + M \rightarrow H_3^+ + M$	3.2×10^{-41}	<i>Moses and Bass</i> [2000]; <i>Kim and Fox</i> [1994]
$H^+ + H_2O \rightarrow H_2O^+ + H$	8.2×10^{-15}	<i>Moses and Bass</i> [2000]; <i>Anicich</i> [1993]
$H_2^+ + H \rightarrow H^+ + H_2$	6.4×10^{-16}	<i>Moses and Bass</i> [2000]; <i>Anicich</i> [1993]
$H_2^+ + H_2 \rightarrow H_3^+ + H$	2.0×10^{-15}	<i>Moses and Bass</i> [2000]; <i>Kim and Fox</i> [1994]
$H_2^+ + H_2O \rightarrow H_2O^+ + H_2$	3.9×10^{-15}	<i>Moses and Bass</i> [2000]; <i>Anicich</i> [1993]
$H_2^+ + H_2O \rightarrow H_3O^+ + H$	3.4×10^{-15}	<i>Moses and Bass</i> [2000]; <i>Anicich</i> [1993]
$H_3^+ + H_2O \rightarrow H_3O^+ + H_2$	5.3×10^{-15}	<i>Moses and Bass</i> [2000]; <i>Anicich</i> [1993]
$He^+ + H_2 \rightarrow H^+ + H + He$	8.8×10^{-20}	<i>Matcheva et al.</i> [2001]; <i>Perry</i> [1999]
$He^+ + H_2 \rightarrow H_2^+ + He$	9.4×10^{-21}	<i>Moses and Bass</i> [2000]; <i>Kim and Fox</i> [1994]
$He^+ + H_2O \rightarrow H^+ + OH + He$	1.9×10^{-16}	<i>Moses and Bass</i> [2000]; <i>Anicich</i> [1993]
$He^+ + H_2O \rightarrow H_2O^+ + He$	5.5×10^{-17}	<i>Moses and Bass</i> [2000]; <i>Anicich</i> [1993]
$H_2O^+ + H_2 \rightarrow H_3O^+ + H$	7.6×10^{-16}	<i>Moses and Bass</i> [2000]; <i>Anicich</i> [1993]
$H_2O^+ + H_2O \rightarrow H_3O^+ + OH$	1.9×10^{-15}	<i>Moses and Bass</i> [2000]; <i>Anicich</i> [1993]

3 dimensional ionospheric model



HOKKAIDO UNIVERSITY

• Primitive equations

• Ion

Density:
$$\frac{\partial \rho_i}{\partial t} + \frac{1}{A} \frac{\partial (A \rho_i v_{i,\parallel})}{\partial s} = \boxed{S_i - L_i}$$
 Source and Loss rate

Momentum:
$$\rho_i \frac{\partial v_{i,\parallel}}{\partial t} + \rho_i v_{i,\parallel} \frac{\partial v_{i,\parallel}}{\partial s} = n_i e E_{\parallel} - \frac{\partial p_i}{\partial s} - \rho_i g - \sum_k \rho_i v_{ik} (v_{i,\parallel} - v_{k,\parallel})$$

Temperature: $T_i = T_e$

v_{\parallel}	Field-aligned Velocity
E_{\parallel}	Electric field
A	Magnetic flux cross-section
g	Gravity and CF
T	Temperature
Q	Heating rate
κ	Diffusion coefficient

• Electron

Density:
$$n_e = \sum_i n_i$$

Momentum:
$$E_{\parallel} = -\frac{1}{en_e} \frac{\partial p_e}{\partial s}$$

Temperature:
$$\frac{\partial T_e}{\partial t} - \frac{2}{3} \frac{1}{A} \frac{\partial}{\partial s} \left(A \kappa_e \frac{\partial T_e}{\partial s} \right) = \boxed{Q_{EUUV} + Q_{coll} + Q_{joule} + Q_{ph,ionos} + Q_{ph,mag}}$$

Heat flow, Q_{HF}

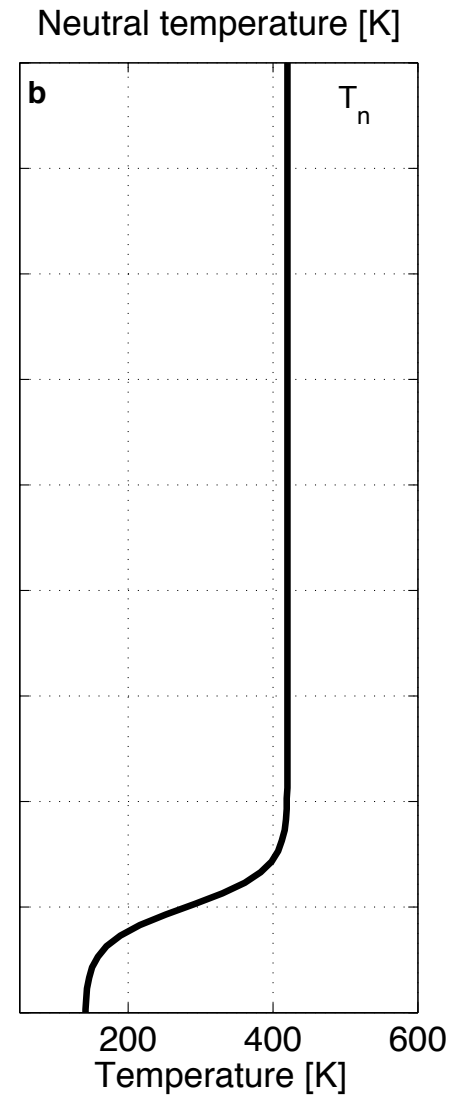
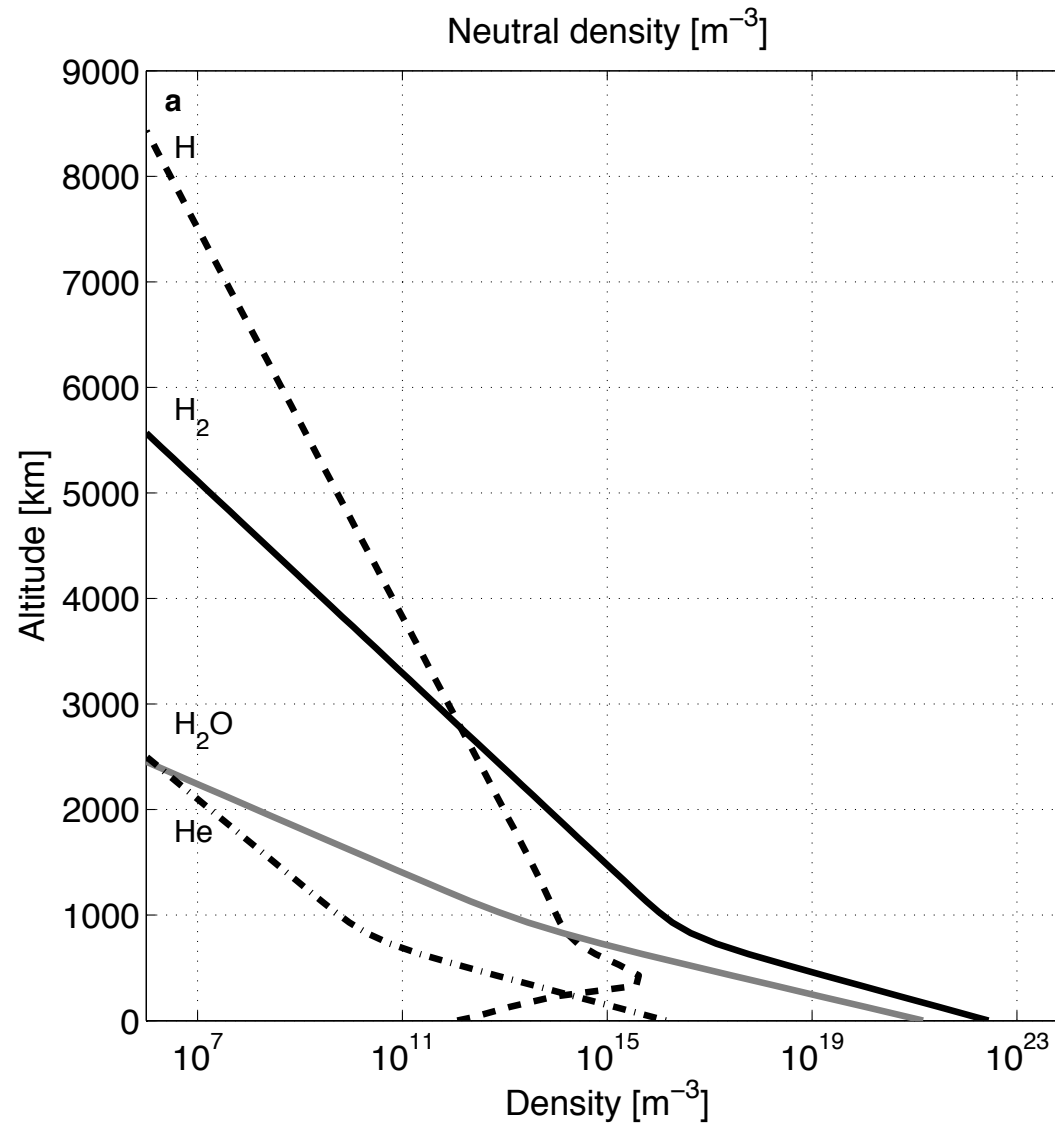
Heating rate

N_i (H^+ , H_2^+ , H_3^+ , He^+ , H_2O^+ and H_3O^+),
 V_i (H^+ , H_2^+ , H_3^+ , He^+ , H_2O^+ and H_3O^+),
 T_e, T_i

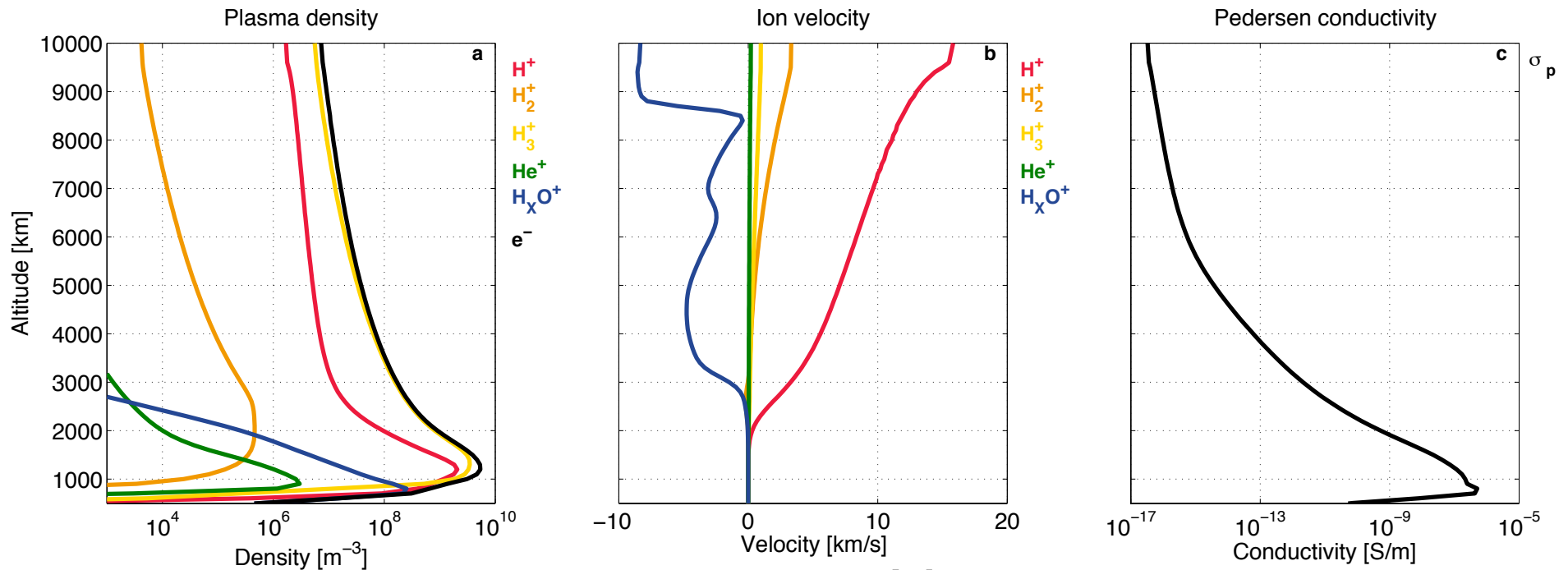
Background neutral atmosphere



HOKKAIDO UNIVERSITY



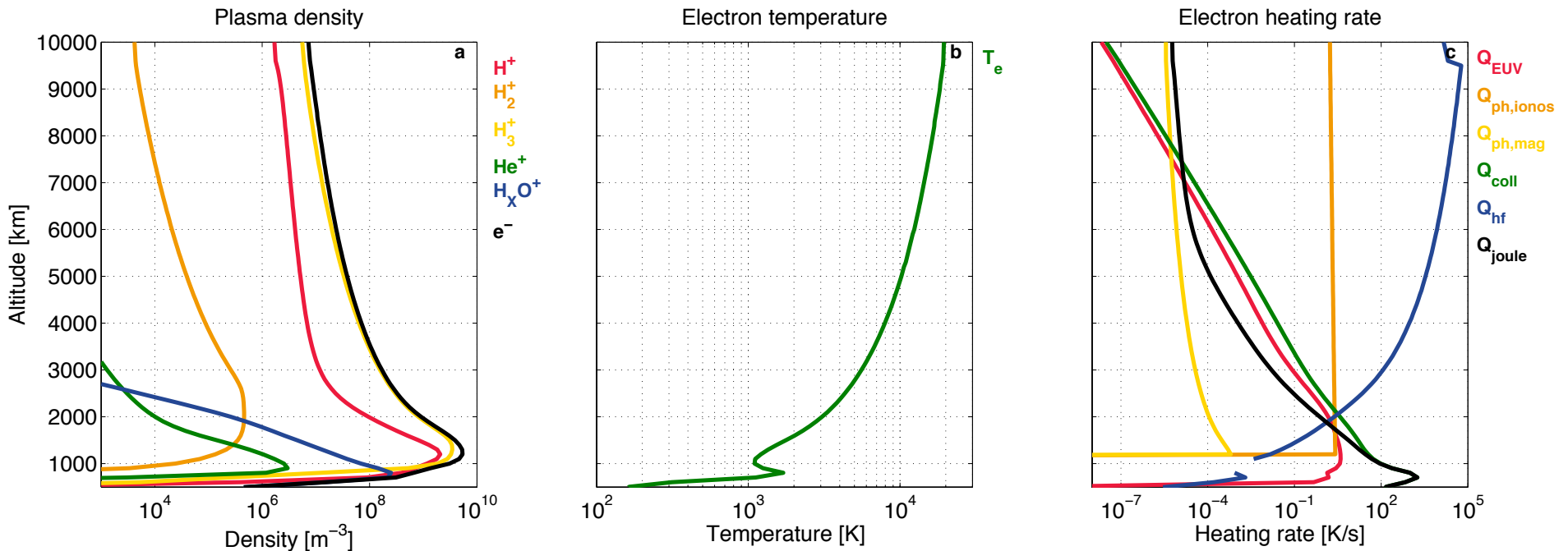
N_i, V_i, σ_p (L=5, LT=12)



- N_i
 - H_3^+ is dominant.
 - Max: $\sim 10^{10} \text{ m}^{-3}$
- σ_i
 - Maximum around 1000 km

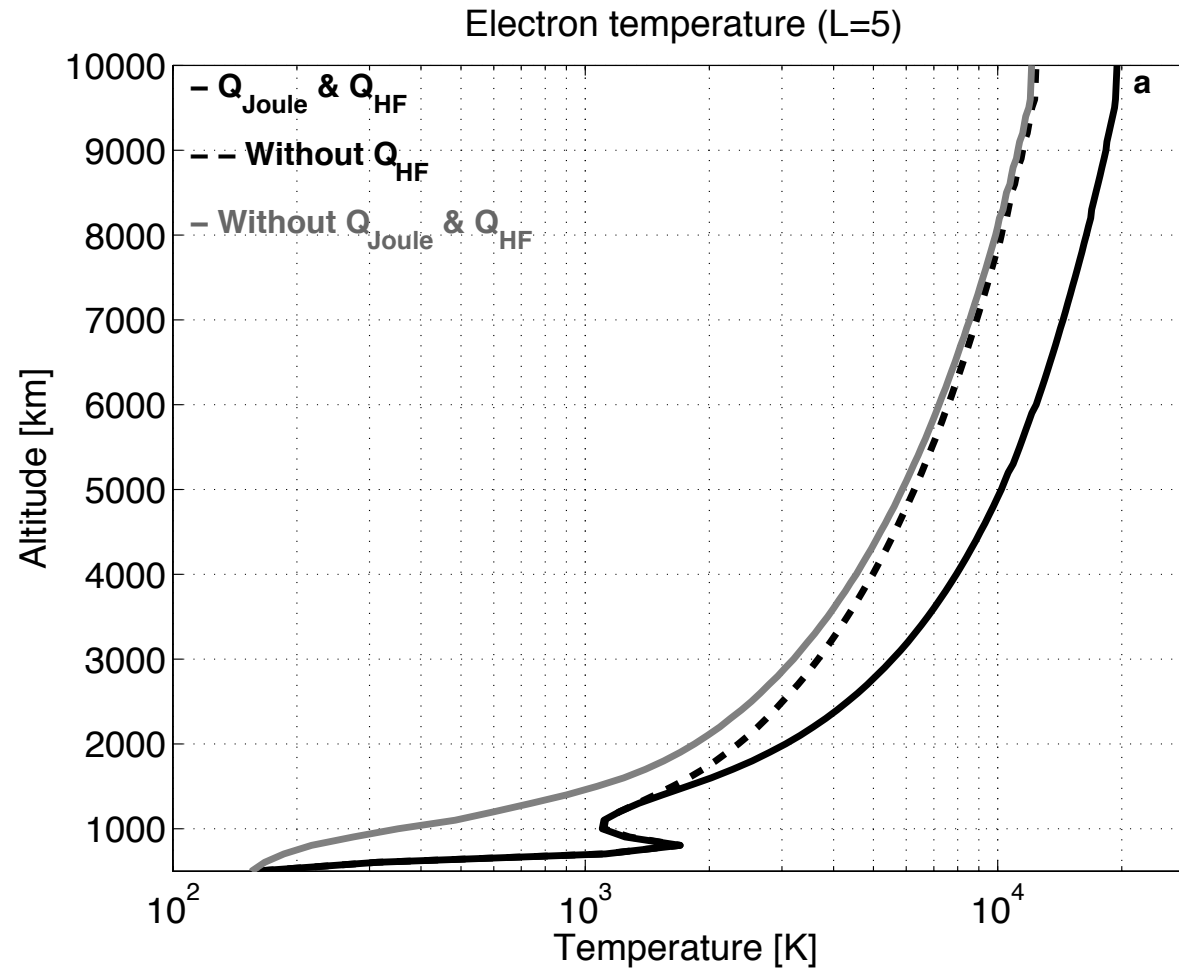
- V_i
 - Upward velocity
 - Light component
 - Downward velocity
 - Heavy component

N_i, T_e, Q_e (L=5, LT=12)



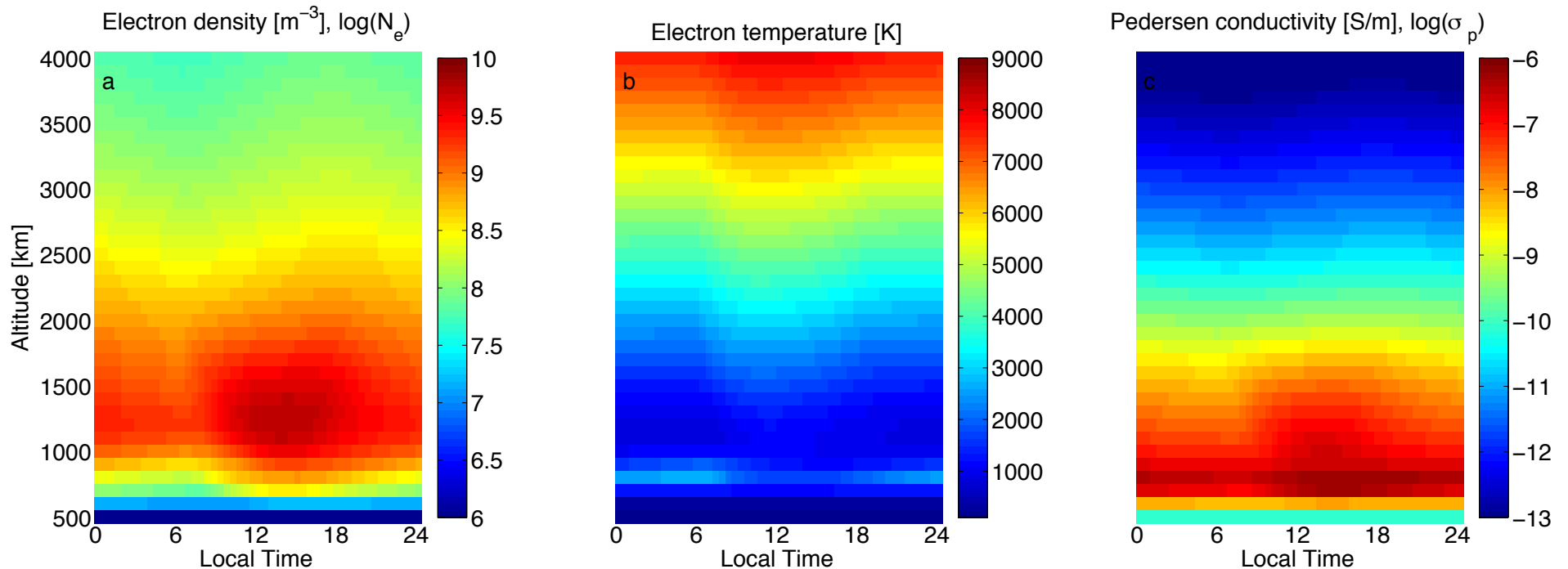
- T_e
 - 2000 K at ~1200 km
 - T_e drastically increases.
- Heating rate
 - Q_{Joule} and Q_{coll} are important at low altitude.
 - Q_{HF} is contributing to heat process above topside.

Joule heating & Heat flow



- T_e doesn't have a peak without Q_{Joule} .
- T_e decreases at topside without Q_{HF} .

Diurnal variations of N_e , T_e and σ_p (L=5) HOKKAIDO UNIVERSITY



- N_e , σ_p
 - Start to increase after 6 LT
 - Max: ~14 LT
 - N_e and σ_p decreases at high altitudes.

- T_e
 - Max: ~12 LT
 - T_e is kept to high temperature in all LT by Q_{HF} .

Pedersen conductivity

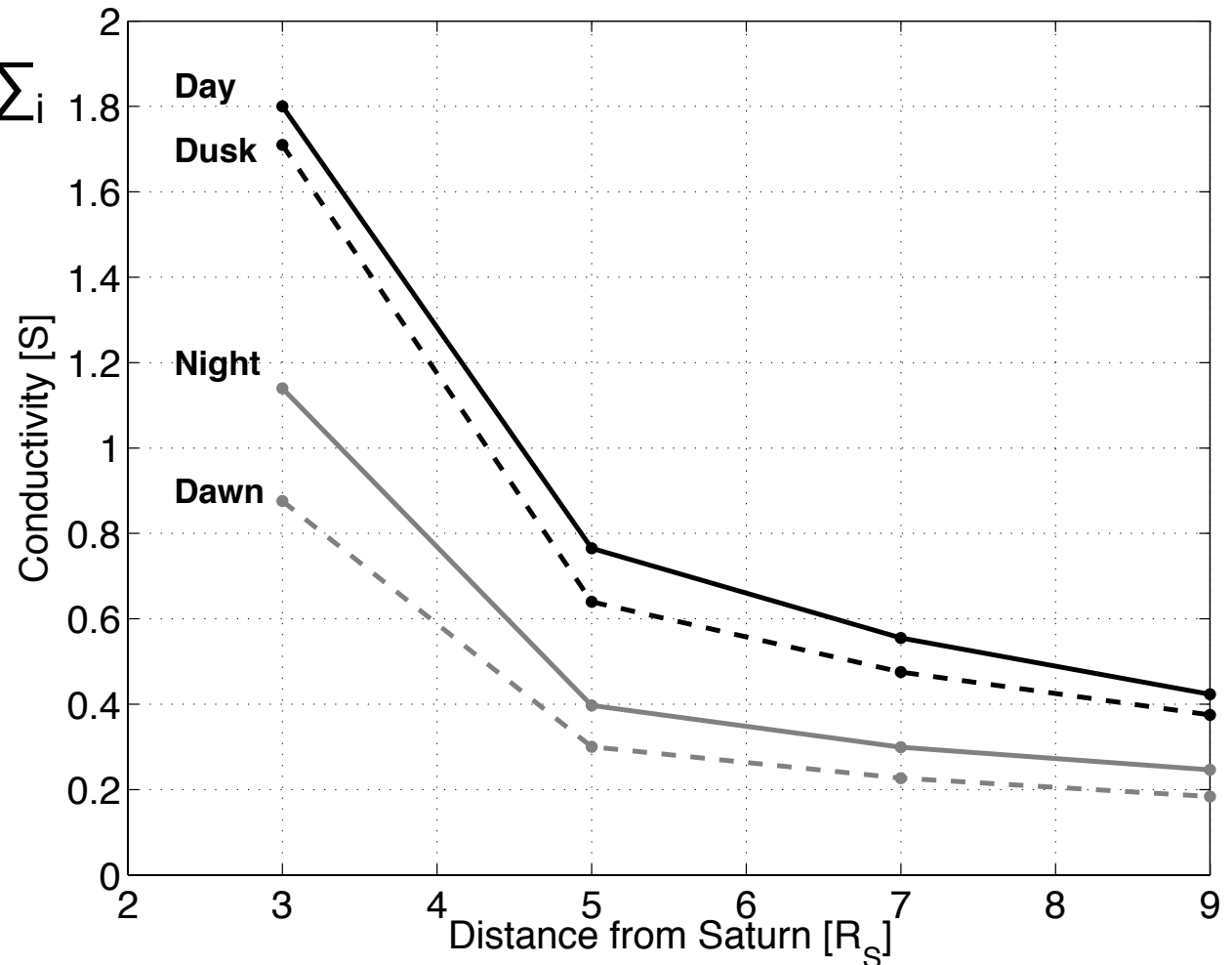


$$\sigma_p = \sum_i \frac{v_i}{v_{in}^2 + \omega_{ci}^2} \frac{n_i e^2}{m_i} + \frac{v_e}{v_{en}^2 + \omega_{ce}^2} \frac{n_e e^2}{m_e}$$

$$\Sigma_i = \int_{z_1}^{z_2} \sigma_p ds$$

Pedersen Conductivity

- LT dependence of Σ_i
- Σ_i decreases with increase of R_s

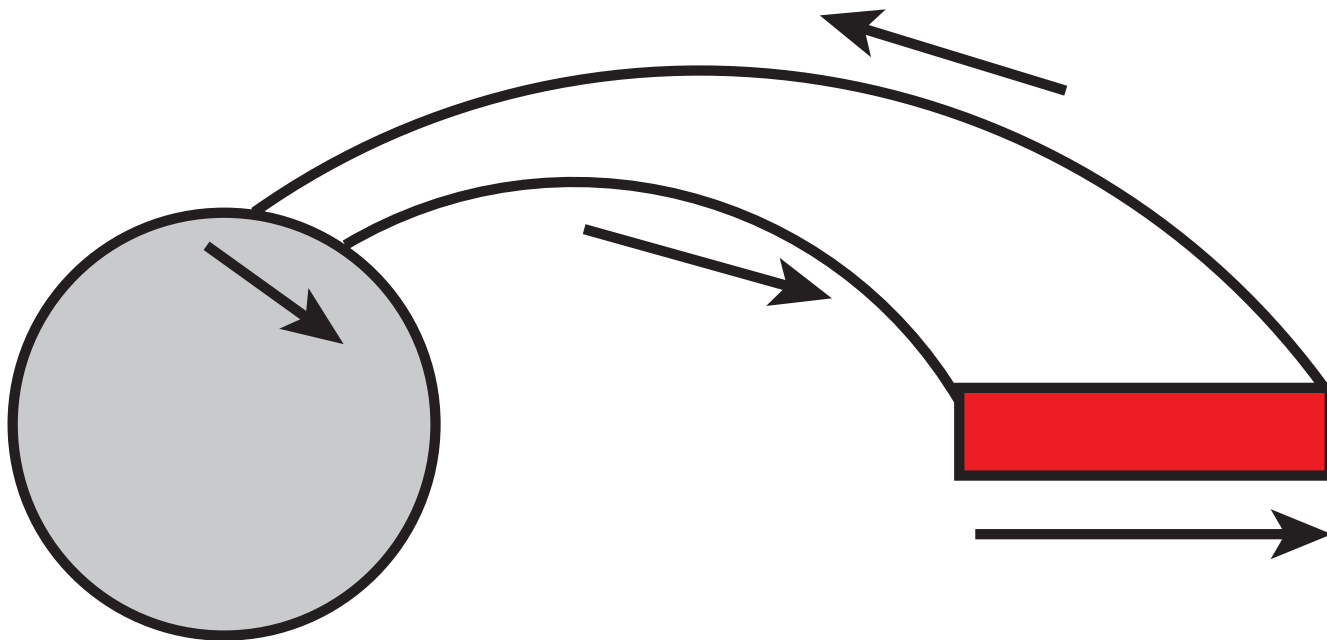


Magnetospheric ion velocity



HOKKAIDO UNIVERSITY

1. Modeling of inner magnetosphere with dust-plasma interaction
2. Modeling of ionosphere
3. Magnetosphere-ionosphere coupling

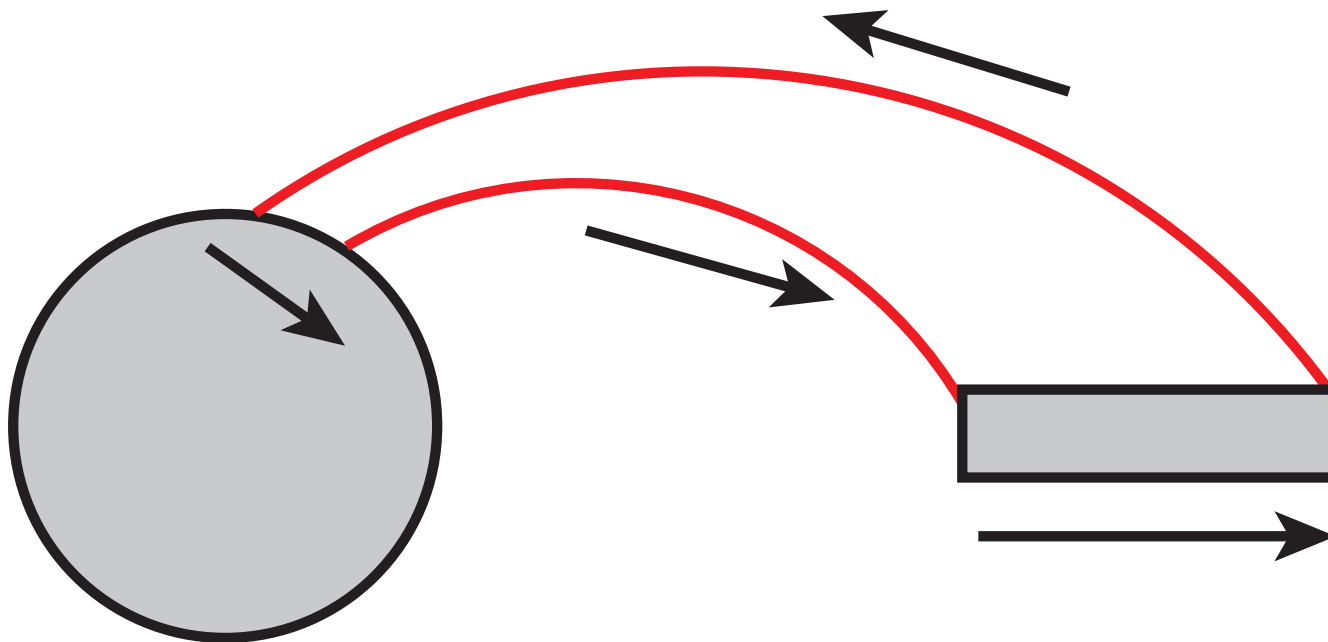


Magnetospheric ion velocity



HOKKAIDO UNIVERSITY

1. Modeling of inner magnetosphere with dust-plasma interaction
2. Modeling of ionosphere
3. Magnetosphere-ionosphere coupling

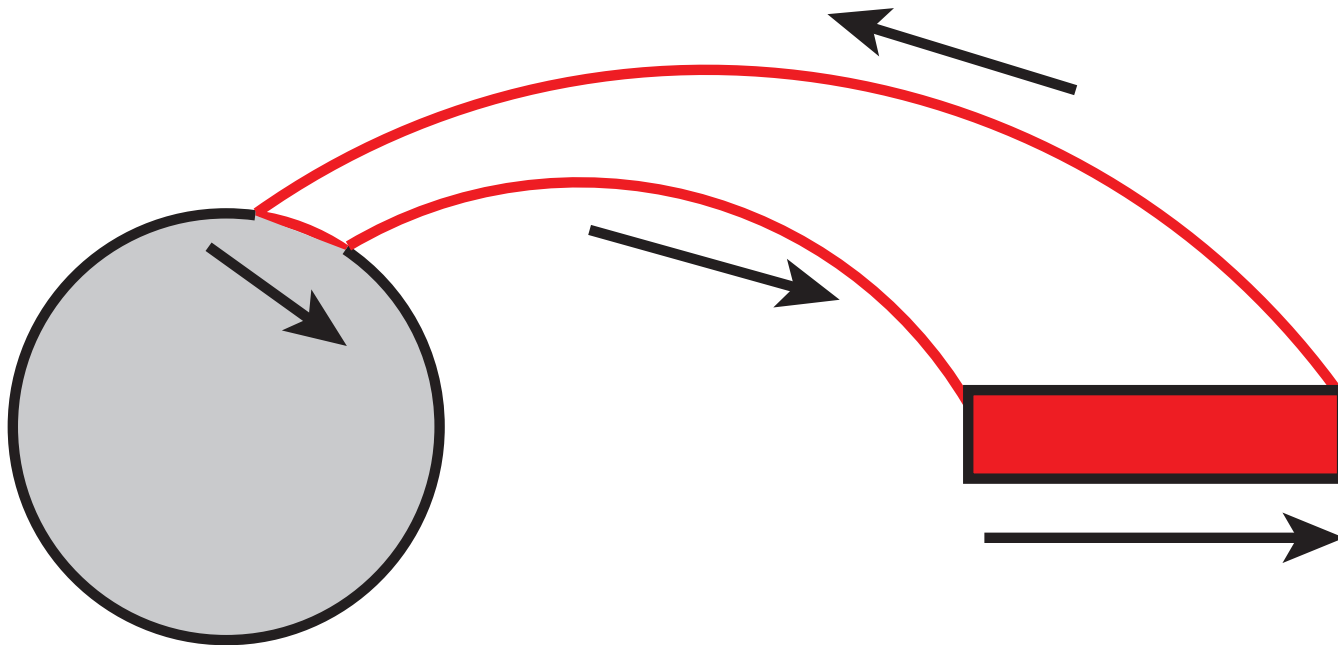


Magnetospheric ion velocity



HOKKAIDO UNIVERSITY

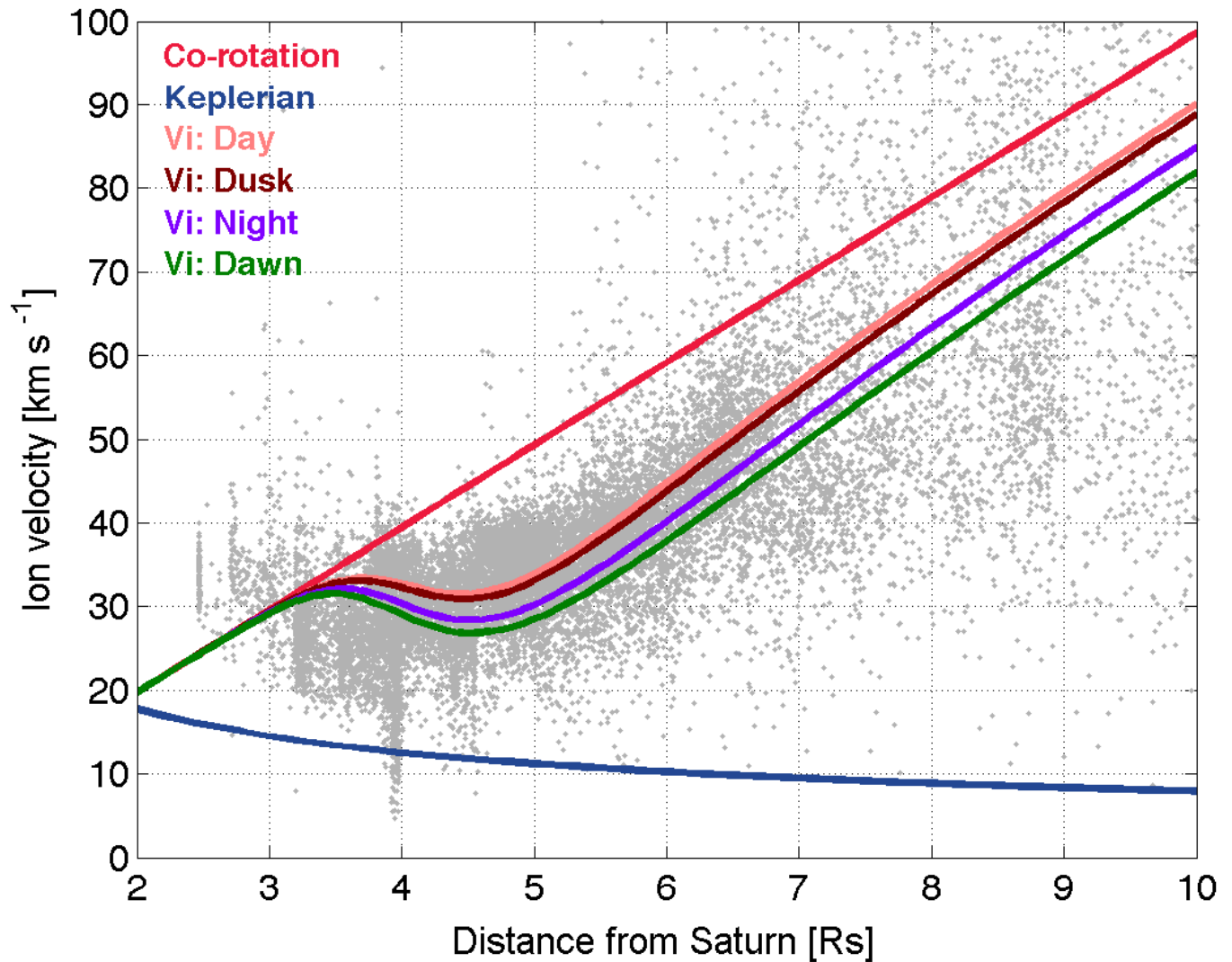
1. Modeling of inner magnetosphere with dust-plasma interaction
2. Modeling of ionosphere
3. Magnetosphere-ionosphere coupling



Magnetospheric ion velocity



$$\Sigma_i (\mathbf{E}_{cor} - \mathbf{E}) = \mathbf{j}D$$



Large dust density, $D=1 R_S$

- V_i depends on LT.

- Ionospheric plasma distribution
 - H_3^+ is dominant at $L=5$.
 - Peak: 10^9 - 10^{10} m^{-3}
 - T_e is much higher than that of previous studies at high altitude.
 - 2000 K at $\sim 1200 \text{ km}$; 10000 K at $\sim 5000 \text{ km}$
 - **Joule heating** and **collision heating** are important at low altitude, and **heat flow** at high altitude.
- Ionospheric conductivity
 - Pedersen conductivity depends on LT.
 - Day \rightarrow Dusk \rightarrow Night \rightarrow Dawn
 - The magnetospheric ion speed shows the same tendency as the diurnal variation of conductivity.

From Observations

- Inner magnetospheric ion speed is slow down from the co-rotation speed.
- Ion speed is Keplerian in the Enceladus plume.

From Modelings

- Ion speed is slow down from the co-rotation speed due to **dust-plasma interaction** and **magnetosphere-ionosphere coupling**.

Reference Works



- **Sakai, S.**, S. Watanabe, M. W. Morooka, M. K. G. Holmberg, J. –E. Wahlund, D. A. Gurnett, and W. S. Kurth (2013), Dust-plasma interaction through magnetosphere-ionosphere coupling in Saturn’s plasma disk, *Planet. Space Sci.*, 75, 11-16, doi:10.1016/j.pss.2012.11.003.
- **Sakai, S.**, and S. Watanabe (2014), High-speed flow and high temperature plasma in Saturn’s mid-latitude ionosphere, in preparation.
- **Sakai, S.**, M. W. Morooka, J. –E Wahlund, and S. Watanabe (2014), Dusty plasma distribution of Enceladus plume observed by Cassini RPWS/LP, in preparation.